

Nuclear reactions in the early universe II

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Organization

Nuclear reactions in the early universe

- Lectures (Paris/E. Grohs)
 - I. Overview of cosmology/Kinetic theory/Big bang nucleosynthesis (BBN)
 - II. Scattering & reaction formalism/Neutrino energy transport
- Workshop sessions (E. Grohs/Paris)
 - I. BBN exercises: compute Nuclear Statistical Equilibrium/electron fraction
 - II. Compute primordial abundances vs $\Omega_b h^2$: code parallelization
- Lecture notes
 - Will be available online (URL TBA)

Outline

Lecture I

- Overview
- Cosmological dynamics in GR
- Big bang nucleosynthesis (BBN)
- Boltzmann equation
 - ▣ Flat & curved spacetime

Lecture II

- Unitary reaction network (URN) of light nuclei
- Neutrino energy transport
- Evan Grohs: observations of primordial abundances

Light nuclear reaction program @ LANL

□ Motivation

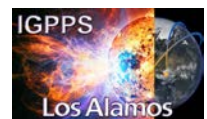
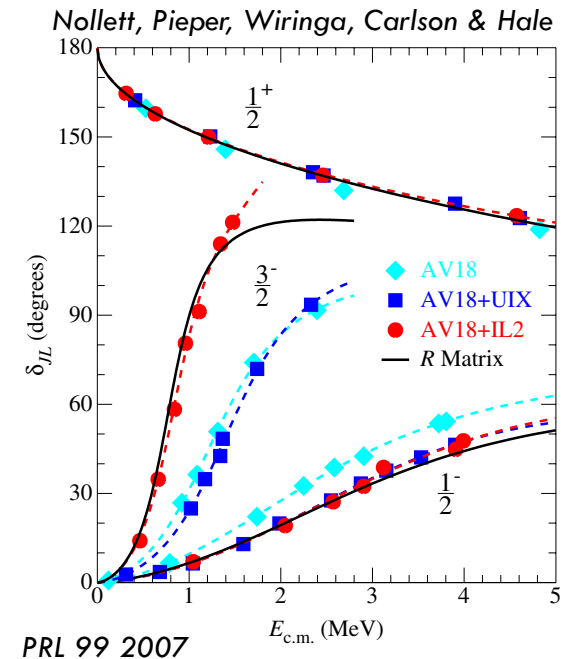
- Data sets: σ , $\sigma(\theta)$, $A_i(\theta)$, $C_{i,j}$, K_i^i , $\Sigma(\gamma)$, ... \rightarrow T matrix \rightarrow resonance spectrum
- **Unitary** parametrization of compound nuclear system
- Applications: **astrophysical**, nuclear security, inertial confinement fusion, **criticality safety**, charge-particle transport, nuclear data (ENDF, ENSDF)

□ Ab initio

- Variational MC; Green's function MC
- GFMC [PRL **99**, 022502 (2007)]
 - n - ^4He phase shifts
 - comparison GFMC/R-matrix
- challenge: multichannel
 - eg. $n\alpha \rightarrow n\alpha$, $n\alpha \rightarrow dt$ & $dt \rightarrow dt$

□ Phenomenology

- R matrix (2 \rightarrow 2 body scatt/reaqs)
- 3-body channels being incorporated



EDA Analyses of Light Systems

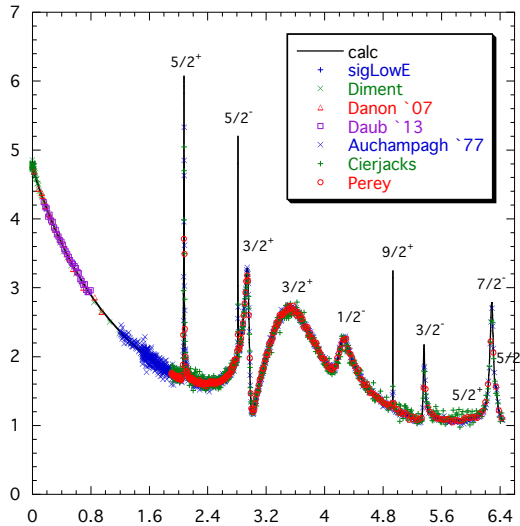
A	System	Channels	Energy Range (MeV)
2	N-N	p+p; n+p, γ +d	0-30 0-40
3	N-d	p+d; n+d	0-4
4	⁴ H ⁴ Li	n+t p+ ³ He	0-20
	⁴ He	p+t n+ ³ He d+d	0-11 0-10 0-10
5	⁵ He	n+ α d+t ⁵ He+ γ	0-28 0-10
	⁵ Li	p+ α d+ ³ He	0-24 0-1.4

Analyses of Light Systems, Cont.

A	System (Channels)
6	${}^6\text{He}$ (${}^5\text{He}+n$, $t+t$); ${}^6\text{Li}$ ($d+{}^4\text{He}$, $t+{}^3\text{He}$); ${}^6\text{Be}$ (${}^5\text{Li}+p$, ${}^3\text{He}+{}^3\text{He}$)
7	${}^7\text{Li}$ ($t+{}^4\text{He}$, $n+{}^6\text{Li}$); ${}^7\text{Be}$ ($\gamma+{}^7\text{Be}$, ${}^3\text{He}+{}^4\text{He}$, $p+{}^6\text{Li}$)
8	${}^8\text{Be}$ (${}^4\text{He}+{}^4\text{He}$, $p+{}^7\text{Li}$, $n+{}^7\text{Be}$, $p+{}^7\text{Li}^*$, $n+{}^7\text{Be}^*$, $d+{}^6\text{Li}$)
9	${}^9\text{Be}$ (${}^8\text{Be}+n$, $d+{}^7\text{Li}$, $t+{}^6\text{Li}$); ${}^9\text{B}$ ($\gamma+{}^9\text{B}$, ${}^8\text{Be}+p$, $d+{}^7\text{Be}$, ${}^3\text{He}+{}^6\text{Li}$)
10	${}^{10}\text{Be}$ ($n+{}^9\text{Be}$, ${}^6\text{He}+\alpha$, ${}^8\text{Be}+nn$, $t+{}^7\text{Li}$); ${}^{10}\text{B}$ ($\alpha+{}^6\text{Li}$, $p+{}^9\text{Be}$, ${}^3\text{He}+{}^7\text{Li}$)
11	${}^{11}\text{B}$ ($\alpha+{}^7\text{Li}$, $\alpha+{}^7\text{Li}^*$, ${}^8\text{Be}+t$, $n+{}^{10}\text{B}$); ${}^{11}\text{C}$ ($\alpha+{}^7\text{Be}$, $p+{}^{10}\text{B}$)
12	${}^{12}\text{C}$ (${}^8\text{Be}+\alpha$, $p+{}^{11}\text{B}$)
13	${}^{13}\text{C}$ ($n+{}^{12}\text{C}$, $n+{}^{12}\text{C}^*$)
14	${}^{14}\text{C}$ ($n+{}^{13}\text{C}$)
15	${}^{15}\text{N}$ ($p+{}^{14}\text{C}$, $n+{}^{14}\text{N}$, $\alpha+{}^{11}\text{B}$)
16	${}^{16}\text{O}$ ($\gamma+{}^{16}\text{O}$, $\alpha+{}^{12}\text{C}$)
17	${}^{17}\text{O}$ ($n+{}^{16}\text{O}$, $\alpha+{}^{13}\text{C}$)
18	${}^{18}\text{Ne}$ ($p+{}^{17}\text{F}$, $p+{}^{17}\text{F}^*$, $\alpha+{}^{14}\text{O}$)

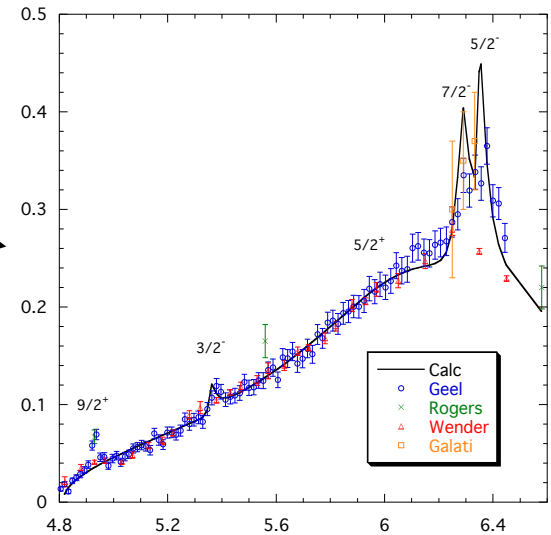
$^{13,14}\text{C}$ system analyses: σ_T (b) vs. E_n (MeV)

$n+^{12}\text{C}$ Total Cross Section

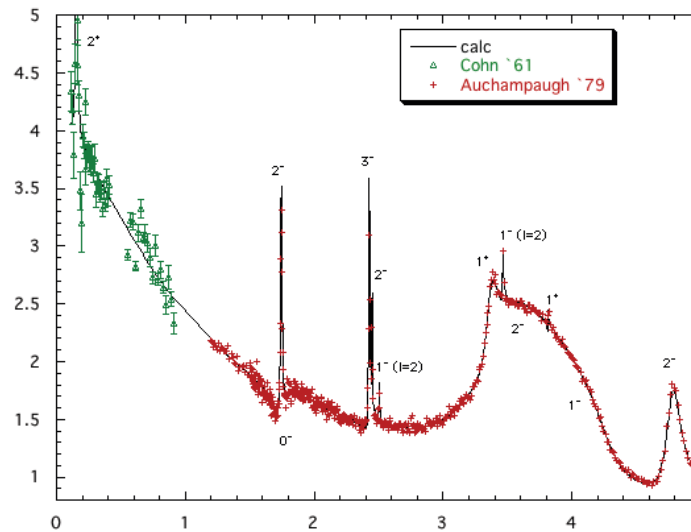


Two-channel analysis

$^{12}\text{C}(n,n')$ Cross Section

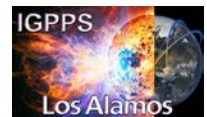


$n+^{13}\text{C}$ Total Cross Section



Single-channel analysis

Analyses by GMH/MWP



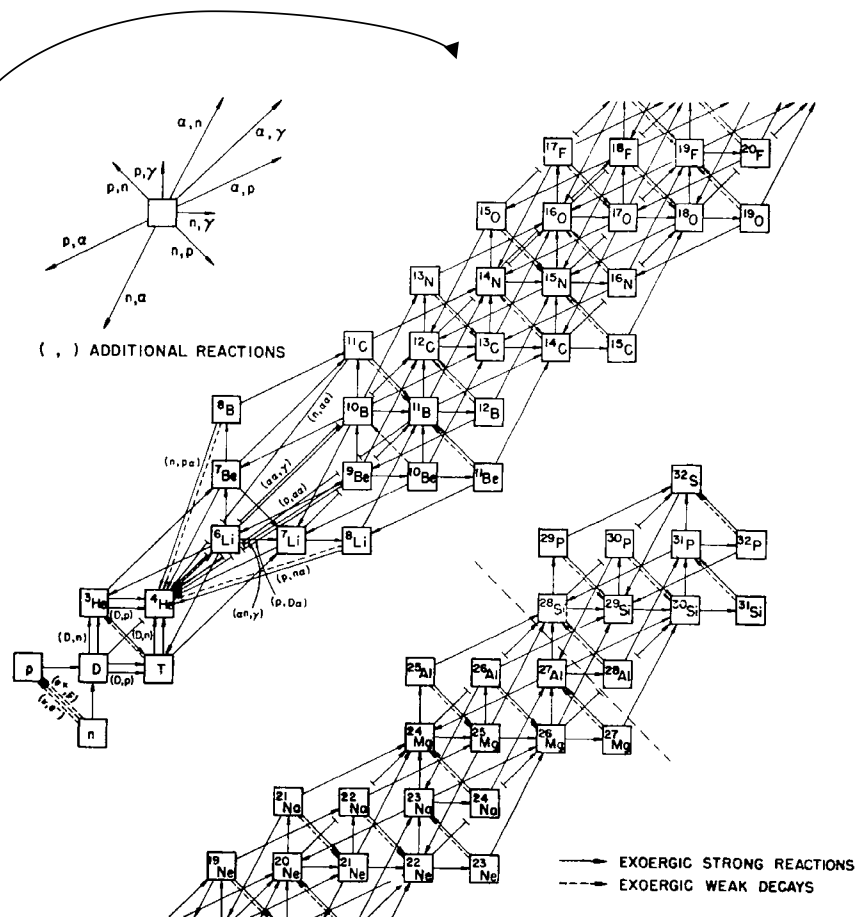
Unitary, self-consistent primordial nucleosynthesis

