

Stellar Feedback and Galaxy Formation: Issues and Non-issues

James Wadsley (McMaster)

Ben Keller (McMaster), Tom Quinn (Washington)

$$t/t_{\text{KH}} = 0.00$$

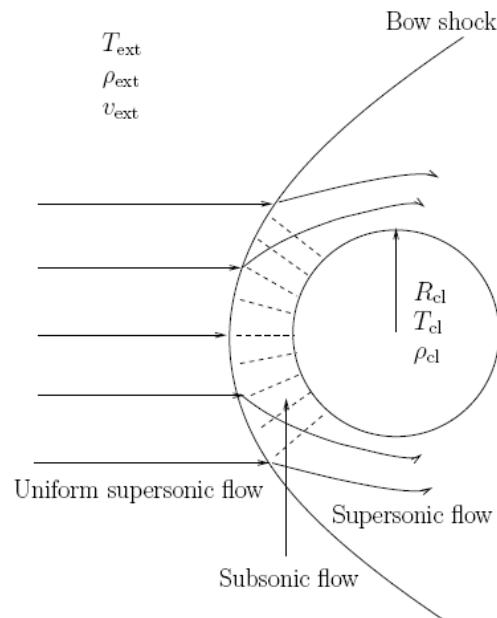
Gasoline /
ChaNGa SPH (James Wadsley/Tom Quinn)



Agertz et al 2007
Code comparison
paper from the
proto AstroSim
conference
(2004)



Test



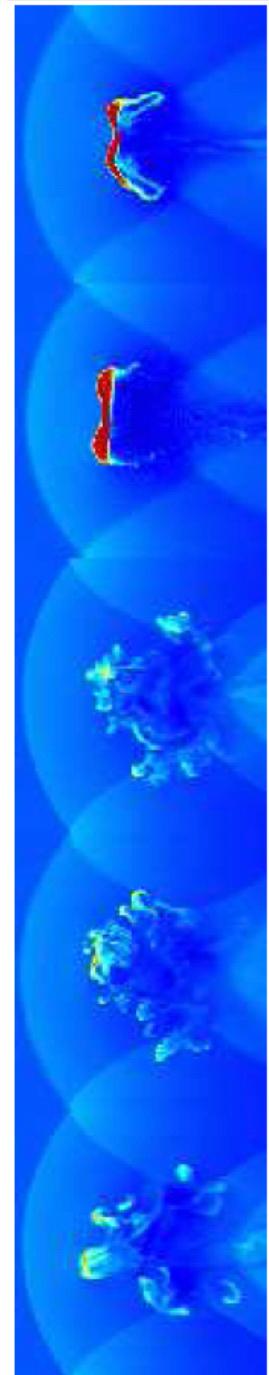
Gasoline
(Wadsley,
Stadel &
Quinn 2004)

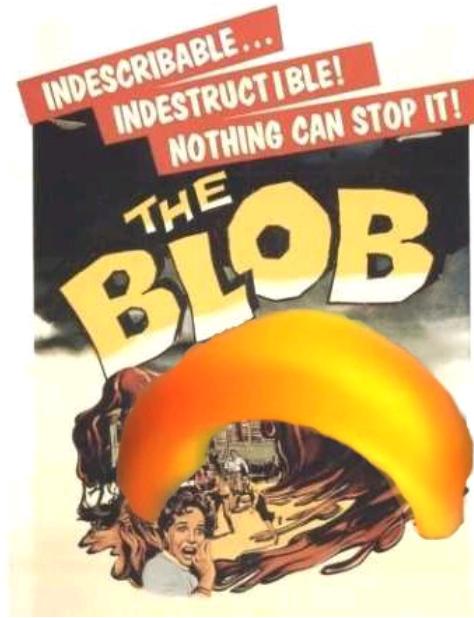
Gadget
(Springel)

FLASH

ENZO

ART



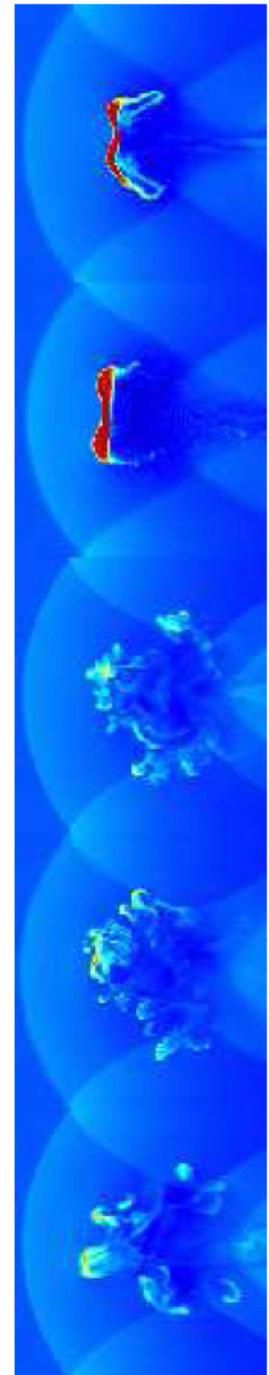
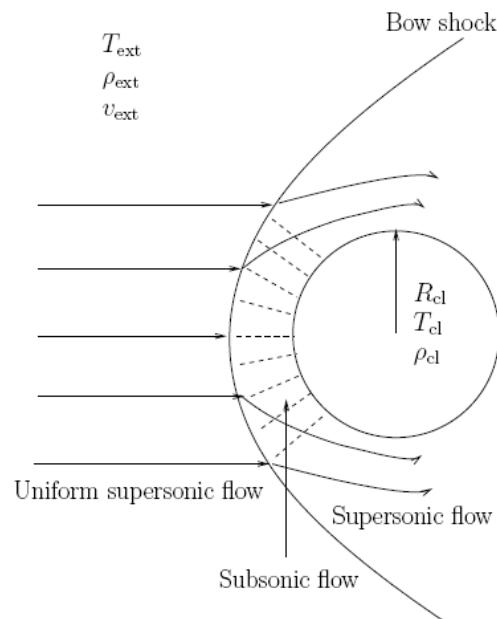


Test

Agertz et al 2007
Code comparison
paper from the
proto AstroSim
conference
(2004)

SPH
Smoothed
Particle
Hydrodynamics
(Monaghan 1992,
Springel & Hernquist 2002)

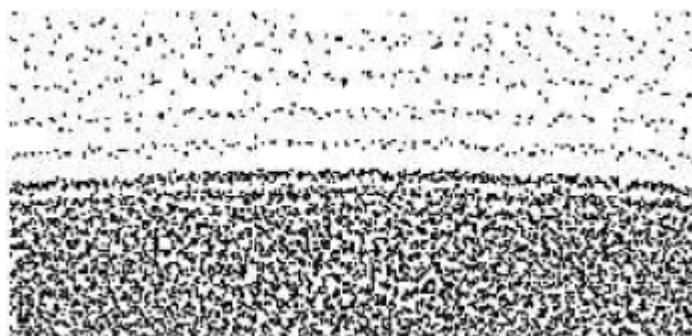
PPM
Piecewise
Parabolic
Method
(Collela &
Woodward
1987)



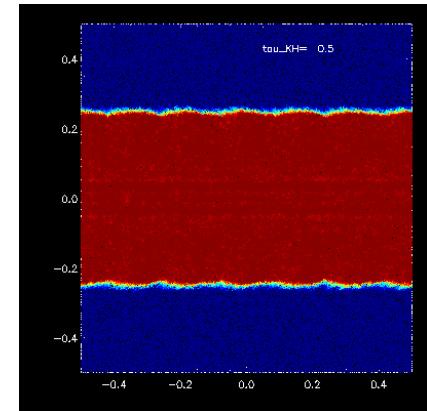
Agertz et al (2007) Basic Result: SPH blobs don't break up

Immediate SPH issue: Surface Tension present in arithmetic sum Pressure force (e.g. Monaghan 1992, Gadget 2, ...)