- State of standard big-bang nucleosynthesis (BBN)
 - d & ^4He abundances: signature success cosmology+nucl astro+astroparticle
 - but there's at least one **Lithium (^7Li) Problem** [^6Li too? See: [Lind et.al. 2013](#)]
 - coming *precision* observations of d, ^4He , η , N_{eff} demand new BBN capabilities
 - resolution of ^7Li problem:
 - observational/stellar astrophysics?
 - **^7Li controversial anomaly: nuclear physics solution?**
 - **new physics?**
- Advance BBN as a tool for precision cosmology
 - incorporate **unitarity** into strong & electroweak interactions (**next slide**)
 - couple **unitary reaction network (URN)** to full Boltzmann transport code
 - neutrino energy distribution function evolution/transport code
 - fully coupled to nuclear reaction network
 - calculate light primordial element abundance for non-standard BBN
 - active-sterile ν mixing
 - massive particle out-of-equilibrium decays \rightarrow energetic active SM particles
 - Produce tools/codes for nuc-astro-particle community: test new physics w/BBN
 - existing codes are based on Wagoner's (1969) code

Nuclear reaction network

- Single-process (non-unitary) analysis
 - $\sigma_{\alpha\beta}(E) \pm \delta \sigma_{\alpha\beta}(E)$ from expt
 - fit form (non-res+narrow res) to $\sigma_{\alpha\beta}(E)$
 - compute $\langle \sigma v \rangle(T) \rightarrow$ reactivity \rightarrow network
 - **NB: norm. systematics can be large**
 - ^{17}O case (below)

- Multi-channel (unitary) analysis
 - Construct unitary parametrization
 - R-matrix (Wigner-Eisenbud '47)
 - simultaneous fit of unpolarized/pol'd scatt/reac data \rightarrow determine T (or S) matrix
 - determines a unitary reaction network (URN) for analyzed compound systems



Wagoner ApJSuppl '69

Boltzmann eq., cross sections, thermal averages

□ Boltzmann equation

□ Toy model, single reaction $\rightarrow \frac{1}{a^3} \frac{d(n_1 a^3)}{dt} = -\langle \sigma v \rangle \left\{ n_1 n_2 - n_3 n_4 \frac{n_1^{(0)} n_2^{(0)}}{n_3^{(0)} n_4^{(0)}} \right\}$

■ Full code has 144 reactions

□ Thermal (Maxwellian) averaged flux(v)*cross section

$$\langle \sigma v \rangle = \left(\frac{8}{\pi \mu} \right)^{1/2} \left(\frac{1}{kT} \right)^{3/2} \int_0^\infty dE E \sigma_{12 \rightarrow 34}(E) e^{-E/kT}$$

□ Energy dependent, angle-integrated cross section is determined from data; Ranking worst \rightarrow best:

- Guess: sometimes necessary when no data/calc. (e.g. TALYS)
- Parametrize resonance data: undesirable since res/non-res related by unitarity; results in model dependent reaction cross section
- Fit to experimental cross section: can be OK; normalization often problematic; subject to sometimes large systematic uncertainty
- Unitary theory: multichannel R-matrix: sure-fire; downside: need multichannel data

Observables from transition (T) matrix

- Scattering matrix: QM amplitude for (i)nitia → (f)inal

$$\langle f|S(E)|i\rangle = \delta_{fi} + 2iT_{fi}(E)$$

- All observables \sim T matrix bilinears

- unpolarized differential cross section

$$\frac{d\sigma_{fi}}{d\Omega} = \frac{4\pi}{k^2} \frac{1}{N_{spins,i}} \sum_{spins,f} |T_{fi}|^2$$

- polarization asymmetry

$$P = \frac{\sigma_{\uparrow\uparrow} - \sigma_{\downarrow\uparrow}}{\sigma_{\uparrow\uparrow} + \sigma_{\downarrow\uparrow}}$$

- Diff cross section \rightarrow int'd cross section \rightarrow thermal averaged

$$\sigma(E) = \int d\Omega \frac{d\sigma}{d\Omega} \rightarrow \langle \sigma v \rangle$$

Unitarity: consequences on T matrix

$$\left. \begin{aligned} \delta_{fi} &= \sum_n S_{fn}^\dagger S_{ni} \\ S_{fi} &= \delta_{fi} + 2i\rho_f T_{fi} \\ \rho_n &= \delta(H_0 - E_n) \end{aligned} \right\} T_{fi} - T_{fi}^\dagger = 2i \sum_n T_{fn}^\dagger \rho_n T_{ni}$$

NB: **unitarity** implies *optical theorem* $\sigma_{\text{tot}} = \frac{4\pi}{k} \text{Im } f(0)$; but *not only* the O.T.

■ Implications of **unitarity** constraint on transition matrix

1. Doesn't uniquely determine T_{ij} ; highly restrictive, however

Elastic: $\text{Im } T_{11}^{-1} = -\rho_1$ (assuming T & P invariance)

Multichannel: $\text{Im } \mathbf{T}^{-1} = -\boldsymbol{\rho}$

2. Unitarity violating transformations

• cannot scale **any** set: $T_{ij} \rightarrow \alpha_{ij} T_{ij} \quad \alpha_{ij} \in \mathbb{R}$

• cannot rotate **any** set: $T_{ij} \rightarrow e^{i\theta_{ij}} T_{ij} \quad \theta_{ij} \in \mathbb{R}$

★ consequence of linear 'LHS' \propto quadratic 'RHS'

3. Unitary parametrizations constrain the experimental data itself

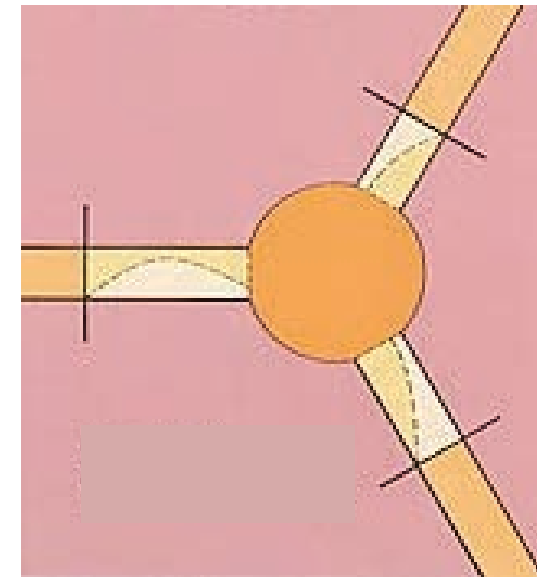
★ *normalization*, in particular

★ case studies: ^{17}O & ^9B compound system

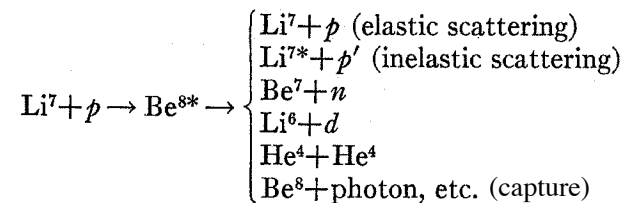
Most important feature:
linear \sim quadratic

Basics of R-matrix (data \Rightarrow amplitudes)

- Assumptions (cf. Lane & Thomas RMP '58)
 - a) Non-relativistic QM (L&T58); LANL-EDA uses rel.
 - b) Two-body channels only ('c'); aux. spectra code
 - c) Conservation of N, Z
 - d) Finite radius a_c beyond $V_{\text{pol}} \approx 0$; sharp boundaries
- Separated pairs, "channels"
 - A nucleons $\rightarrow (A_1, A_2)$
 - $c = \{\alpha s_1 m_1 s_2 m_2\} \rightarrow \{\alpha (s_1 s_2) s m_s \ell m_\ell\} \rightarrow \{\alpha (s_1 s_2) s \ell, JM\}$
 - Assume $a_c = a_\alpha \rightarrow$ many c have same channel in configuration space
- Channel surface
 - Consider configuration space of $3A$ dimensions
 - Set of points: $\cup_c r_{\alpha(c)} = a_{\alpha(c)}$
 - Surfaces coincide but assumed to have negl. prob.
 - Channels are cylinders normal to channel surf.



Example: ${}^8\text{Be}$ compound system

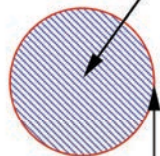


R-matrix formalism

INTERIOR (Many-Body) REGION
(Microscopic Calculations)

ASYMPTOTIC REGION
(S-matrix, phase shifts, etc.)

$H + \mathcal{L}_B$
compact, hermitian
operator with real,
discrete spectrum;
eigenfunctions in
Hilbert space



$$|\psi^+\rangle = (H + \mathcal{L}_B - E)^{-1} \mathcal{L}_B |\psi^+\rangle$$

Measurements

$$\langle r_{c'} | \psi_c^+ \rangle = -I_{c'}(r_{c'}) \delta_{c'c} + O_{c'}(r_{c'}) S_{c'c}$$

SURFACE

$$\mathcal{L}_B = \sum_c |c\rangle \langle c| \left(\frac{\partial}{\partial r_c} r_c - B_c \right),$$

$$\langle \mathbf{r}_c | c \rangle = \frac{\hbar}{\sqrt{2\mu_c a_c}} \frac{\delta(r_c - a_c)}{r_c} \left[(\phi_{s_1}^{\mu_1} \otimes \phi_{s_2}^{\mu_2})_s^\mu \otimes Y_l^m(\hat{\mathbf{r}}_c) \right]_j^M$$

$$R_{c'c} = \langle c' | (H + \mathcal{L}_B - E)^{-1} | c \rangle = \sum_\lambda \frac{\langle c' | \lambda \rangle \langle \lambda | c \rangle}{E_\lambda - E}$$

Bloch operator $\mathcal{L}_B = \sum_c |c\rangle \langle c| \left[\frac{\partial}{\partial r_c} r_c - B_c \right]$ ensures
Hermiticity of Hamiltonian restricted to internal region

□ R-matrix theory: **unitary**,
multichannel parametrization
of (not just resonance) data

□ Interior/Exterior regions

- Interior: strong interactions
- Exterior: Coulomb/non-polarizing interactions
- Channel surface

$$\mathcal{S}_c : r_c = a_c \quad \mathcal{S} = \sum_c \mathcal{S}_c$$

□ R-matrix elements

- Projections on channel surface
functions $\langle \mathbf{r}_c | c \rangle$ of Green's
function

$$G_B = [H + \mathcal{L}_B - E]^{-1}$$

- Boundary conditions

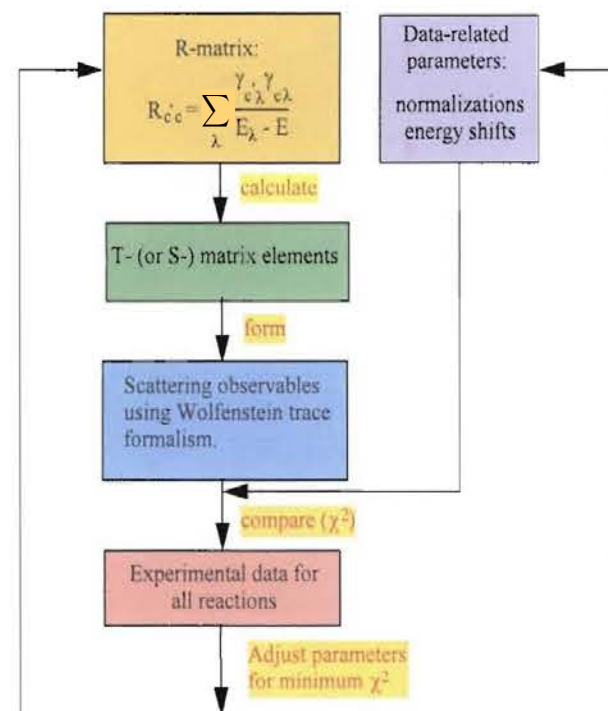
$$B_c = \frac{1}{u_c(a_c)} \frac{du_c}{dr_c} \Big|_{r_c=a_c}$$

R-matrix implementation in EDA

- EDA = Energy Dependent Analysis
 - Adjust E_λ & $\gamma_{c\lambda}$
- Any number of two-body channels
 - Arbitrary spins, masses, charges (zero mass)
- Scattering observables
 - Wolfenstein trace formalism
- Data
 - Normalization
 - Energy shifts
 - Energy resolution/spread
- Fit (rank-1 var. metric) solution

$$\chi_{EDA}^2 = \sum_i \left[\frac{nX_i(\mathbf{p}) - R_i}{\delta R_i} \right]^2 + \left[\frac{nS - 1}{\delta S/S} \right]^2$$