Suppresses Kelvin Helmholtz instabilities

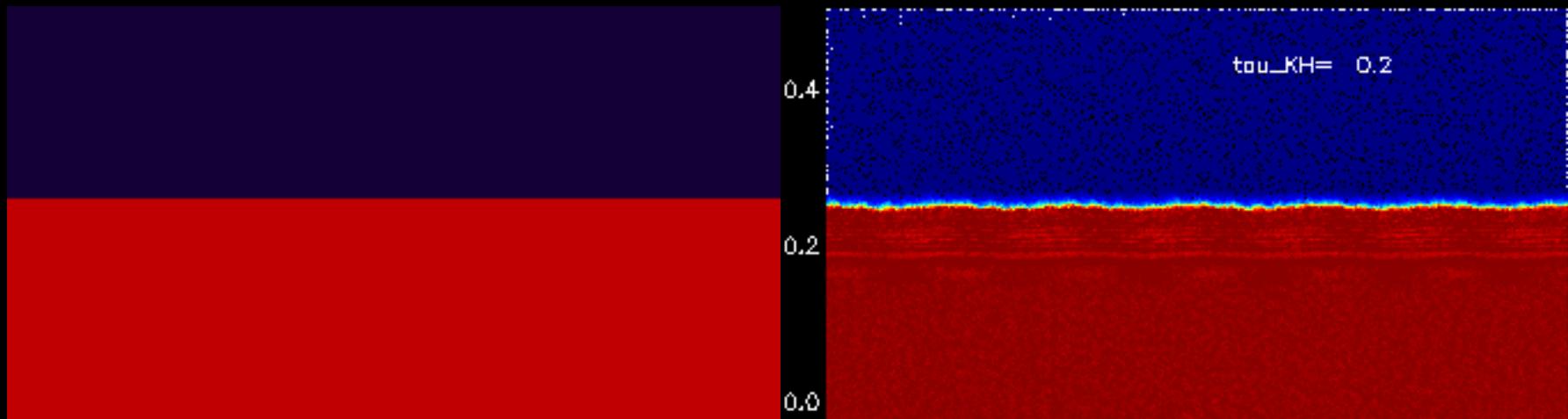


SPH Kelvin Helmholtz fixes



- Ritchie & Thomas (2001) – smooth pressure not density and Geometric Density Average in Force: remove surface tension (pressure errors at density jump)
- Price (2008) – smear density jumps
- Read, Hayfield & Agertz (2010), Read & Hayfield (2011), Abel (2011), Murante et al (2011) ... modified SPH
- Pressure-Entropy SPH (Hopkins 2013)

1:10 Kelvin Helmholtz test

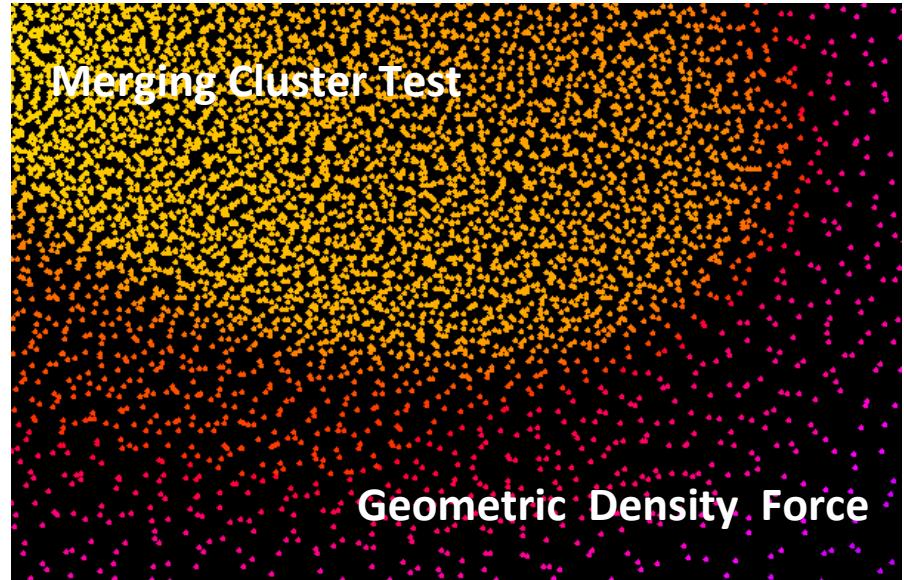
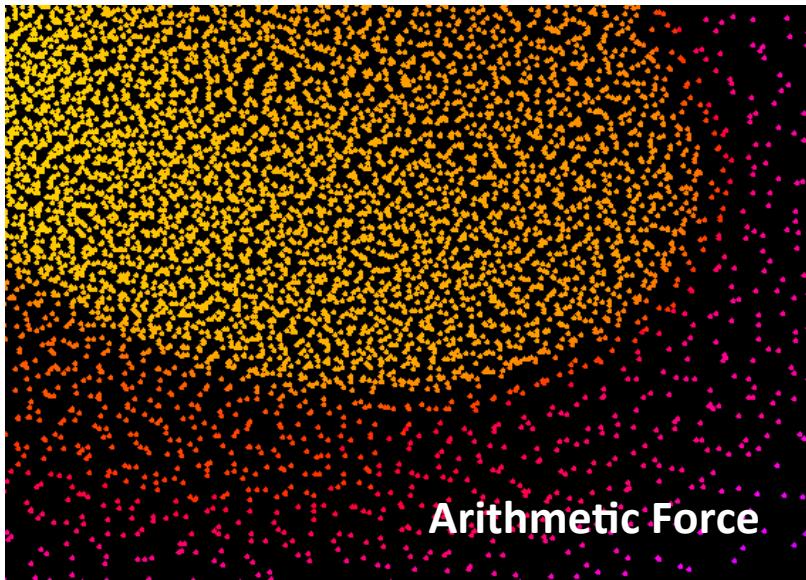


Common element in relieving SPH surface tension:

- Geometric Density Average in Force (GD Force):

$$\frac{dv_a}{dt} = - \sum_b m_b \left(\frac{P_a + P_b}{\rho_a \rho_b} \right) \nabla_a W_{ab}$$

Morris (1996), Monaghan (1992)
Ritchie and Thomas (2001),
Can be derived from a Lagrangian:
Monaghan & Rafiee (2012)
see also Abel (2011), Hopkins (2013)



Is removing surface tension enough?

Blob Test in Entropy ($T^{3/2}/\rho$)



Hi-Res
ENZO



Hi-Res
Old
SPH

Is removing surface tension enough? No

Blob Test in Entropy ($T^{3/2}/\rho$)

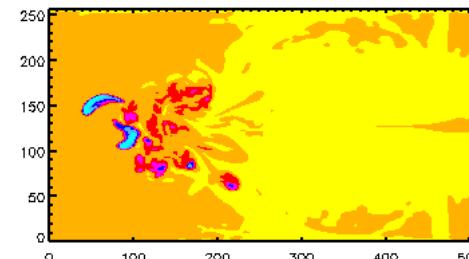
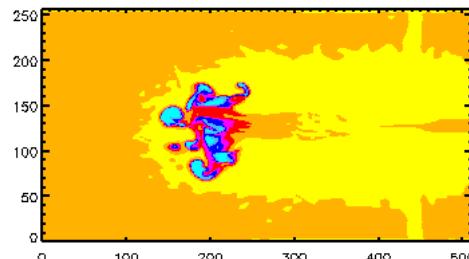
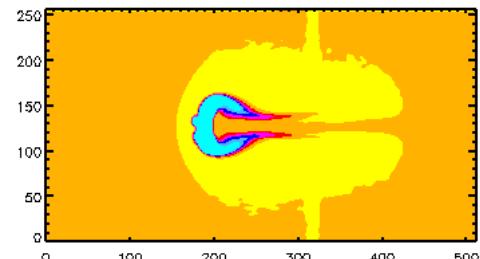


Hi-Res
ENZO

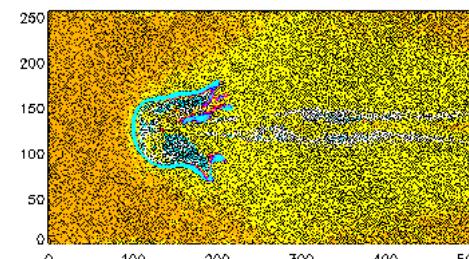
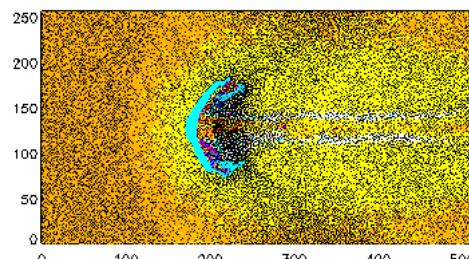
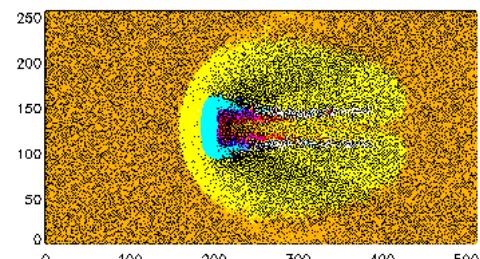