- Covariance determined



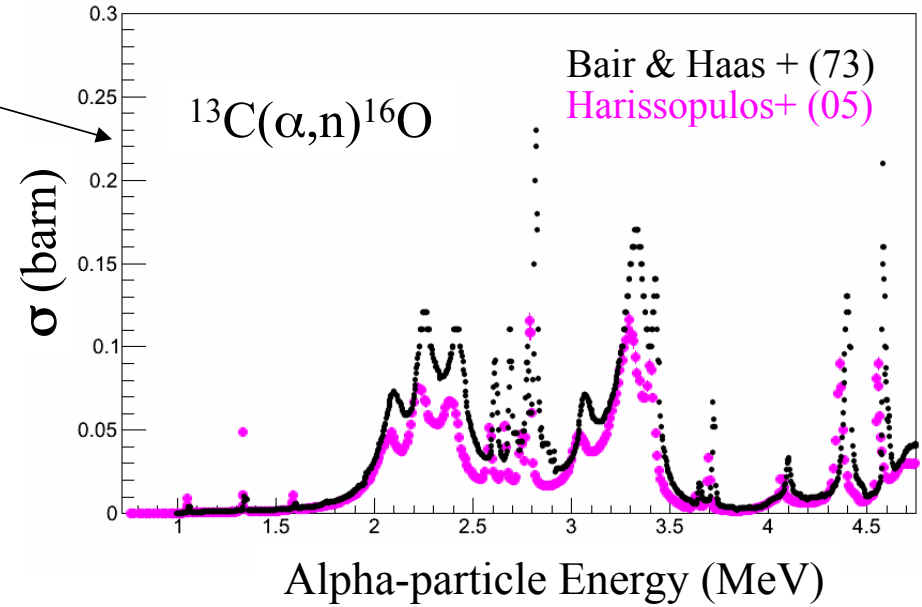
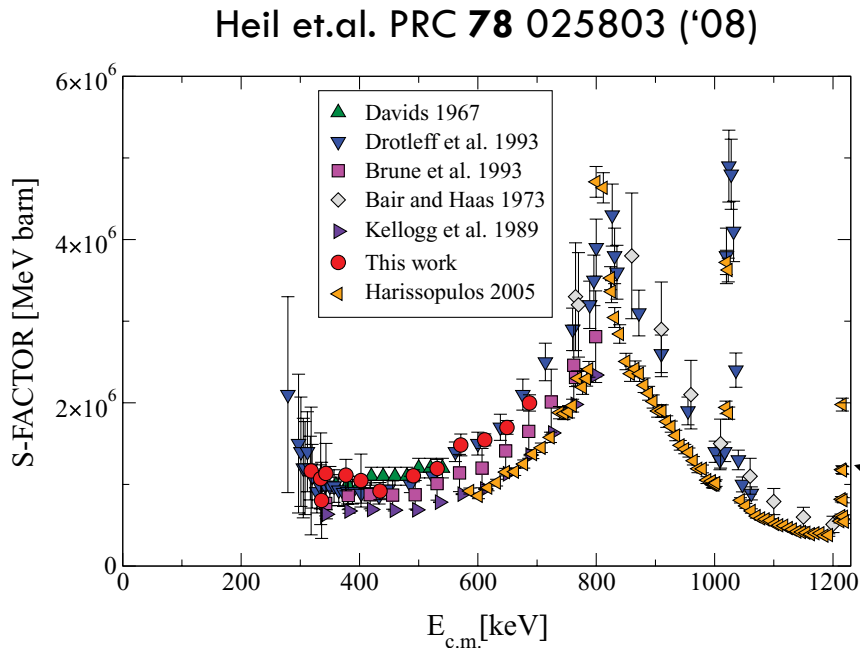
^{17}O analysis configuration

Channel	a_c (fm)	l_{\max}
$n+^{16}\text{O}$	4.3	4
$\alpha+^{13}\text{C}$	5.4	5

Reaction	Energies (MeV)	# data points	Data types
$^{16}\text{O}(n,n)^{16}\text{O}$	$E_n = 0 - 7$	2718	$\sigma_T, \sigma(\theta), P_n(\theta)$
$^{16}\text{O}(n,\alpha)^{13}\text{C}$	$E_n = 2.35 - 5$	850	$\sigma_{\text{int}}, \sigma(\theta), A_n(\theta)$
$^{13}\text{C}(\alpha,n)^{16}\text{O}$	$E_\alpha = 0 - 5.4$	874	σ_{int}
$^{13}\text{C}(\alpha,\alpha)^{13}\text{C}$	$E_\alpha = 2 - 5.7$	1296	$\sigma(\theta)$
total		5738	8

^{17}O compound system: experimental status

Recent (Harissopulos '05) measurement
 $^{13}\text{C}(\alpha, n)^{16}\text{O}$ vs. older (Bair & Haas '73)



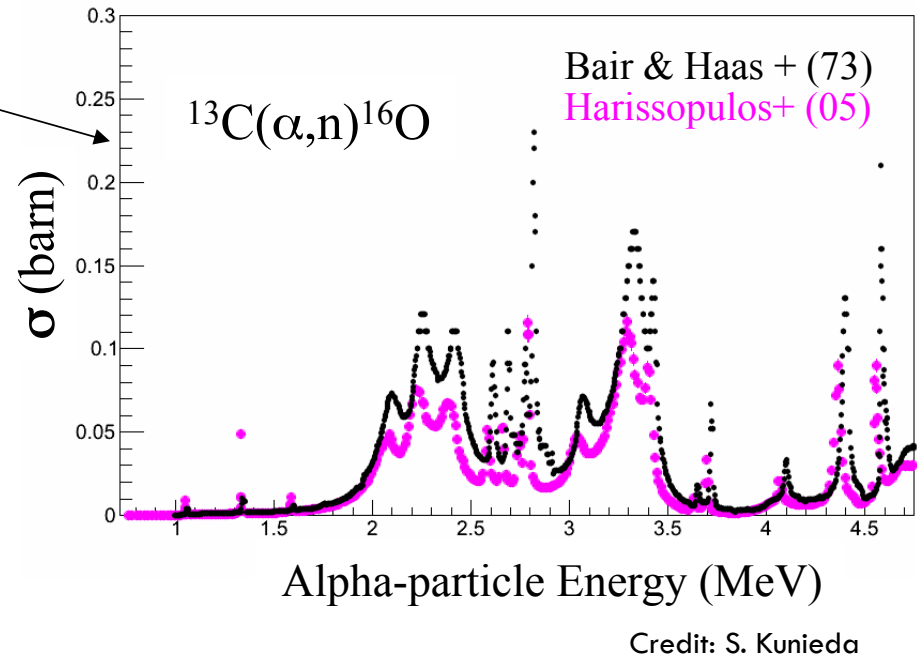
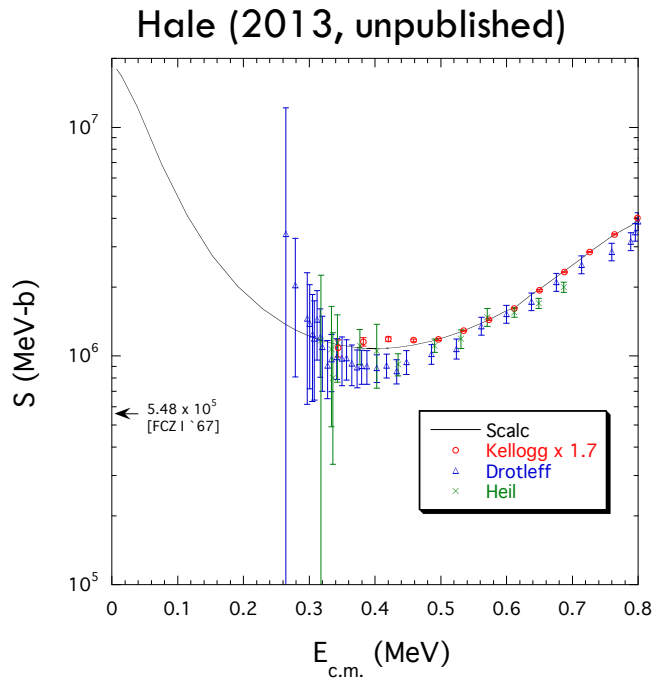
Credit: S. Kunieda

Harissopulos(05) data $2/3 \times$ B&H(73)
 Heil(08) data consistent with B&H

Tempting to conclude that B&H73 was right all along!

^{17}O compound system: experimental status

Recent (Harissopulos '05) measurement
 $^{13}\text{C}(\alpha, n)^{16}\text{O}$ vs. older (Bair & Haas '73)



Subthreshold $\frac{1}{2}^+$
 deep min in σ_T
 $S(0) \gg S_{\text{FCZ67}}(0)$

Tempting to conclude that B&H73 was right all along!

R-matrix analyses support B&H73/Heil08

LANL R-matrix fit to Bair&Haas73

two-channel fit: ($^{16}\text{O}, n$) & ($^{13}\text{C}, \alpha$)

$\ell_n = 0, \dots, 4; \quad \ell_\alpha = 0, \dots, 5$

data included: $\sigma_T(E)$

$^{16}\text{O}(n, n), ^{16}\text{O}(n, \alpha), ^{13}\text{C}(\alpha, n)$

$\sigma_{el}, d\sigma/d\Omega, A_y$

χ^2 min: normalizations float

Test Hariss05 data

remove B&H73/Heil08 data

fix Hariss05 norm to unity

unable to obtain fit $\chi^2 (< 2.0)$

now allow Hariss05 norm to float

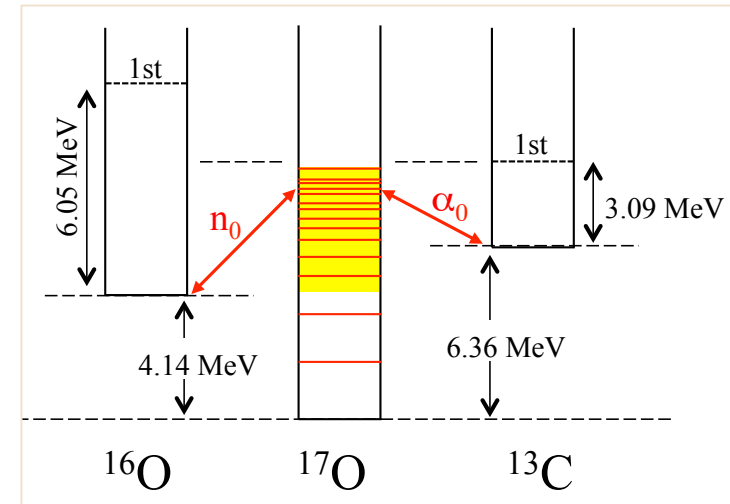
requires scale factor of ~ 1.5 , consistent with B&H73

Kunieda/Kawano analysis [2013]

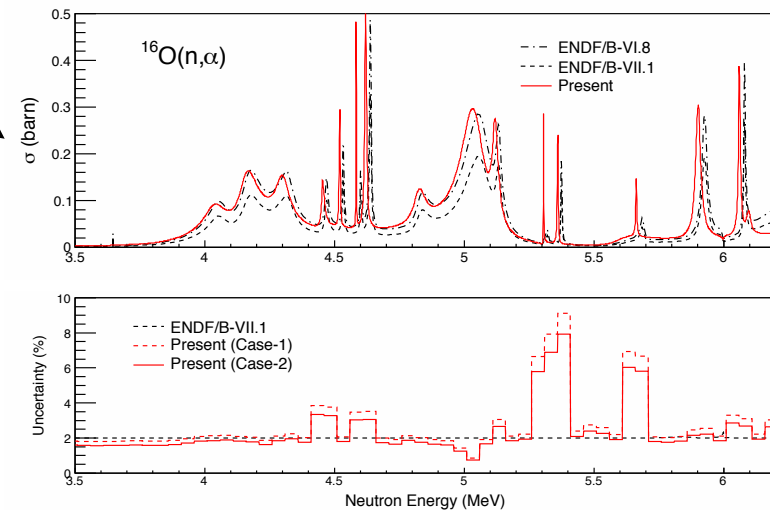
cf. LANL R-matrix(EDA)/ENDF/B-VI.8

with independent R-matrix code

Right to conclude B&H73 data correct on the basis of unitarity!



Credit: S. Kunieda



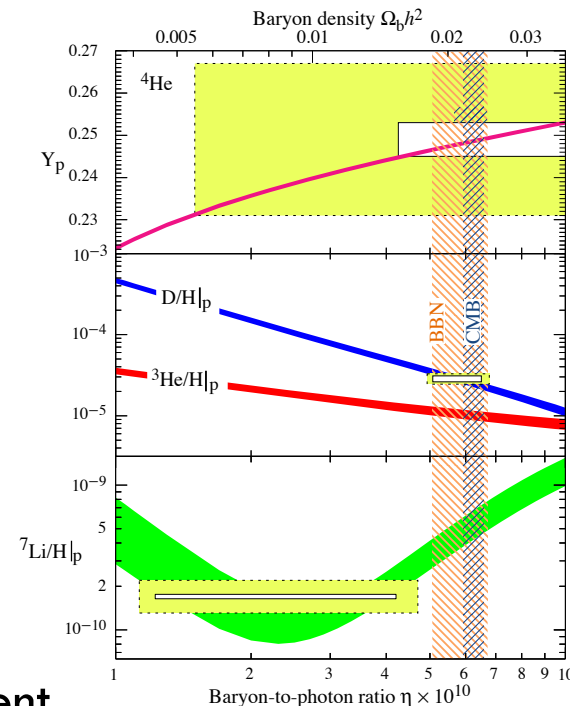
Toward a unitary reaction network for BBN

□ Primordial nucleosynthesis

- Can unitarity play a role in precision BBN?
- $D, {}^4\text{He}$ abund. agree with theo/expl uncertainties
- At η_{wmap} (CMB) ${}^7\text{Li}/\text{H}|_{\text{BBN}} \sim (2.2-4.2) * {}^7\text{Li}/\text{H}|_{\text{halo}}$ *
- Discrepancy $\sim 4.5-5.5 \sigma \rightarrow$ the “Li problem”

□ Resonant destruction ${}^7\text{Li}$

- Prod. mass 7 “well understood”; destruction not
- Cyburt & Pospelov [arXiv:0906.4373](https://arxiv.org/abs/0906.4373); *IJMPE*, 21(2012)
 - ${}^7\text{Be}(d,p) \alpha \alpha$ & ${}^7\text{Be}(d, \gamma) {}^9\text{B}$ resonant enhancement
 - Identify ${}^9\text{B} E_{5/2+} \approx 16.7 \text{ MeV} \approx E_{\text{thr}}(d+{}^7\text{Be}) + 200 \text{ keV}$
 - *Near threshold*
 - $(E_r, \Gamma_d) \approx (170-220, 10-40) \text{ keV}$ solve Li problem
- ‘Large’ widths
 - Conclude “large channel radius” required



NB: both approaches assume validity of TUNL-NDG tables

${}^9\text{B}$ analysis: included data

- ${}^6\text{Li}+{}^3\text{He}$ elastic *Buzhinski et.al., Izv. Rossiiskoi Akademii Nauk, Ser.Fiz., Vol.43, p.158 (1979)*
 - Differential cross section
 - $1.30 \text{ MeV} < E({}^3\text{He}) < 1.97 \text{ MeV}$
- ${}^6\text{Li}+{}^3\text{He} \rightarrow \text{p}+{}^8\text{Be}^*$ *Elwyn et.al., Phys. Rev. C 22, 1406 (1980)*
 - Integrated cross section
 - Quasi-two-body, excited-state, summed final channel
 - $0.66 \text{ MeV} < E({}^3\text{He}) < 5.00 \text{ MeV}$
- ${}^6\text{Li}+{}^3\text{He} \rightarrow \text{d}+{}^7\text{Be}$ *D.W. Barr & J.S. Gilmore, unpublished (1965)*
 - Integrated cross section
 - $0.42 \text{ MeV} < E({}^3\text{He}) < 4.94 \text{ MeV}$
- ${}^6\text{Li}+{}^3\text{He} \rightarrow \gamma + {}^9\text{B}$ *Aleksic & Popic, Fizika 10, 273-278 (1978)*
 - Integrated cross section
 - $0.7 \text{ MeV} < E({}^3\text{He}) < 0.825 \text{ MeV}$
 - New to ${}^9\text{B}$ analysis
- New evaluation
 - Separate ${}^8\text{Be}^*$ states
 - 2^+ @200 keV [16.9 MeV], 1^+ @650 keV [17.6 MeV], 1^+ @1.1 MeV[18.2 MeV]
 - $\text{n}+{}^8\text{B}$: $E_{\text{thresh}}({}^3\text{He}) = 3 \text{ MeV}$
 - Simultaneous analysis with ${}^9\text{Be}$ mirror system

Data accessed via
EXFOR/CSISRS
database (C4 format)

R-matrix configuration in EDA code

Hadronic channels (in blue, not included)

$A_1 A_2 \pi$	${}^3\text{He}{}^6\text{Li}^+(1)$		$p{}^8\text{Be}^{*+}(2)$		$d{}^7\text{Be}^-(3)$		
ℓ \ / S	$\frac{3}{2}$	$\frac{1}{2}$	$\frac{5}{2}$	$\frac{3}{2}$	$\frac{5}{2}$	$\frac{3}{2}$	$\frac{1}{2}$
0	${}^4S_{3/2}$	${}^2S_{1/2}$	${}^6S_{5/2}$	${}^4S_{3/2}$	${}^6S_{5/2}$	${}^4S_{3/2}$	${}^2S_{1/2}$
1	${}^4P_{5/2,3/2,1/2}$	${}^2P_{3/2,1/2}$	${}^6P_{7/2,5/2,3/2}$	${}^4P_{5/2,3/2,1/2}$	${}^6P_{7/2,5/2,3/2}$	${}^4P_{5/2,3/2,1/2}$	${}^2P_{3/2,1/2}$
2	${}^4D_{7/2,5/2,3/2,1/2}$	${}^2D_{5/2,3/2}$	${}^6D_{9/2,7/2,5/2,3/2,1/2}$	${}^4D_{7/2,5/2,3/2,1/2}$	${}^6D_{9/2,7/2,5/2,3/2,1/2}$	${}^4D_{7/2,5/2,3/2,1/2}$	${}^2D_{5/2,3/2}$
$E_{\text{thr}}(\text{CM, MeV})$	16.6		16.7		16.5		

Electromagnetic channel:

$$\gamma + {}^9\text{B} \rightarrow E_1^{3/2}, M_1^{5/2}, M_1^{3/2}, M_1^{1/2}, E_1^{5/2}, E_1^{1/2}$$

Full model space:

state number;

channel pair;

LS; J; channel

radius [fm]

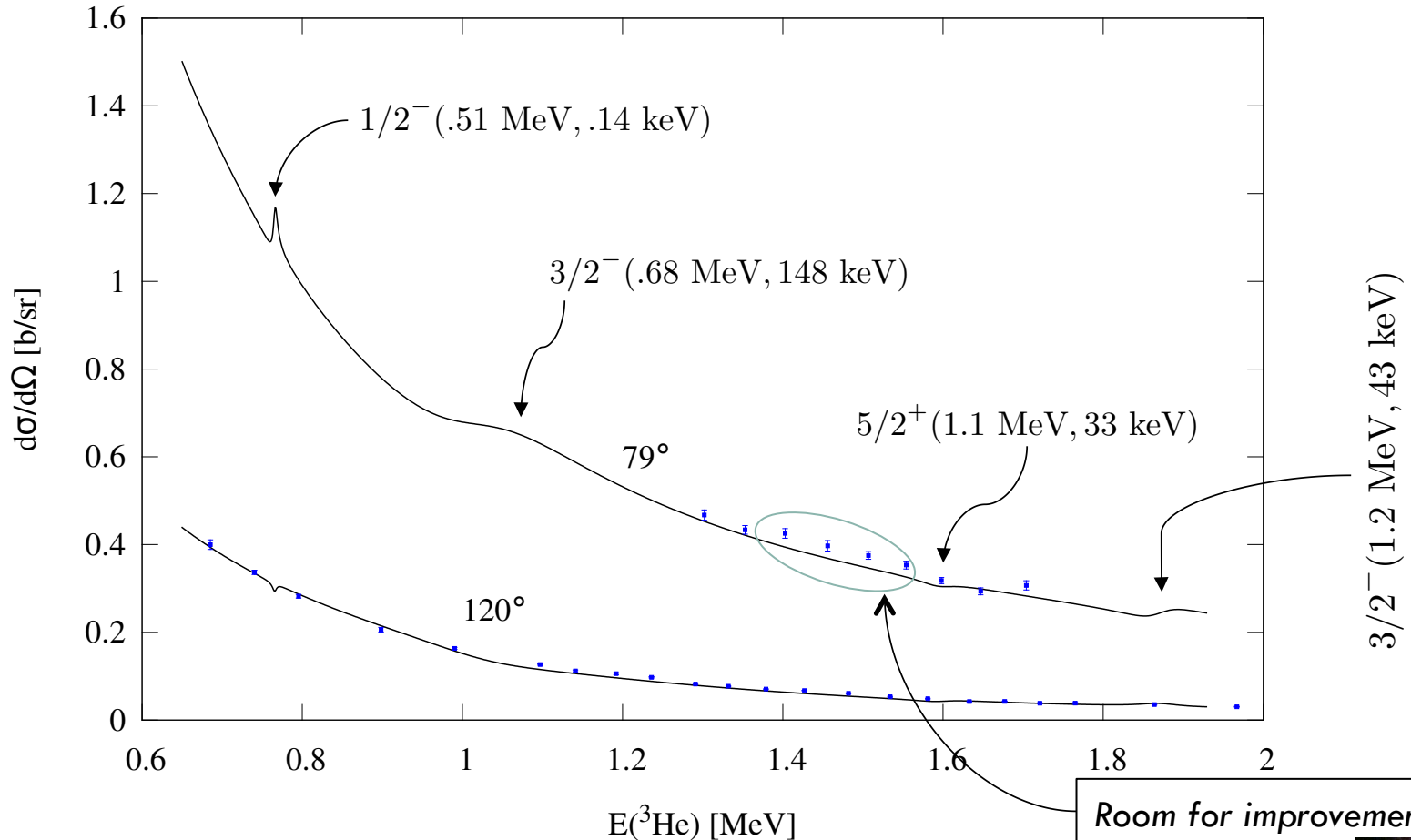
1	1 4s 3/2	7.50000000f	20	1 4p 1/2	7.50000000f
2	1 4d 3/2	7.50000000f	21	1 2p 1/2	7.50000000f
3	1 2d 3/2	7.50000000f	22	2 4p 1/2	5.50000000f
4	2 4s 3/2	5.50000000f	23	3 2s 1/2	7.00000000f
5	3 6p 3/2	7.00000000f	24	4 M1 1/2	50.00000000f
6	3 4p 3/2	7.00000000f	25	1 4d 7/2	7.50000000f
7	3 2p 3/2	7.00000000f	26	3 6p 7/2	7.00000000f
8	4 E1 3/2	50.00000000f	27	1 4d 5/2	7.50000000f
9	1 4p 5/2	7.50000000f	28	1 2d 5/2	7.50000000f
10	2 6p 5/2	5.50000000f	29	2 6s 5/2	5.50000000f
11	2 4p 5/2	5.50000000f	30	3 6p 5/2	7.00000000f
12	3 6s 5/2	7.00000000f	31	3 4p 5/2	7.00000000f
13	4 M1 5/2	50.00000000f	32	4 E1 5/2	50.00000000f
14	1 4p 3/2	7.50000000f	33	1 4d 1/2	7.50000000f
15	1 2p 3/2	7.50000000f	34	1 2s 1/2	7.50000000f
16	2 6p 3/2	5.50000000f	35	3 4p 1/2	7.00000000f
17	2 4p 3/2	5.50000000f	36	3 2p 1/2	7.00000000f
18	3 4s 3/2	7.00000000f	37	4 E1 1/2	50.00000000f
19	4 M1 3/2	50.00000000f	38	2 6p 7/2	5.50000000f