Hi-Res
GD Force
SPH

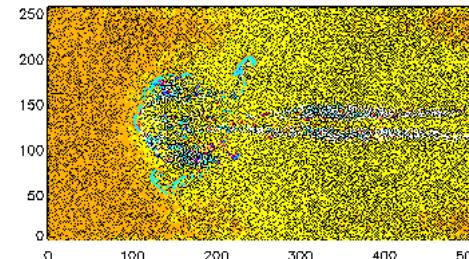
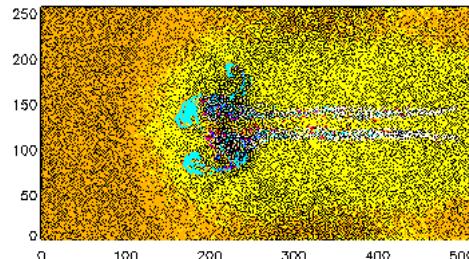
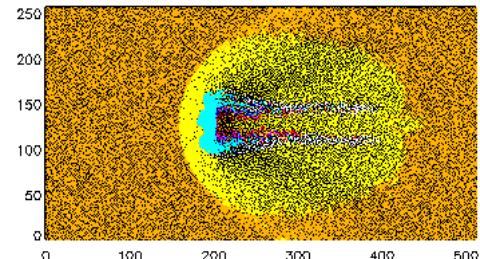
Blob Test in Entropy ($T^{3/2}/\rho$)



ENZO



**Old
SPH**



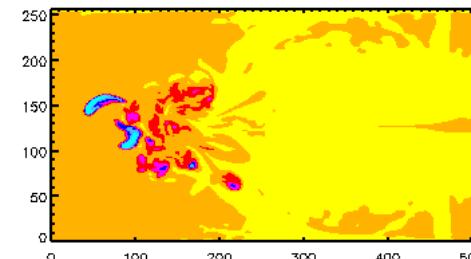
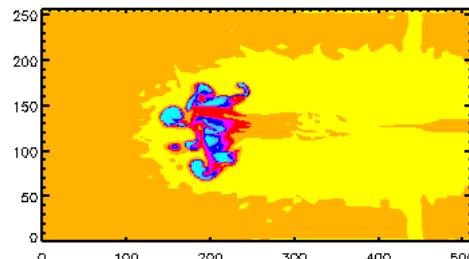
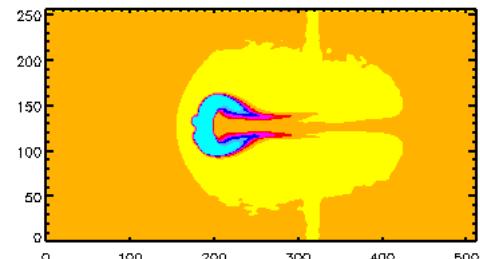
$t = 1.25 \tau_{\text{KH}}$

$t = 2.5 \tau_{\text{KH}}$

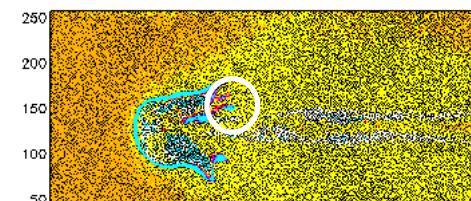
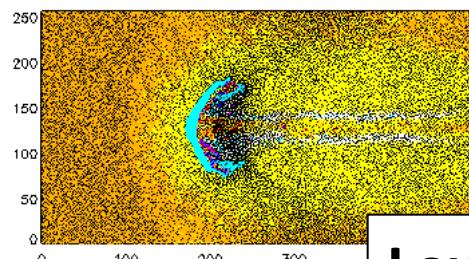
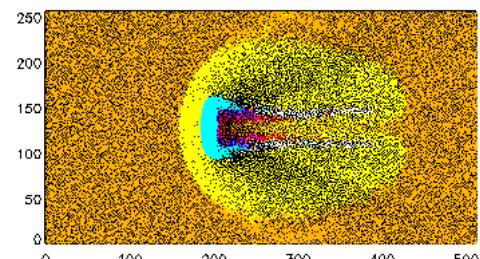
$t = 3.75 \tau_{\text{KH}}$

**GD Force
SPH**

Blob Test in Entropy ($T^{3/2}/\rho$)

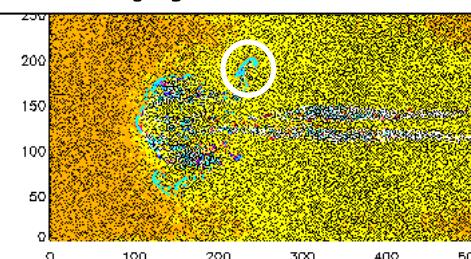
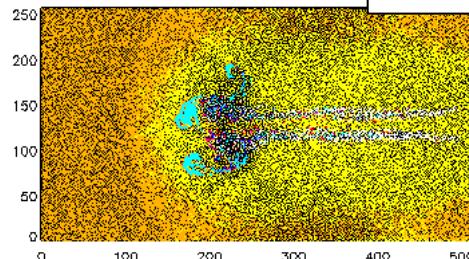
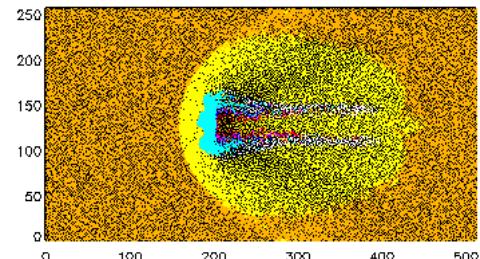


ENZO



**Old
SPH**

Low Entropy Blobs Indestructible!



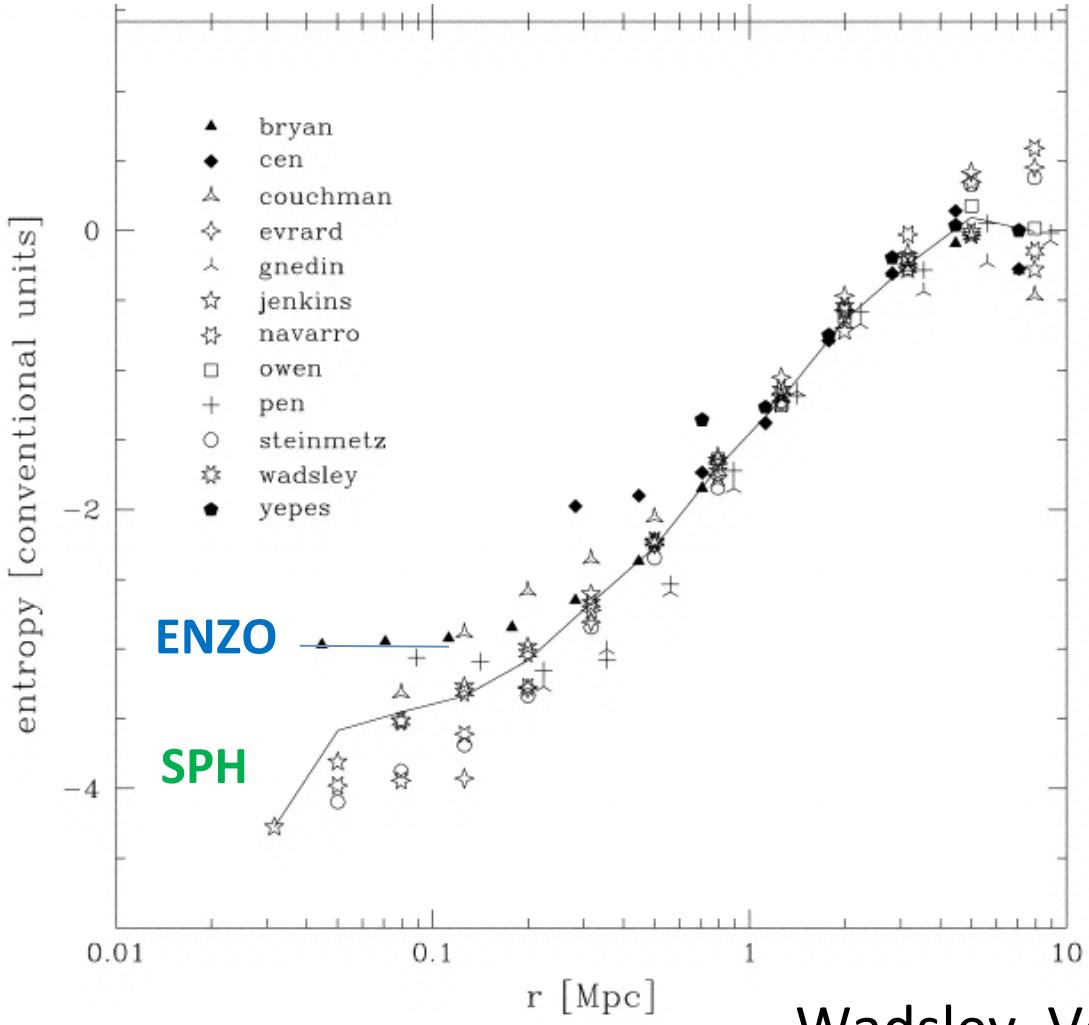
**GDForce
SPH**

$t = 1.25 \tau_{KH}$

$t = 2.5 \tau_{KH}$

$t = 3.75 \tau_{KH}$

The second issue: Mixing



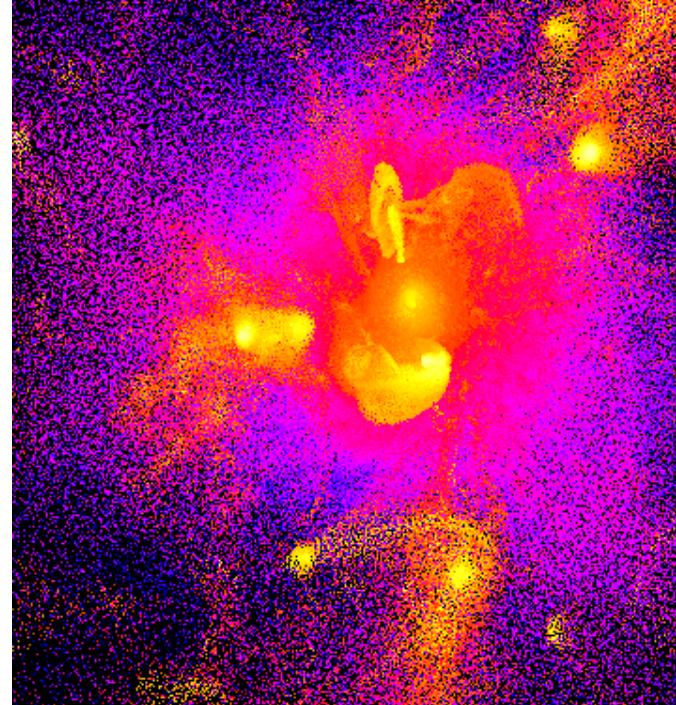
Cluster Comparison
(Frenk et al 1999)

Grid codes have
entropy cores,
SPH codes didn't
(because they
didn't mix)

How to get entropy cores?

- Shocks (while $c_s < v$)
- Mix hot & cold cluster gas

SPH can't:



$$\frac{du}{dt} = -(\gamma - 1) u(\nabla \cdot \mathbf{v}) \Rightarrow A(s) = \frac{P}{\rho^\gamma} = \begin{matrix} \text{const.} \\ \text{following flow} \end{matrix}$$

Eulerian codes can (accidentally):

$$\frac{\partial u}{\partial t} + \mathbf{v} \cdot \nabla u + \begin{matrix} \text{advection} \\ \text{errors} \end{matrix} = -(\gamma - 1) u(\nabla \cdot \mathbf{v})$$

Subgrid Turbulent Mixing

- Fluid elements on a fixed (resolved) physical scale do exchange energy/entropy due to unresolved (turbulent) motions

Turbulent diffusive heat flux

$$\frac{\partial u}{\partial t} + \mathbf{v} \cdot \nabla u = -(\gamma - 1) u (\nabla \cdot \mathbf{v}) \text{ goes to}$$

$$\frac{\partial \bar{u}}{\partial t} + \bar{\mathbf{v}} \cdot \nabla \bar{u} + \boxed{\bar{\delta v} \cdot \nabla \delta u} = -(\gamma - 1) \left(\bar{u} (\nabla \cdot \bar{\mathbf{v}}) + \boxed{\delta u (\nabla \cdot \delta \mathbf{v})} \right)$$

where \bar{a} = resolved (filtered) part of field a ,

$$\delta a = \text{unresolved part}, \quad \overline{\delta a} = 0$$

Turbulent diffusion

- Lowest-order turbulent diffusion model:

$$\frac{\partial \bar{u}}{\partial t} + \bar{v} \cdot \nabla \bar{u} = -(\gamma - 1) \bar{u} (\nabla \cdot \bar{v}) + \nabla \kappa_{\text{Turb}} \nabla \bar{u}$$

κ_{Turb} has units of velocity x length

Smagorinsky model (1963): $\kappa_{\text{Turb}} = l_s^2 S$, $S = \sqrt{S_{ij} S_{ij}}$

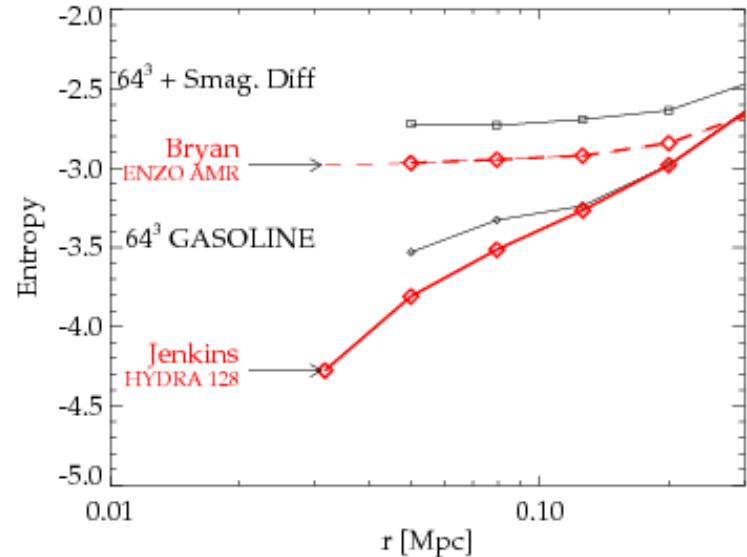
S_{ij} = strain tensor of resolved flow, l_s Smagorinsky length

Incompressible grid models set $l_s^2 \sim 0.02 \Delta x^2$ (Lilly 1967)

For SPH we can use $\kappa_{\text{Turb}} = C h^2 S$ $C \sim 0.01-0.1$

Turbulent diffusion

- Cluster Entropy Cores occur in SPH when thermal diffusion included
- Need: Galilean invariance, correct Prandtl numbers – see new paper: Power, Reid and Hobbs (2013)
- Not all diffusions are equal! Grid advection errors do not give correct solution!



Wadsley, Veeravalli & Couchman (2008)
Shen, Wadsley & Stinson (2010)

Blob Test in Entropy ($T^{3/2}/\rho$)

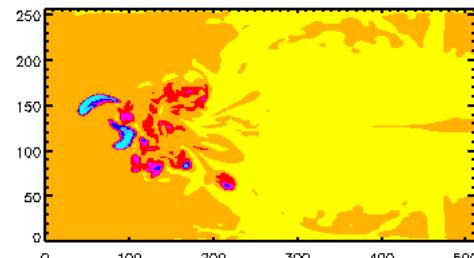
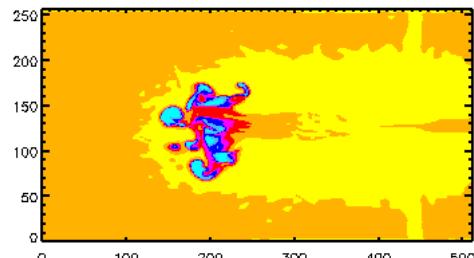
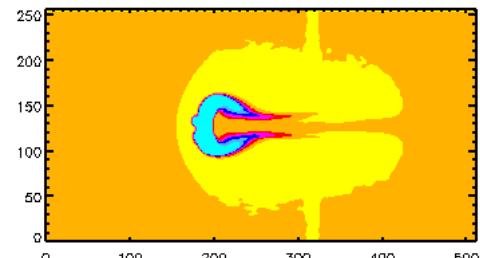


Hi-Res
ENZO

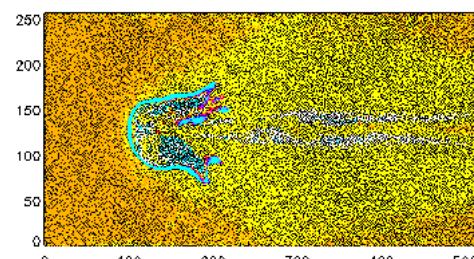
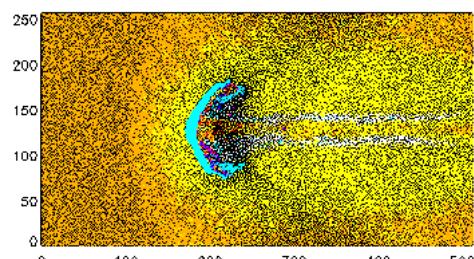
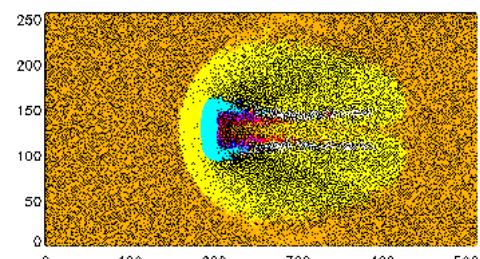