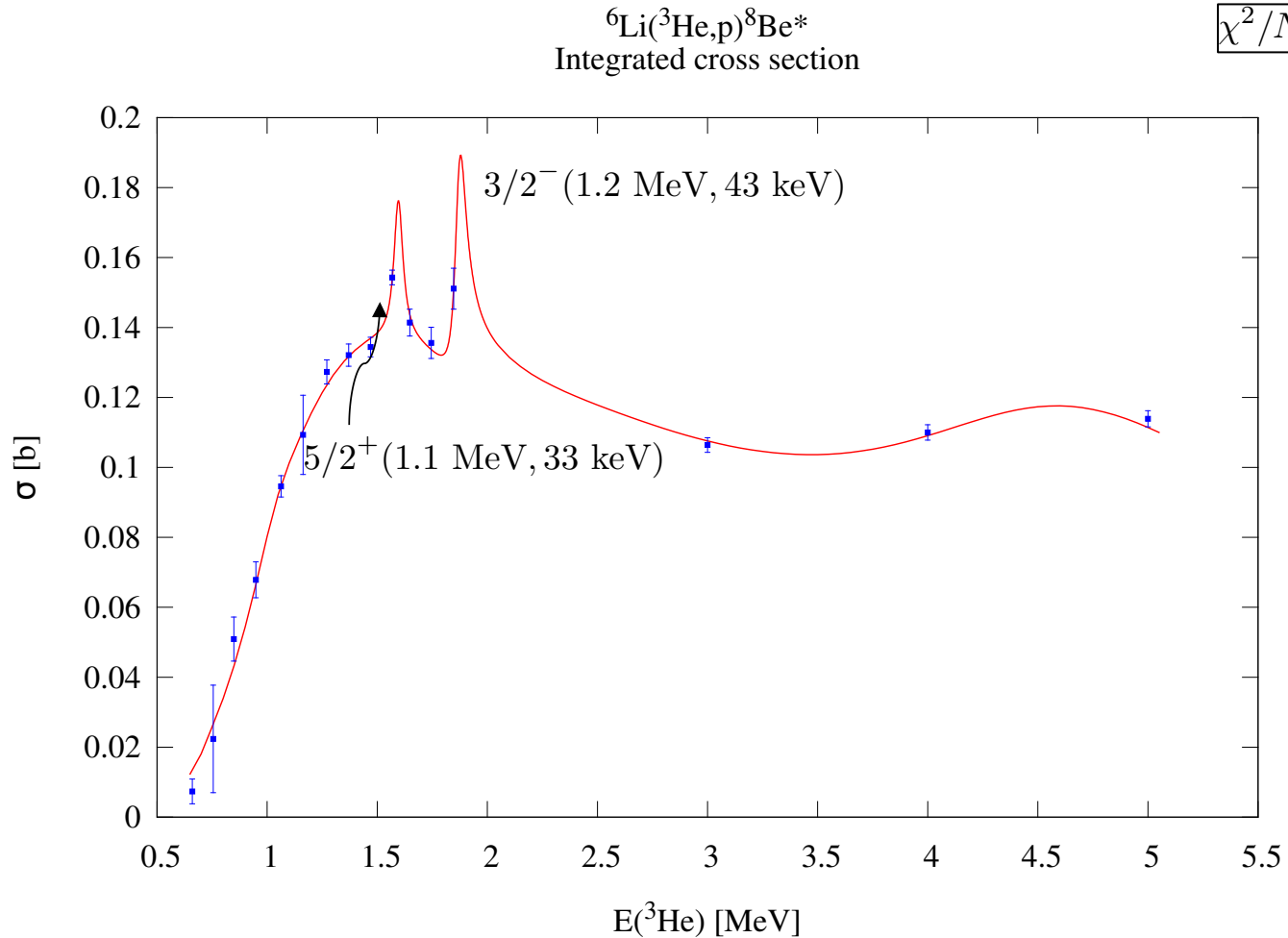
Observable fit: ${}^3\text{He}+{}^6\text{Li}$ elastic DCS

${}^6\text{Li}({}^3\text{He},\text{Elastic})$
Differential cross section

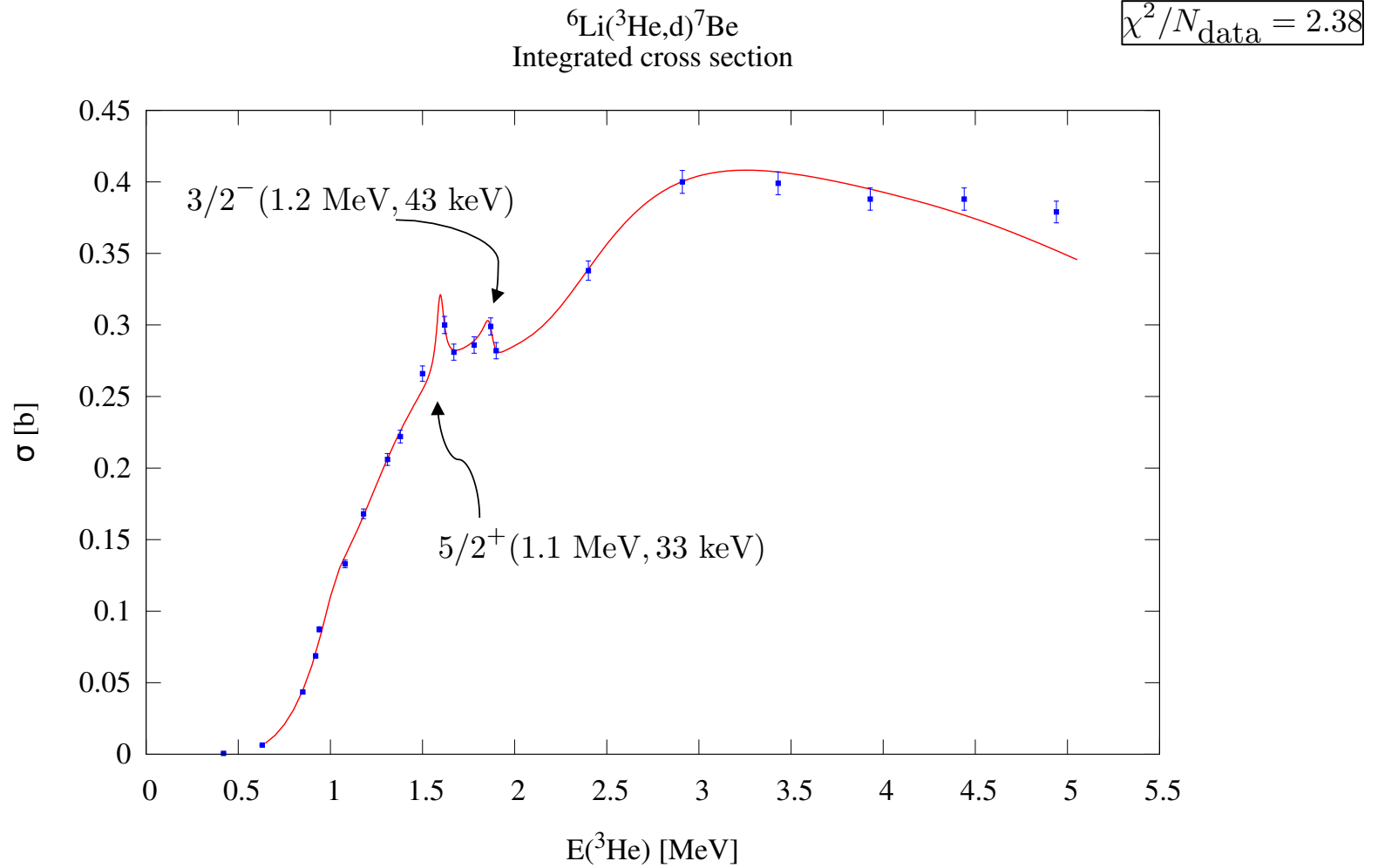
$\chi^2/N_{\text{data}} = 1.91$



Observable fit: ${}^6\text{Li}({}^3\text{He},p){}^8\text{Be}^*$ integrated x-sec



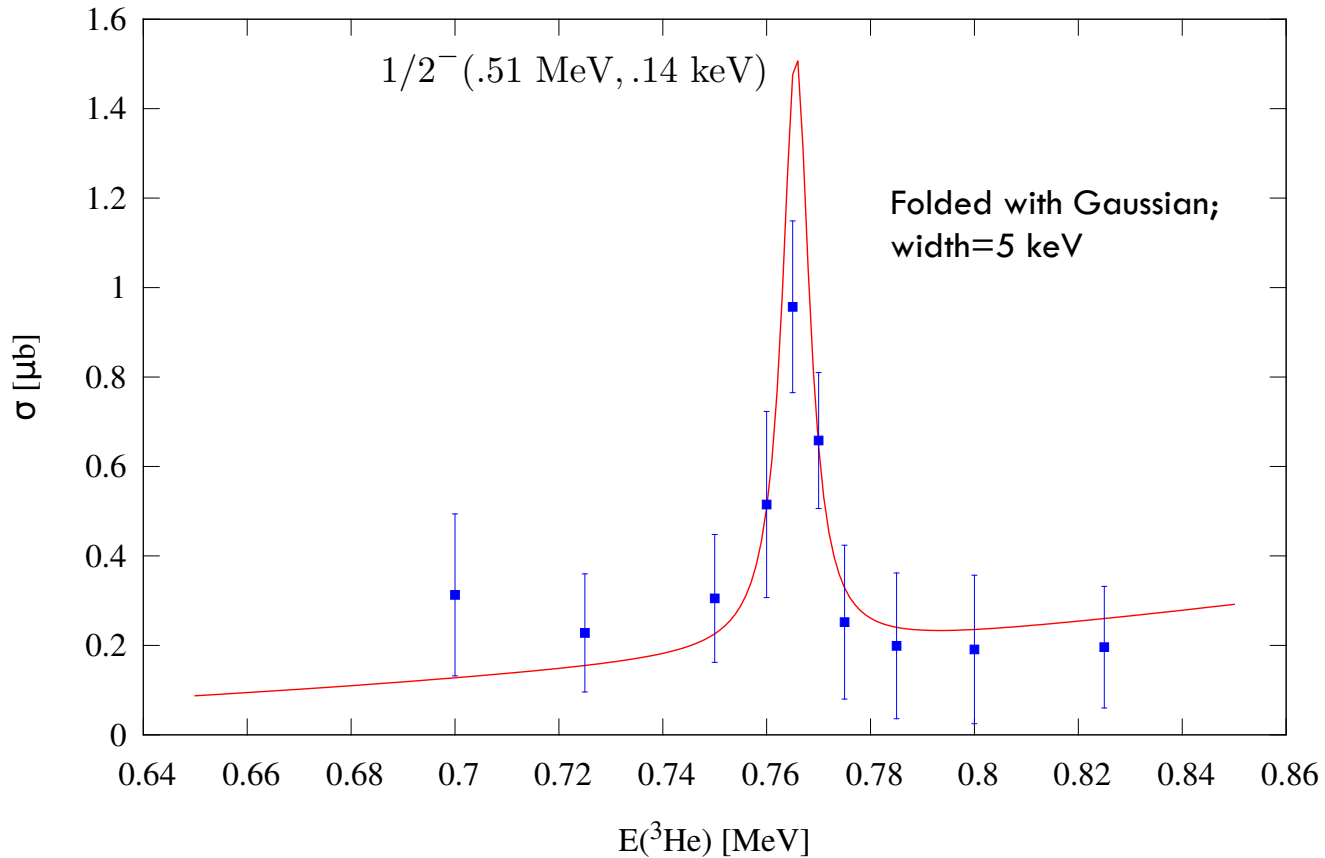
Observable fit: ${}^6\text{Li}({}^3\text{He},d){}^7\text{Be}$ integrated x-sec



Observable fit: ${}^6\text{Li}({}^3\text{He}, \gamma){}^9\text{B}$ integrated x-sec

$$\chi^2/N_{\text{data}} = 0.37$$

${}^6\text{Li}({}^3\text{He}, \gamma){}^9\text{B}$
Integrated cross section



^9B analysis result: resonance structure

Ex (MeV)	Jpi	Gamma (keV)	Er (MeV)	ImEr (MeV)	E (3He)	Strength
16.46539	1/2-	768.46	-.1369	-0.3842	-0.2054	0.06 weak
17.11317	1/2-	0.14	0.5109	-0.6771E-04	0.7664	1.00 strong
17.20115	5/2-	871.63	0.5989	-0.4358	0.8984	0.40 weak
17.28086	3/2-	147.78	0.6785	-0.0739	1.0178	0.77 strong
17.66538	5/2+	33.33	1.0631	-0.0167	1.5947	0.98 strong
17.83619	7/2+	2036.21	1.2339	-1.0181	1.8509	0.15 weak
17.84773	3/2-	42.52	1.2454	-0.0213	1.8681	0.97 strong
18.04821	3/2+	767.11	1.4459	-0.3836	2.1689	0.54 weak
18.42292	1/2+	5446.32	1.8206	-2.7232	2.7309	0.03 weak
18.67716	1/2-	10278.41	2.0749	-5.1392	3.1124	0.15 weak
19.60923	3/2-	1478.22	3.0069	-0.7391	4.5104	0.52 weak

TUNL-NDG/ENSDF
parameters

**NB: no strong resonance seen
~100 keV of $^3\text{He}+^6\text{Li}$ threshold**

E_x^a (MeV keV)	$J^\pi; T$	Γ_{cm} (keV)	Decay
16 024 25	$T = (\frac{1}{2})$	180 16	
16 71 100 ^h	$(\frac{5}{2}^+); (\frac{1}{2})$		
17 076 4	$\frac{1}{2}^-; \frac{3}{2}$	22 5	$(\gamma, ^3\text{He})$
17 190 25		120 40	p, d, ^3He
17 54 100 ^{hi}	$(\frac{7}{2}^+); (\frac{1}{2})$		
17 637 10 ⁱ		71 8	p, d, $^3\text{He}, \alpha$