GD Force +
Turbulent
Diffusion SPH

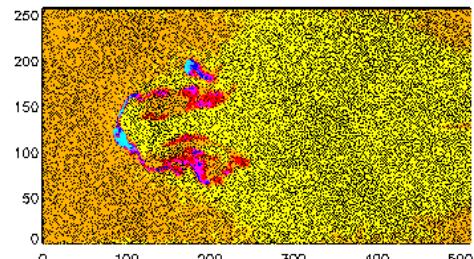
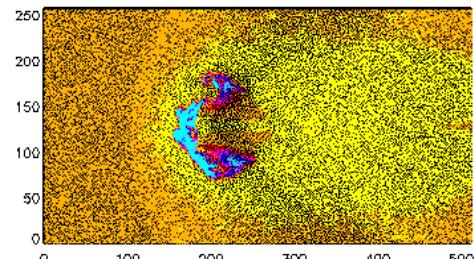
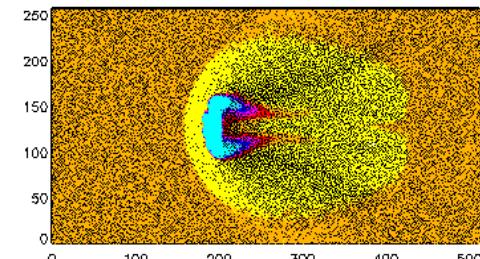
Blob Test in Entropy ($T^{3/2}/\rho$)



ENZO



**Old
SPH**



$t = 1.25 \tau_{KH}$

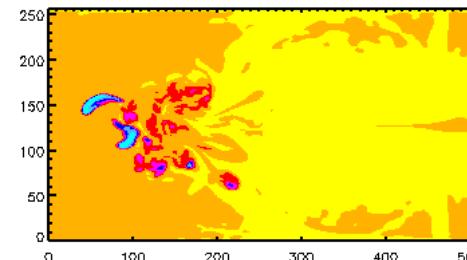
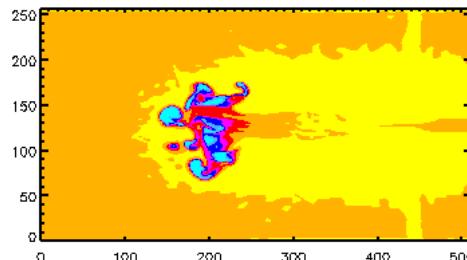
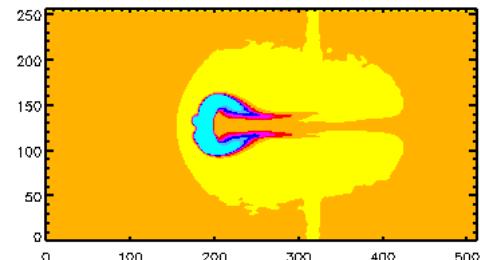
$t = 2.5 \tau_{KH}$

$t = 3.75 \tau_{KH}$

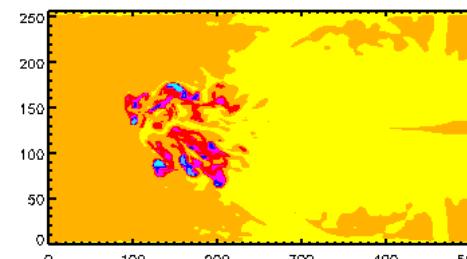
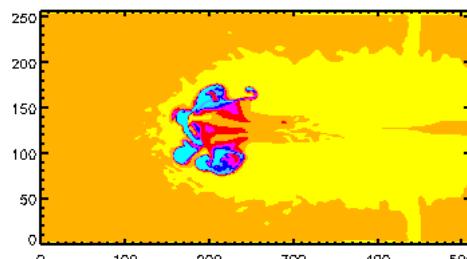
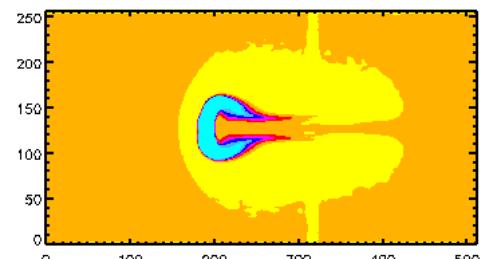
**GD Force
Turbulent
Diffusion
SPH**

Is grid (PPM) the right answer?

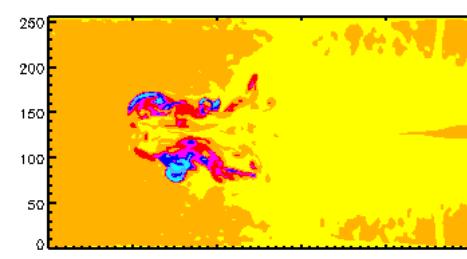
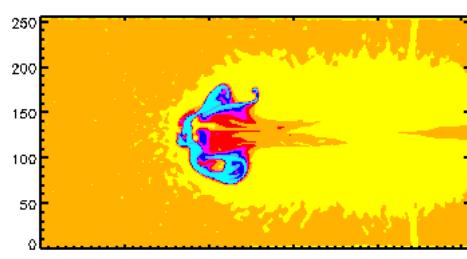
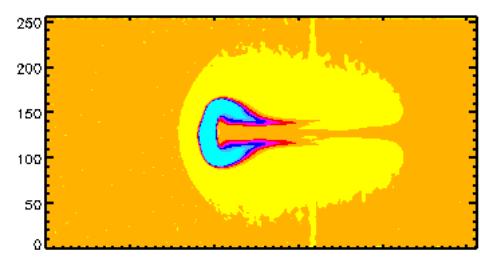
No: Numerical Diffusion Approximate,
e.g. is not Galilean Invariant



**ENZO
Moving
flow**



**ENZO
1/2 – 1/2**



**ENZO
Moving
blob**

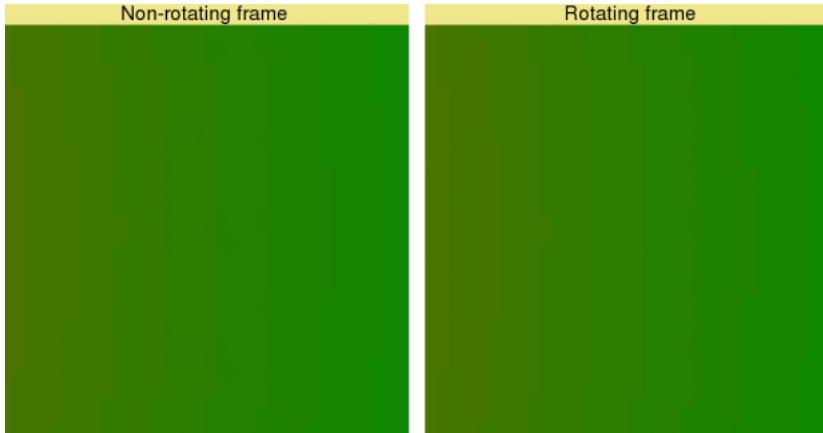
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$t = 2.5 \tau_{\text{KH}}$

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Aside:

Reducing numerical diffusion in grid codes



Galaxy disk
200 km/s rotation
Gives large advection errors
unless you work in a rotating
frame

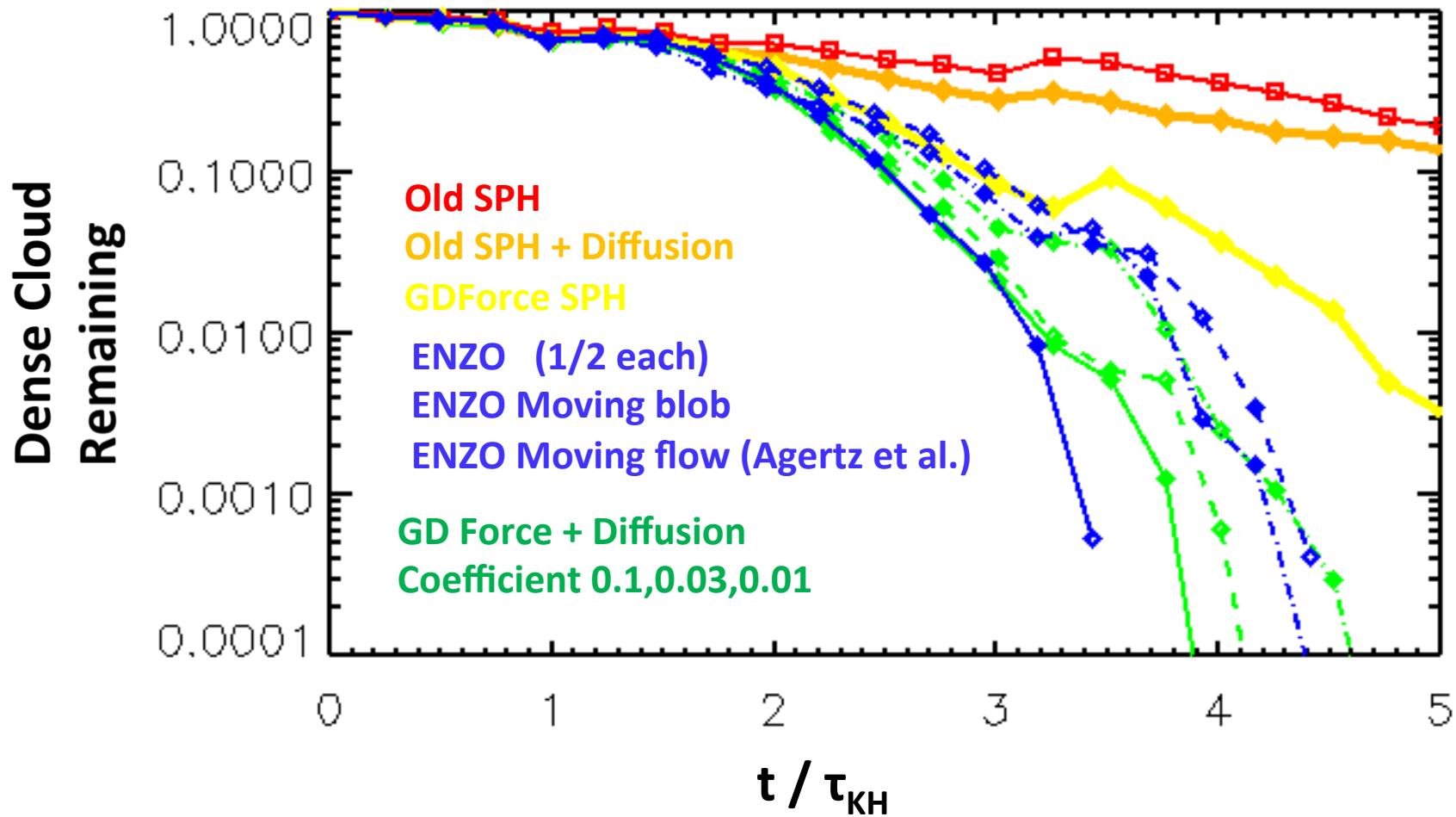
500 pc subregion in model MW galaxy ENZO simulation, both 30 pc resolution

- Pick a rotation rate: radii near co-rotation see large benefit
- Need to add coriolis force
- Effective resolution 4x better
- Faster: Courant timesteps much shorter $dt \sim dx/10$ km/s vs. $dx/200$ km/s

Lagrangian methods (e.g. SPH, AREPO) automatically get this benefit

Benincasa, Tasker, Wadsley & Pudritz (2013)

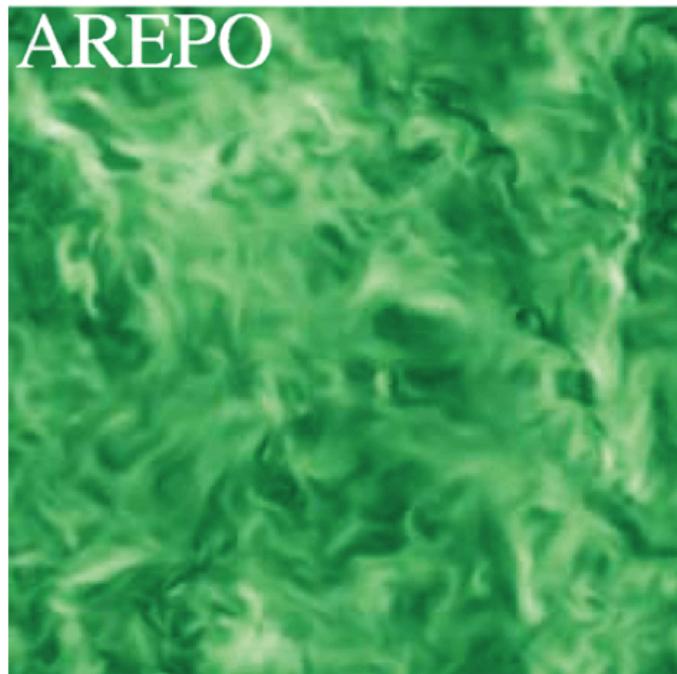
Blob's falling apart... (Log)



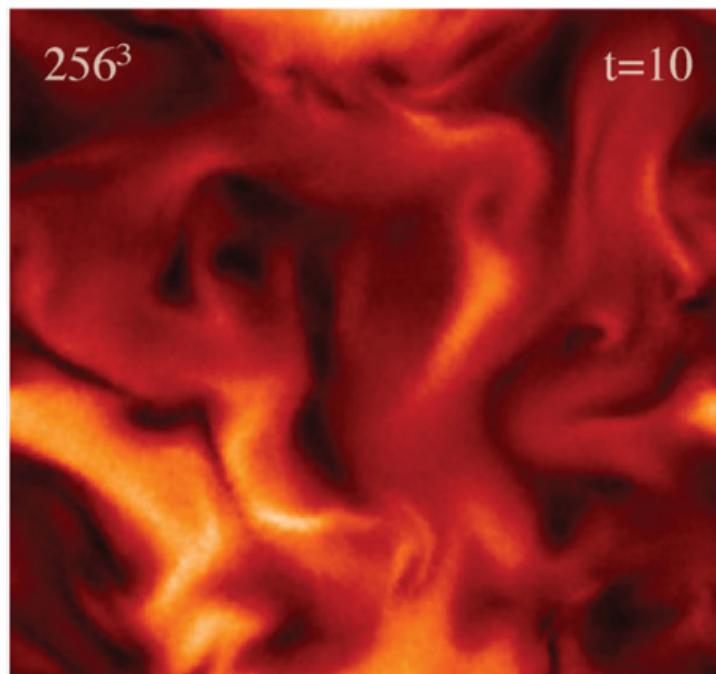
Outstanding issue?

Subsonic turbulence (cf. Bauer & Springel 2012)