Summary

- Provided overview of current work in the LANL light nuclear reaction program
- Emphasize the utility of multichannel, unitary parametrization of light nuc data
 - ^{17}O norm issue: are Bair & Haas '73 data conclusive?
 - ^9B resonance spectrum:
 - no resonances in ^9B that reside within ~ 200 (~ 100) keV of the $d+^7\text{Be}$ ($^3\text{He}+^6\text{Li}$) threshold with 'large' widths 10—40 keV
 - Appears to rule out scenarios considered by *Cyburt & Pospelov (2009)* that low-lying, robust resonance in ^9B could explain the “Li problem”

End Lecture II

BSMs scenarios

- New particles: WIMPs, Axion, SUSY, ...
- GR modifications: new propagating DsOF; scalar-tensor
- Modifications of Cosmological SM: non-zero ν chem. pot.; non-equil. phenomena
- Variation of fundamental couplings
- Cosmic variance
- **Neutrino sector**
 - solar, atmospheric & reactor neutrinos oscillation experiment prove at least two neutrinos have mass
 - “sterile neutrinos”: mass \rightarrow neutrinos have left- & right-hand spin states
 - only left-hand neutrinos interact in SM
 - Massless neutrinos (recall)
 - have only one spin state

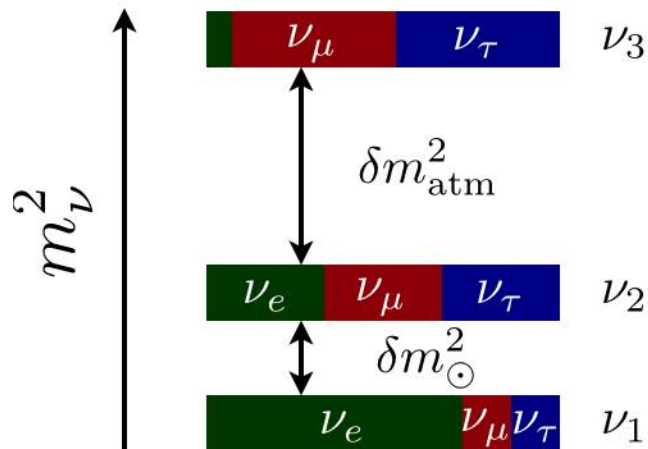
Neutrino Mass: what we know and don't know

We know the *mass-squared* differences: $\left\{ \begin{array}{l} \delta m_{\odot}^2 \approx 7.6 \times 10^{-5} \text{ eV}^2 \\ \delta m_{\text{atm}}^2 \approx 2.4 \times 10^{-3} \text{ eV}^2 \end{array} \right.$

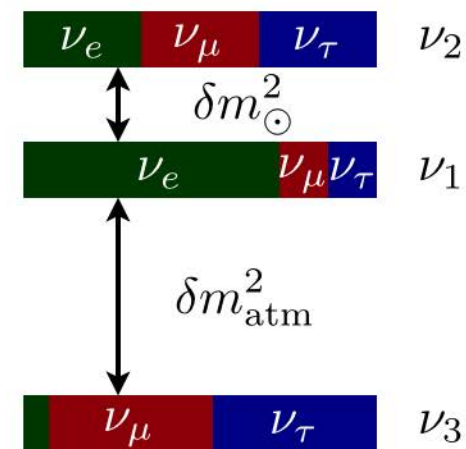
$$e.g., \delta m_{21}^2 \equiv m_2^2 - m_1^2$$

We *do not* know the *absolute masses* or the *mass hierarchy*:

normal mass hierarchy



inverted mass hierarchy



Neutrino mass mixing 101

□ Take-away message from experiments: “neutrinos have mass”

□ neutrino flavor eigenstates

$$|\nu_e\rangle, |\nu_\mu\rangle, |\nu_\tau\rangle$$

■ interact via left-hand (L) components

$$\bar{\psi}_e \gamma_\mu \frac{1}{2} (1 - \gamma_5) \psi_{\nu_e} = \bar{\psi}_{e,L} \gamma_\mu \psi_{e,L}$$

■ Mass term, however, mixes L & R:

$$\bar{\psi}_e \psi_e = \bar{\psi}_{e,R} \psi_{e,L} + \bar{\psi}_{e,L} \psi_{e,R}$$

$$\begin{pmatrix} |\nu_e\rangle \\ |\nu_\mu\rangle \\ |\nu_\tau\rangle \end{pmatrix} = U_m \begin{pmatrix} |\nu_1\rangle \\ |\nu_2\rangle \\ |\nu_3\rangle \end{pmatrix} \quad U_m = U_{23} U_{13} U_{12} M$$

$$U_{23} \equiv \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix}$$

$$U_{13} \equiv \begin{pmatrix} \cos \theta_{13} & 0 & e^{i\delta} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{-i\delta} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix}$$

$$\theta_{12}, \theta_{23}, \theta_{13}, \delta$$

$$U_{12} \equiv \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\theta_{12} \approx 0.59_{-0.015}^{+0.02}$$

$$\theta_{23} \approx 0.785_{-0.124}^{+0.124} \approx \frac{\pi}{4}$$

$$\theta_{13} \approx 0.154_{-0.065}^{+0.065}$$

$$\delta = CP \text{ violating phase} = ?$$

□ Mass mixing matrix

□ Pontecorvo-Maki-Nakagawa-Sakata

□ neutrino flavor oscillation: **confirmed!**

Sterile* neutrinos

□ What are they?

- Related to right-handed components

□ Wherefore?

- Mass \rightarrow right-handed neutrinos \rightarrow must exist by Lorentz invariance

- but may have mass modified by interactions

- Non-interacting(?!): only example of particles that interact solely via GR

- Interactions \rightarrow necessarily beyond SM physics

□ What (if anything) do they do?

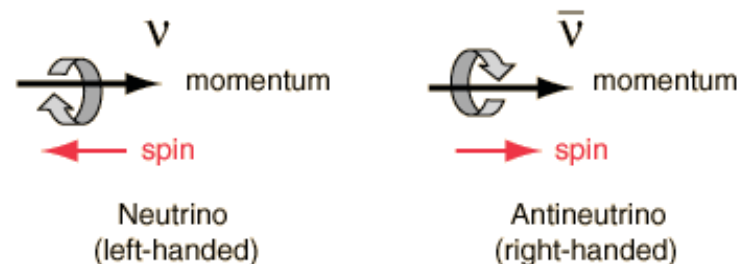
- perhaps they mix with active (e, μ, τ) neutrinos?

- then they're not really "sterile"

□ Why would we want (need?) them?

- leptogenesis; baryogenesis

- **BBN** & N_{eff}



$$|\nu_e\rangle = \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle$$

$$|\nu_s\rangle = -\sin\theta|\nu_1\rangle + \cos\theta|\nu_2\rangle$$



Hints for light sterile neutrinos?

□ mini-BooNE

- neutrino oscillation experiment $\nu_e \rightarrow \nu_s \rightarrow \nu_\mu$
- appearance with $\delta m^2 \sim 1 \text{ eV}^2$
- result inconsistent with flavor oscillation alone

□ ~~Neutrino reactor anomaly~~

- ~~3 σ deficit neutrinos detected in short-baseline (<100m) reactor ν experiments~~

~~$\bar{\nu}_e$ deficit from $\bar{\nu}_e \rightarrow \bar{\nu}_s$ (???) – a disappearance experiment~~

- A. Hayes et al. (2013) find “large corrections”

□ Extra radiation at photon-decoupling (Neff) ??

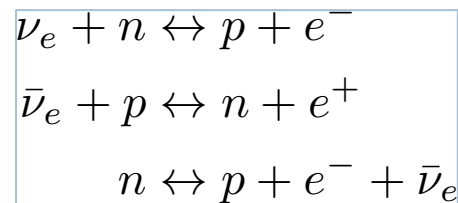
- CMB observations (PolarBear, ACT, SPT, Planck, CMBPol,...)
- ‘extra’ RED could reconcile H_0 and σ_8 inferred from CMB and astronomical observation

Dark radiation

- γ -decoupling (last scattering) $T \sim 0.2 \text{ eV}$ ($z \sim 1000$)
- N_{eff} : “effective number of neutrino degrees of freedom”
 - A misnomer; it refers to any/all relativistic particles at decoupling
 - ‘Baby’ formula: $\rho_{\text{rad}} = 2 \left[1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} N_{\text{eff}} \right] \frac{\pi^2}{30} T_{\gamma}^4$
 - We’ve done this better...
- CSM+SMPP \rightarrow predicts $N_{\text{eff}} = 3.046$ [Dicus et. al. '83; Dolgov, Hansen, Semikoz '97, '99; Gnedin² '98,...]
 - annihilation of neutrinos-antineutrinos at weak decoupling
 - QED corrections
- Measurements
 - WMAP9 (2012): 3.26(35); Planck (2013): 3.30(50); ACT(2013): 2.79(56); SPT-SZ (2012): 3.71(35)
- Sterile neutrinos can affect the physics of dark radiation

CMB as a probe of steriles: caveats

- Sterile neutrinos can decay *out-of-equilibrium*
 - “dilution”: steriles are “sub-weakly” interacting
 - non-thermal energy spectra/number densities
- Care must be applied when
 - computing N_{eff} : non-equilibrium effects; relativistic vs. non-relativistic kinematics
 - determining N_{eff} and Y_p (mass fraction ^4He)
 - current Planck collab. procedure is inconsistent w.r.t. N_{eff} and Y_p
 - in preparation: “**Neutrino physics in the era of precision cosmology**”
- neutron/proton ratio (and therefore ^4He)
 - competing weak reaction rates determine $Y_p(^4\text{He})$
 - **very sensitive to neutrino energy spectra**



Dilution physics (I)

- Consider the presence of ν_s
 - ▣ heavy (~ 100 MeV), unstable (~ 10 s)

- Thermal effects

- ▣ Assume interaction of steriles sufficiently strong at $T \sim \text{few GeV}$ to maintain thermal equilibrium with e, ν, γ, \dots

- ▣ Further, the sterile decouples at $T \sim \text{few MeV}$

$$s = \frac{\rho + p}{T} = g_*(a) \frac{2\pi^2}{45} T^3$$

- ▣ assume relativistic kinematics throughout
 - ▣ proper entropy is conserved: $s a^3 = \text{constant}$ (FLRW)
 - ▣ sterile neutrino temperature distribution cooled or “diluted”

$$\frac{T_{\nu_s}(a_{wdc})}{T_\gamma(a_{wdc})} = \left(\frac{g_*(a_{wdc})}{g_*(a_{\nu_s dc})} \right)^{1/3} = \left(\frac{10.75}{61.75} \right)^{1/3} \approx \frac{1}{1.8}$$

- ▣ number density comparable to photons (since lifetime chosen 10's secs)
 - ▣ $n(\nu_s) \sim 0.1 n(\gamma)$

- **NB:** ν_s is *out-of-equilibrium* with $e\mu\nu\gamma$

Dilution physics (II)