- Test Problem: Driven Mach 0.3 turbulence

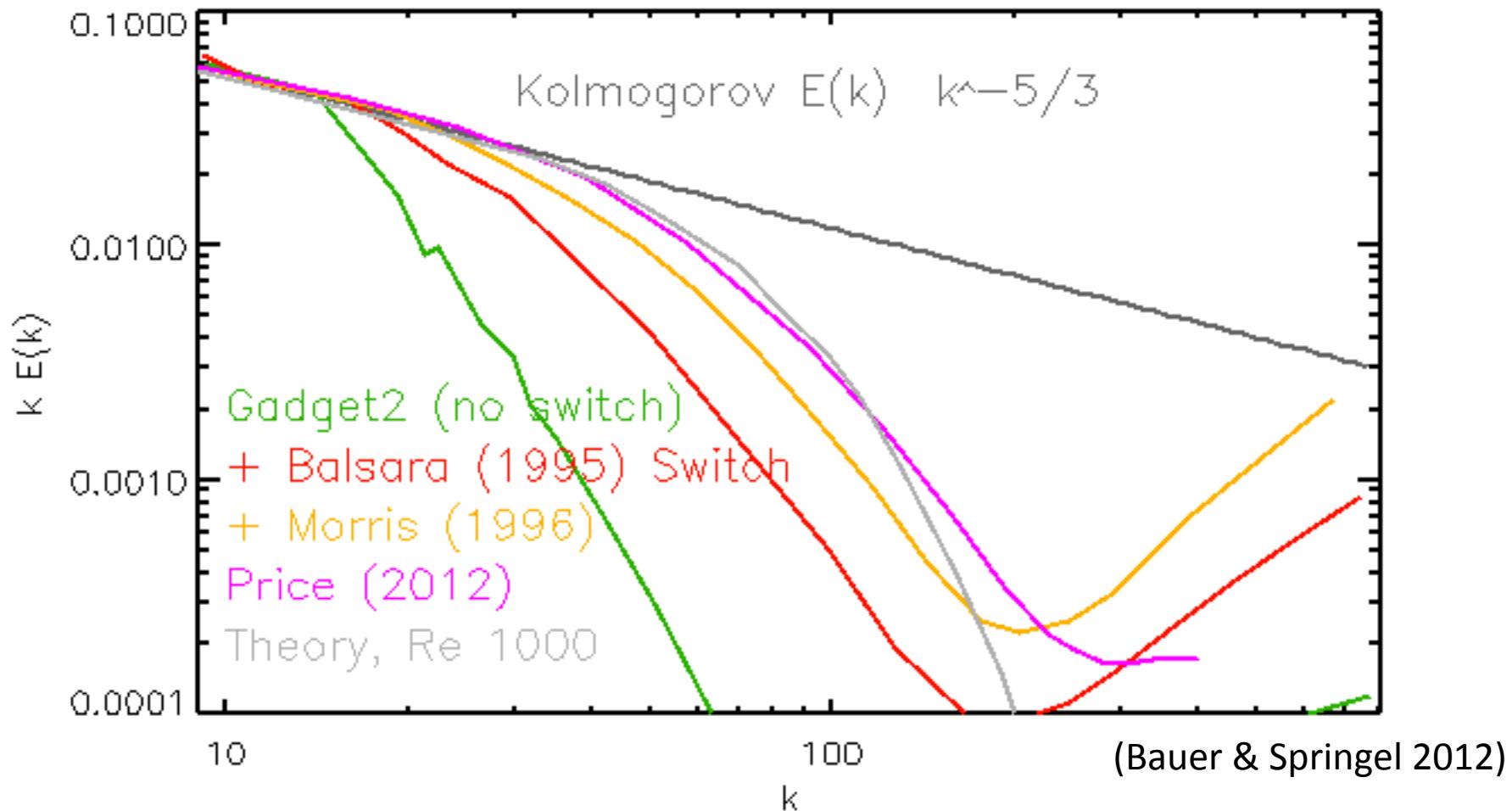


AREPO velocity field
(Bauer & Springel 2012)



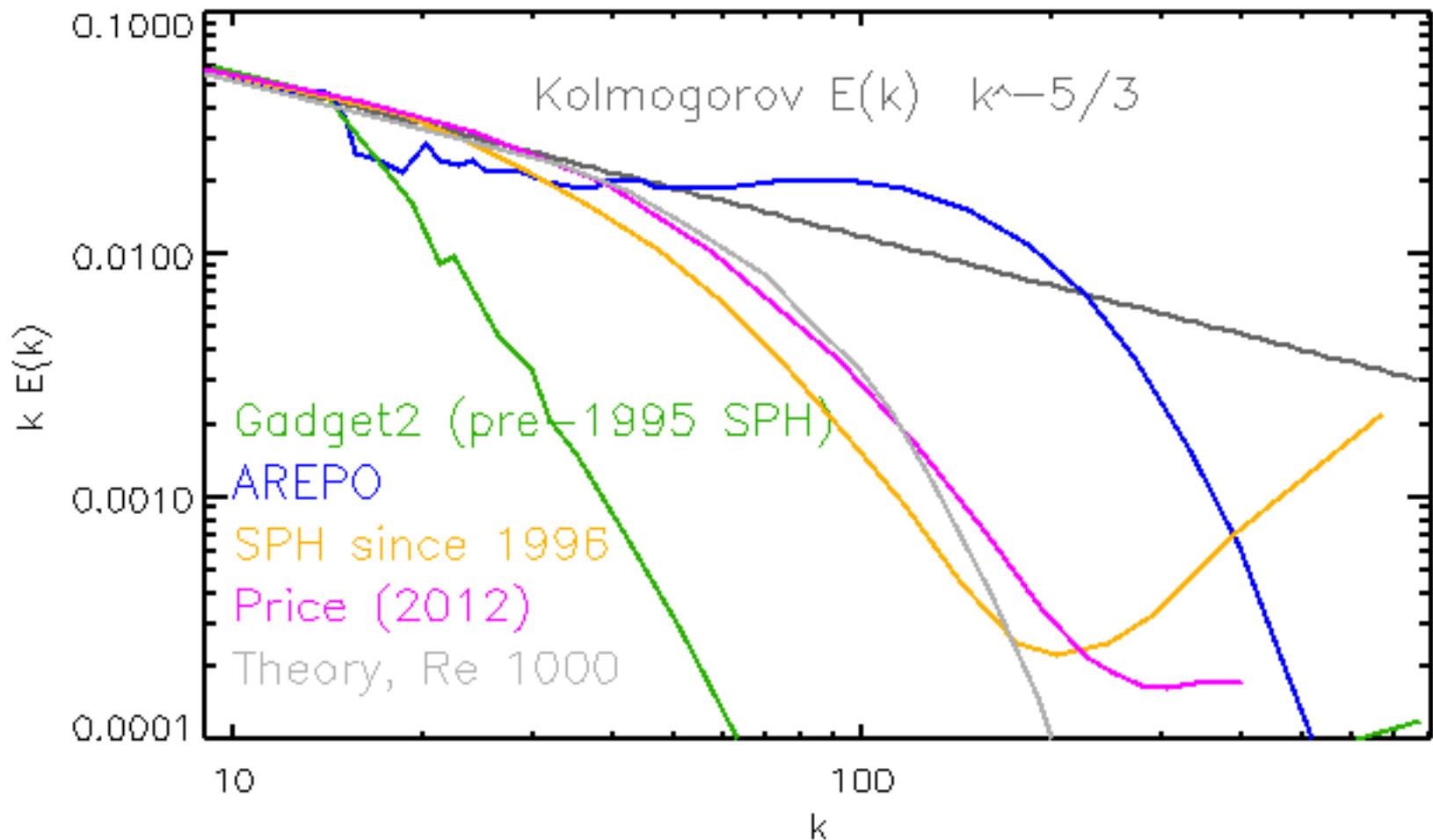
SPH velocity field
(Phantom – Price 2012)

Subsonic Turbulence



SPH dissipation limits the effective Reynolds number
All SPH variants good except non-standard, switch-free Gadget2

Subsonic Turbulence



AREPO & grid codes suffer from bottleneck of excess KE
All codes deviate from Kolmogorov at high k

Subsonic Turbulence

- Turbulence provides effective pressure

$$P_{Eff} = P_{Thermal}(1 + M^2)$$

- Mach No. $M=0.3$ gives $< 10\%$ Effect
- Most power in large modes (similar in all codes)
- Grid (incl. AREPO) few % high, SPH few % low
- Note: Engineers/fluid dynamicists would never use finite volume (e.g. PPM, AREPO) for turbulence
 - Use high order (Spectral methods) with controlled dissipation but poor shock capturing

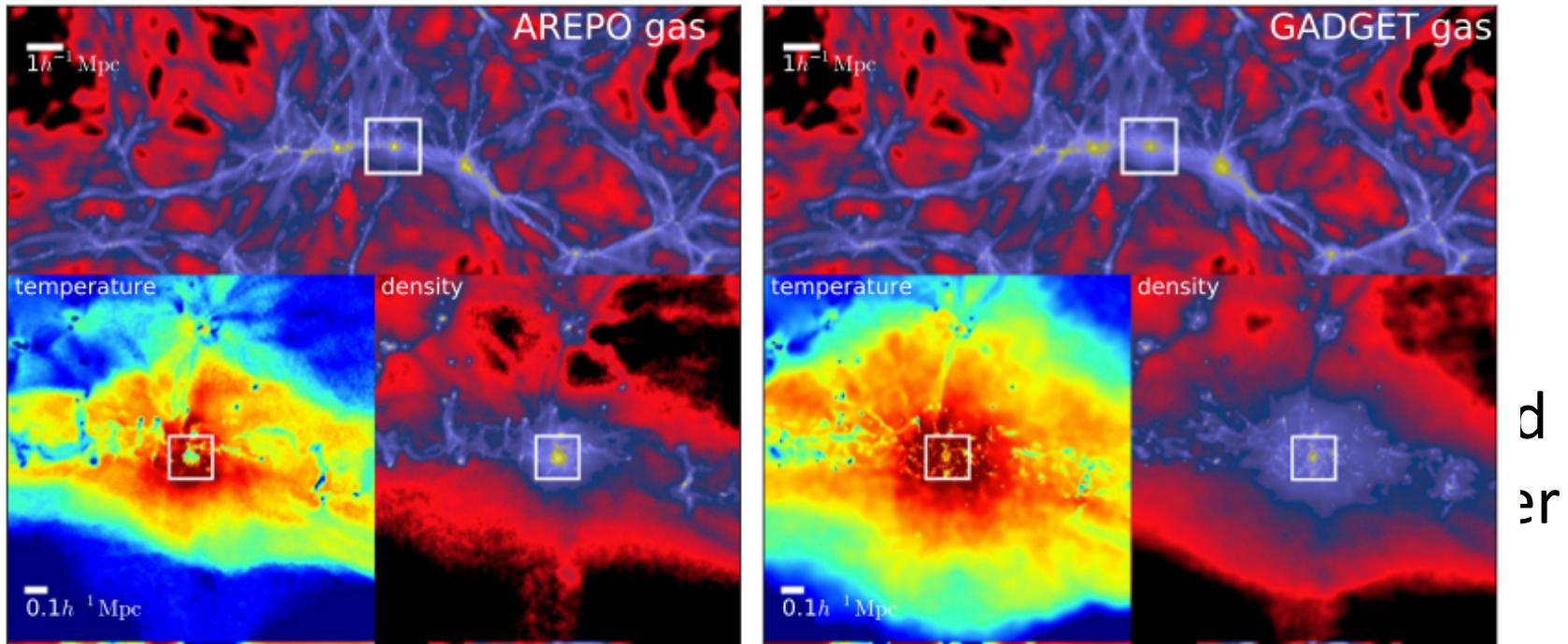
Subsonic Turbulence in galaxy formation

- Post Virial shock, halo gas becomes subsonic
- Grid/SPH bracket reality by few percent up/down