□ Heavy particle decay during/after weak decoupling

□ Interactions

Exothermic

$$\nu_s \rightarrow 3\nu_i$$

$$\nu_s \rightarrow \nu_i + \gamma$$

Endothermic

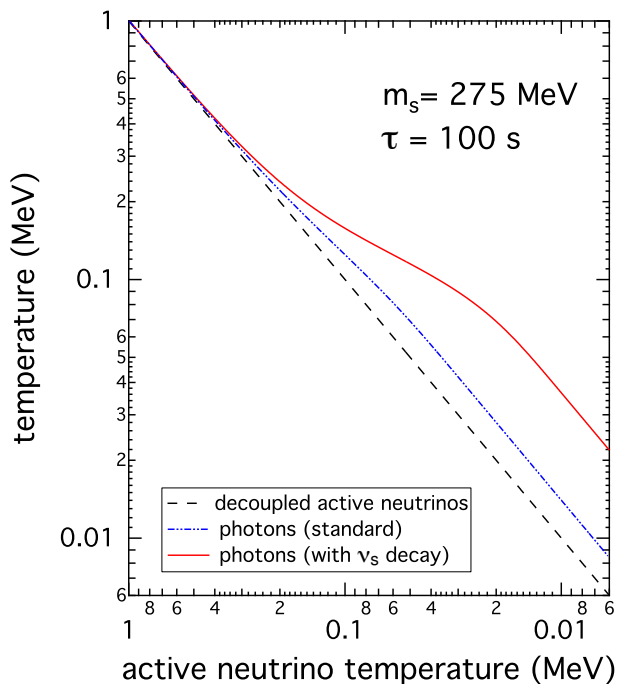
$$\nu_s \rightarrow \nu_i + e^- + e^+$$

$$\nu_s \rightarrow \nu + \mu^+ + \mu^-$$

$$\nu_s \rightarrow \nu + \pi^0$$

$$\nu_s \rightarrow \pi^\pm + e^\mp$$

$$\nu_s \rightarrow \pi^\pm + \mu^\mp$$



□ Entropy production

□ due to out-of-equilibrium decay

□ plasma cools slower than decoupled actives

□ Dilution

□ decoupled actives diluted down

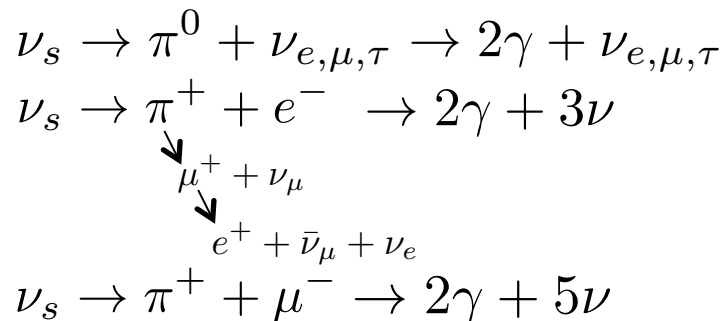
□ Two effects

■ coupling to plasma \rightarrow reduction in N_{eff}

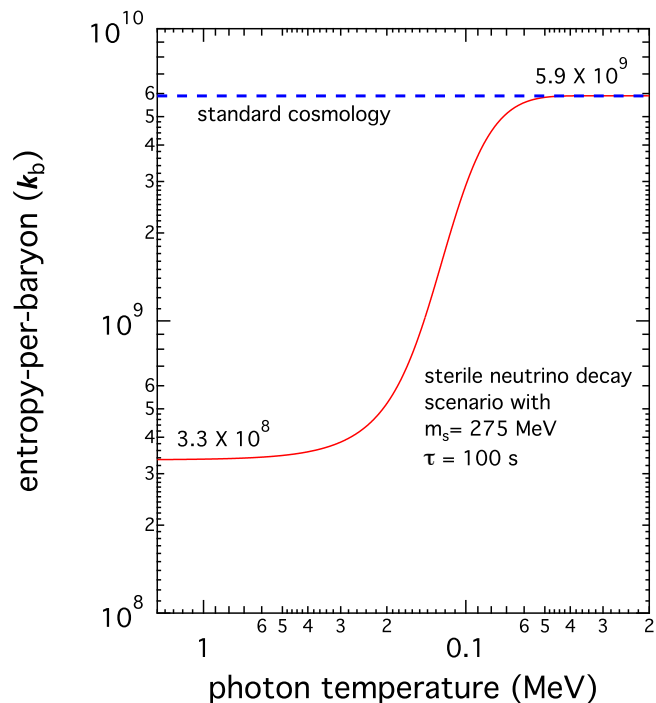
■ coupling to actives \rightarrow increase N_{eff}

Dilution physics (III)

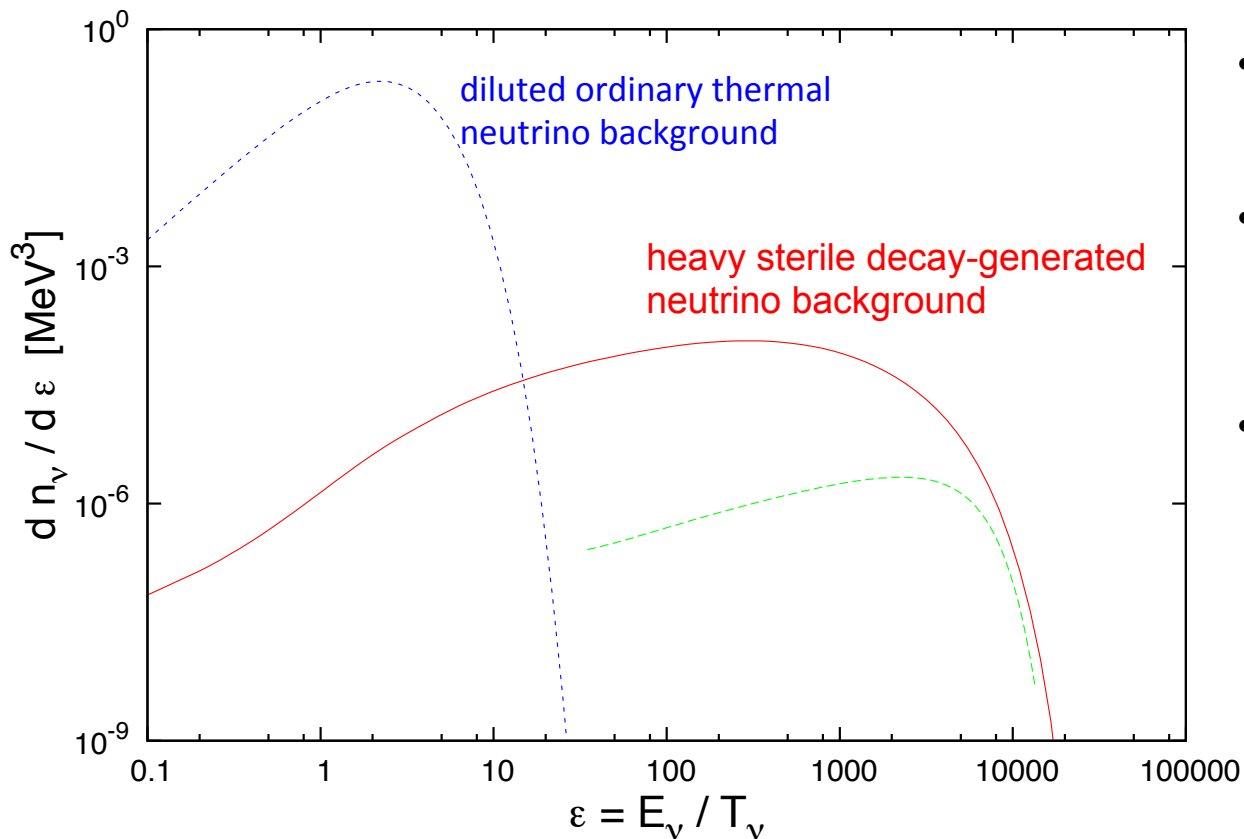
- Photons thermalize
 - ▣ sterile neutrino decay ($m_s < \text{few GeV}$)
- But active neutrinos may not
 - ▣ energy/decay-epoch dependent



- Heavy sterile neutrino decay
 - ▣ dilution of background ($C\nu B$)
 - ▣ generation of radiation energy density: N_{eff}
 - ▣ prodigious entropy production



Non-equilibrium distribution of $C\nu B$



- Heavy sterile dilutes the normal background neutrino spectrum
- decay-generated spectrum $\sim 10^3$ times more energetic than standard; never non-relativistic
- can't detect neutrino rest mass cosmologically

The Big Question: what effect on BBN? Y_p

Code capabilities & design

□ Capabilities

- Boltzmann equation solver: two classes of Boltzmann equations
 - Nucleosynthesis: Unitary Reaction Network for BBN (previous slides)
 - Neutrino energy transport: new capability – never before achieved

$$\frac{Df_1}{Dt} = \int \frac{s}{2E_1} \frac{d^3p_2}{(2\pi)^3(2E_2)} \frac{d^3p_3}{(2\pi)^3(2E_3)} \frac{d^3p_4}{(2\pi)^3(2E_4)} \\ \times \langle |\mathcal{M}|^2 \rangle (2\pi)^4 \delta^4(P_1 + P_2 - P_3 - P_4) F(p_1, p_2, p_3, p_4)$$
$$\frac{Df_1}{Dt} = \frac{\kappa}{32(2\pi)^3} \int_0^\infty p_1 p_2^3 dp_2 \int_{-1}^1 dx \frac{(1-x)^2}{\sqrt{p_1^2 + p_2^2 + 2p_1 p_2 x}} \int_{E_{\min}}^{E_{\max}} dp_3 F(p_1, p_2, p_3, p_1 + p_2 - p_3).$$

- Various reactions result in seven evaluations of this **triple** integral
- Achieved short turn-around time by parallelization

□ Design

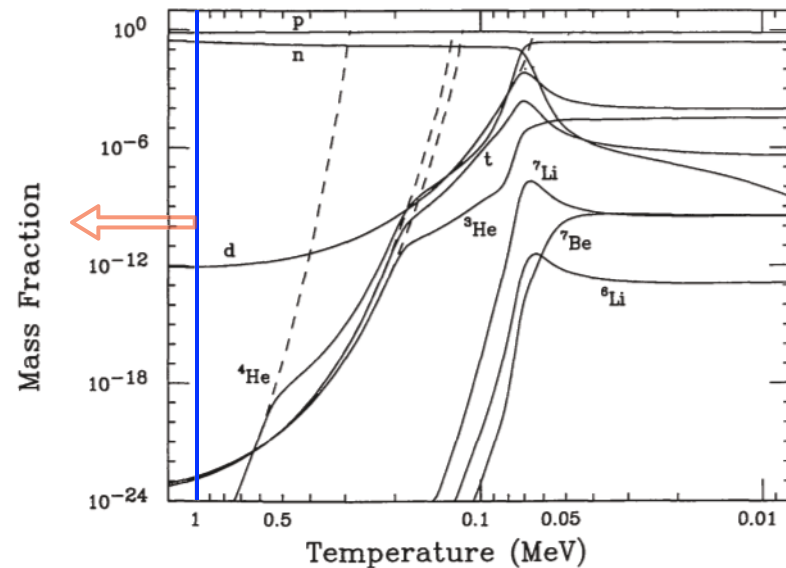
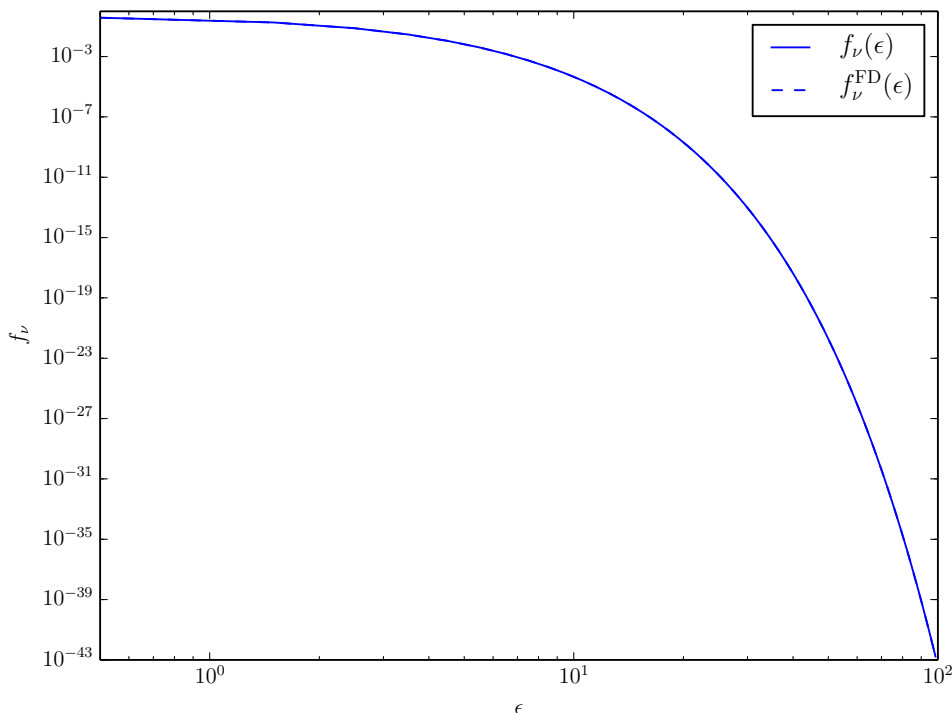
- Modular code design for adaptability for **public code release**
- Allow insertion of “physics packages” to test BSM (not just sterile ν ’s)

Code testing/preliminary results

- Evolve assuming equilibrium from 30 MeV \rightarrow 3 MeV
- Then turn-on only elastic ν -lepton scattering

$$\nu_i + e^\pm \rightarrow \nu_i + e^\pm \quad i = e, \mu, \tau$$

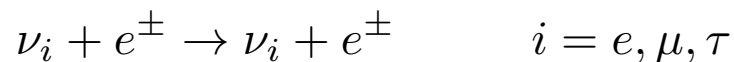
$$T_\nu = 2.892\text{E}+01 \text{ MeV}$$



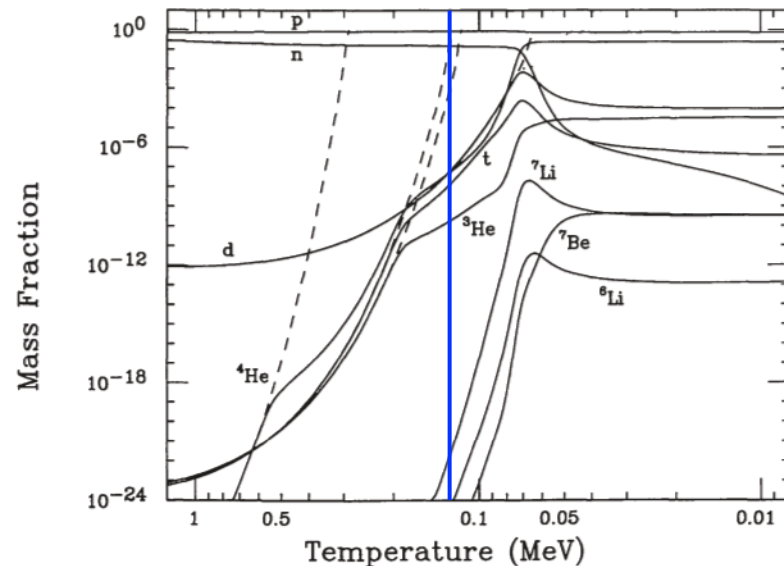
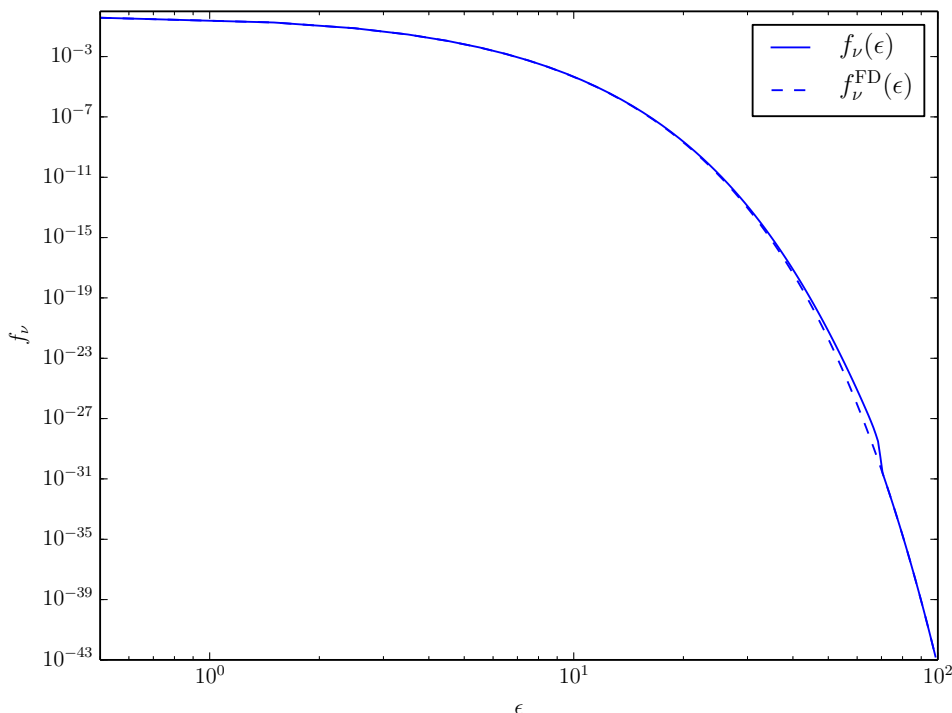
- since the ν & anti- ν are cooler than the e^\pm anticipate upscattering

Code testing/preliminary results

- Evolve assuming equilibrium from 30 MeV \rightarrow 3 MeV
- Then turn-on only elastic ν -lepton scattering



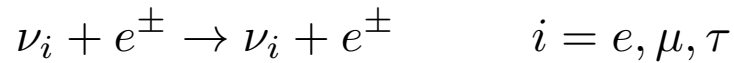
$$T_\nu = 1.134\text{E-}01 \text{ MeV}$$



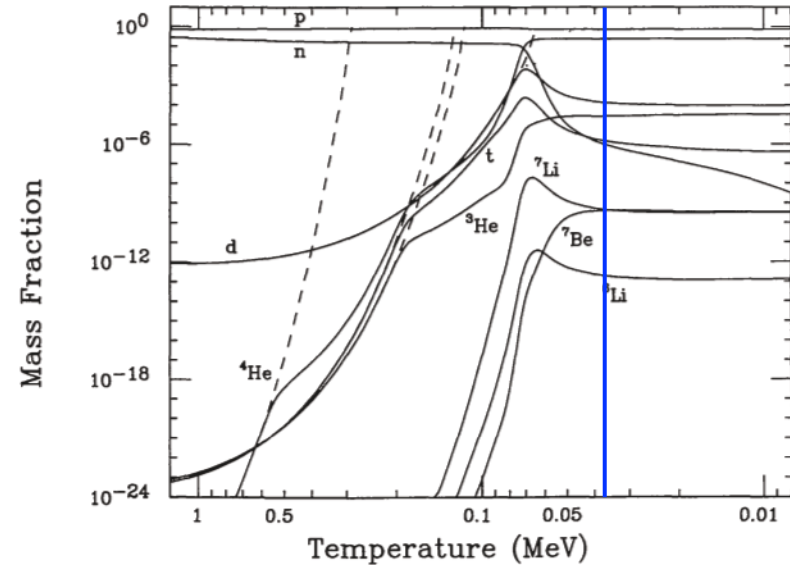
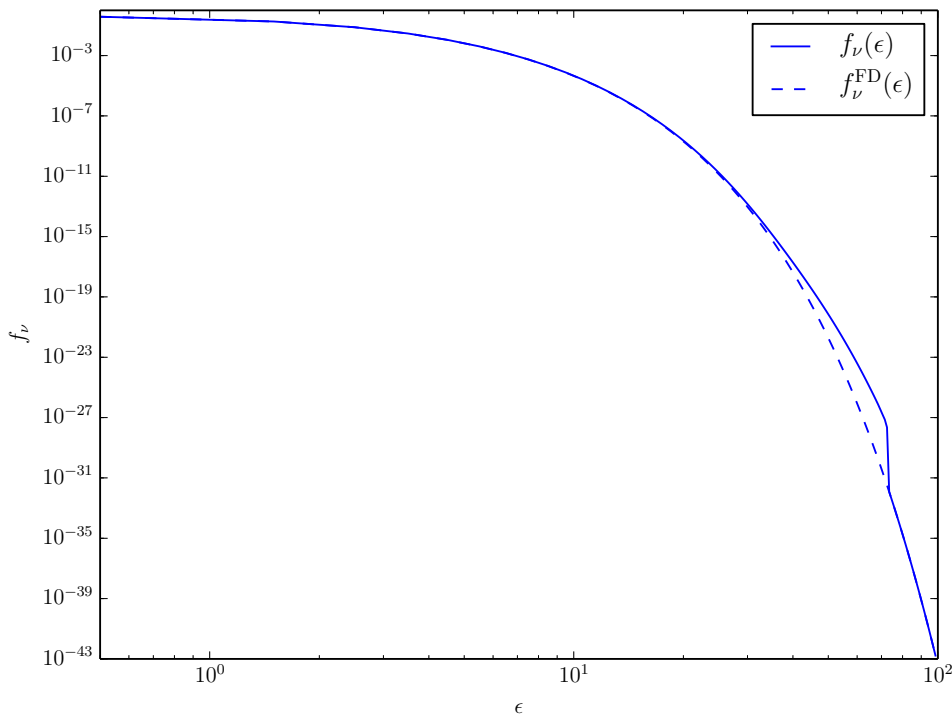
- since the ν & anti- ν are cooler than the e^\pm anticipate upscattering

Code testing/preliminary results

- Evolve assuming equilibrium from 30 MeV \rightarrow 3 MeV
- Then turn-on only elastic ν -lepton scattering



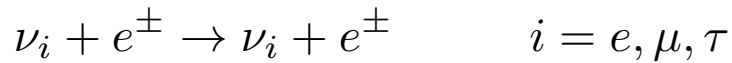
$$T_\nu = 3.875\text{E-}02 \text{ MeV}$$



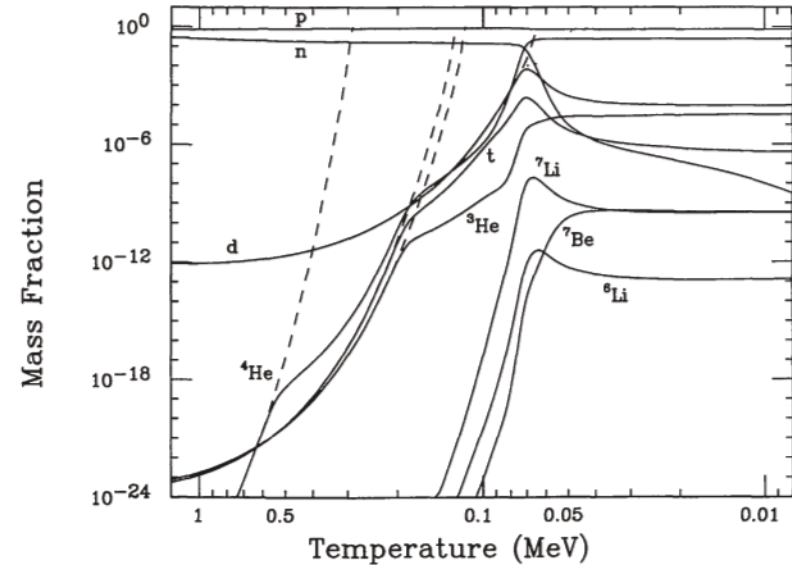
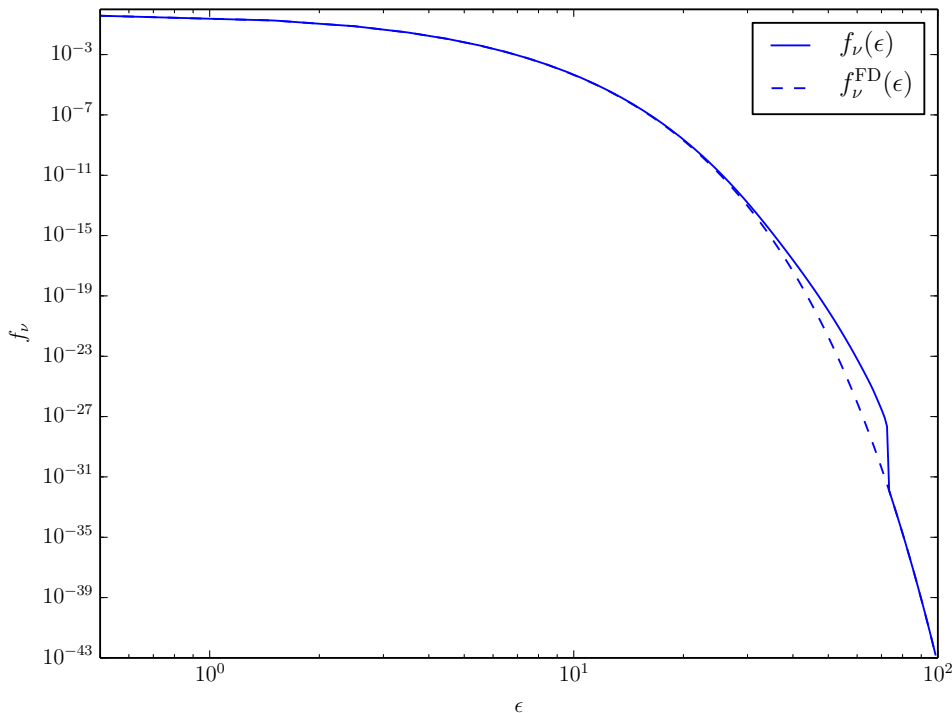
- since the ν & anti- ν are cooler than the e^\pm anticipate upscattering

Code testing/preliminary results

- Evolve assuming equilibrium from 30 MeV \rightarrow 3 MeV
- Then turn-on only elastic ν -lepton scattering



$$T_\nu = 1.886\text{E-}03 \text{ MeV}$$



- since the ν & anti- ν are cooler than the e^\pm anticipate upscattering
- **INTERESTING:** because “ ν decoupl. complete by e^+e^- annihilation”

Elastic scattering

Initial transport temperature [keV]	N_{eff}
20	3.0055
40	3.0055
100	3.005666
200	3.005936
400	3.006555
1000	3.008414
3000	3.013428

 e^{\pm} annihilation

Initial transport temperature [keV]	N_{eff}
20	3.005584
40	3.005590
100	3.005682
200	3.005985
400	3.006604
1000	3.008309
3000	3.xxxxxxx

These preliminary/test results give a nice demonstration that the fundamentals of the neutrino energy transport are working.