NB: “Excess dissipation” of turbulence into thermal energy would allow it to cool. This implies SPH should be under pressured opposite to claims in Vogelsberger + 2012 / Bauer & Springel 2012

Suspect Vogelsberger+ 2012 result is related to lack of modern switch in Gadget2 for shock heating

Subsonic Turbulence in galaxy formation



Suspect Vogelsberger+ 2012 result is related to lack of modern switch in Gadget2 for shock heating

SPH Galaxies: No more blobs

10^{11} Solar Mass Galaxy (Gasoline)

Old SPH



GD Force + Diffusion



Fabio Governato

- Large scale gas accretion similar, but overall star formation higher
 - feedback less effective
- Mixing → More gas at intermediate Temperatures → more cooling (cf. Eagle, Illustris, Teyssier – strong 300% SN FB)

SPH Galaxies: No more blobs

10^{11} Solar Mass Galaxy (Gasoline)

Old SPH

GD Force + Diffusion

SPH is in the same boat as everyone else
State of Hydro:

Fabio Governato

- Large scale gas accretion similar, but overall star formation higher
 - feedback less effective
- Mixing → More gas at intermediate Temperatures → more cooling (cf. Eagle, Illustris, Teyssier – strong 300% SN FB)

Outstanding issue:

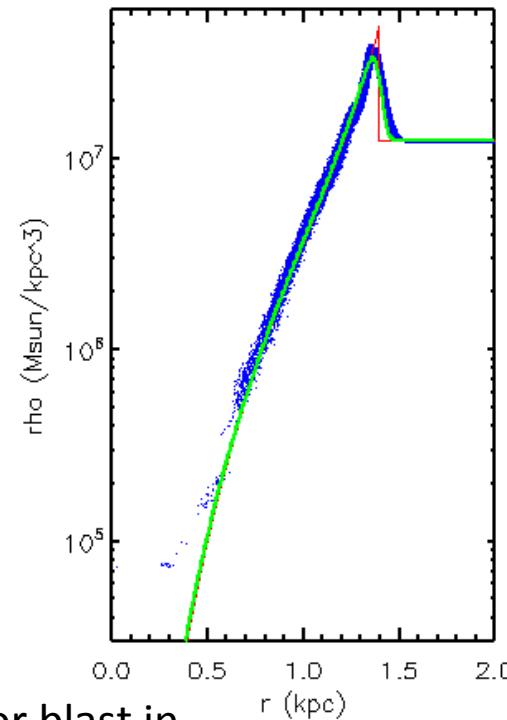
Feedback, Cooling & Mixing

- These processes involve thin layers/small scales no code currently resolves
- Makes feedback less effective, tends to overcool and overmix – not quantified!
- Tricks:
 - Turn Hydro off in winds (Springel & Hernquist 2003 + recent AREPO runs, e.g. Illustris)
 - Extreme “Multiphase” decouple hot & cold (Aumer+ 2013, Scannipieco+ 2006, Marri & White 2003)

Gasoline

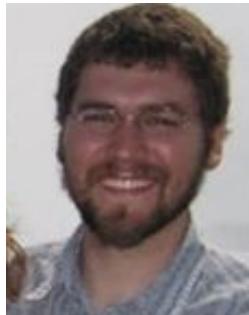
Current Version (2013):

- Fixed number of neighbours (e.g. 64 for Wendland C_2 kernel, Dehnen & Aly 2012)
- Single SPH smooth (no iterations)
- Standard density, geometric density forces
- Turbulent Diffusion (Shen, Wadsley & Stinson 2010)
- f correction to PdV work
- Multisteping power of 2 KDK plus Saitoh & Makino (2009) timestep adjustment



good integrator test: Sedov-Taylor blast in
 $T=0$ K gas (128^3) 0.08 % Energy error

Stellar Feedback



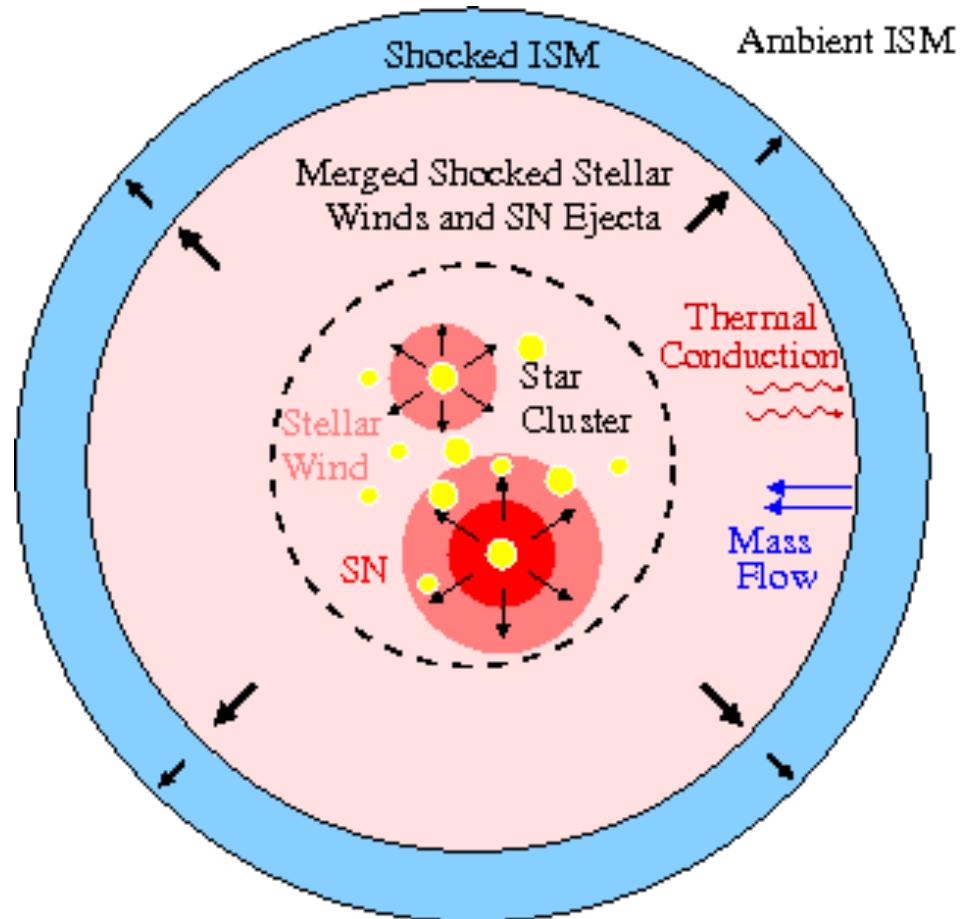
Efficient Stellar Feedback

Keller & Wadsley (in prep)

- Radiation pressure and UV feedback: pre-process medium around star cluster but self-limiting to roughly $v_{\text{esc GMC}} \sim 20 \text{ km/s}$ (for normal galaxies)
- Many stellar feedback ideas based on single supernovae (e.g. Stinson et al. 2006, “blastwave”). Feedback from star clusters is qualitatively different ...
- Stellar winds and supernovae combine into a super bubble that can drive outflows

Super bubble features

- Star cluster output: winds supernova, shock and thermalize in bubble
- Mechanical Luminosity $L=10^{38} \text{ erg/s}/10^4 M_{\text{SUN}}$ cluster
- Thin shell forms quickly: immediately get pressure driven snowplough
- Mass loading of bubble due to evaporation by thermal conduction



MacLow & McCray 1988, Weaver et al 1977, Silich et al 1996

Super bubble features

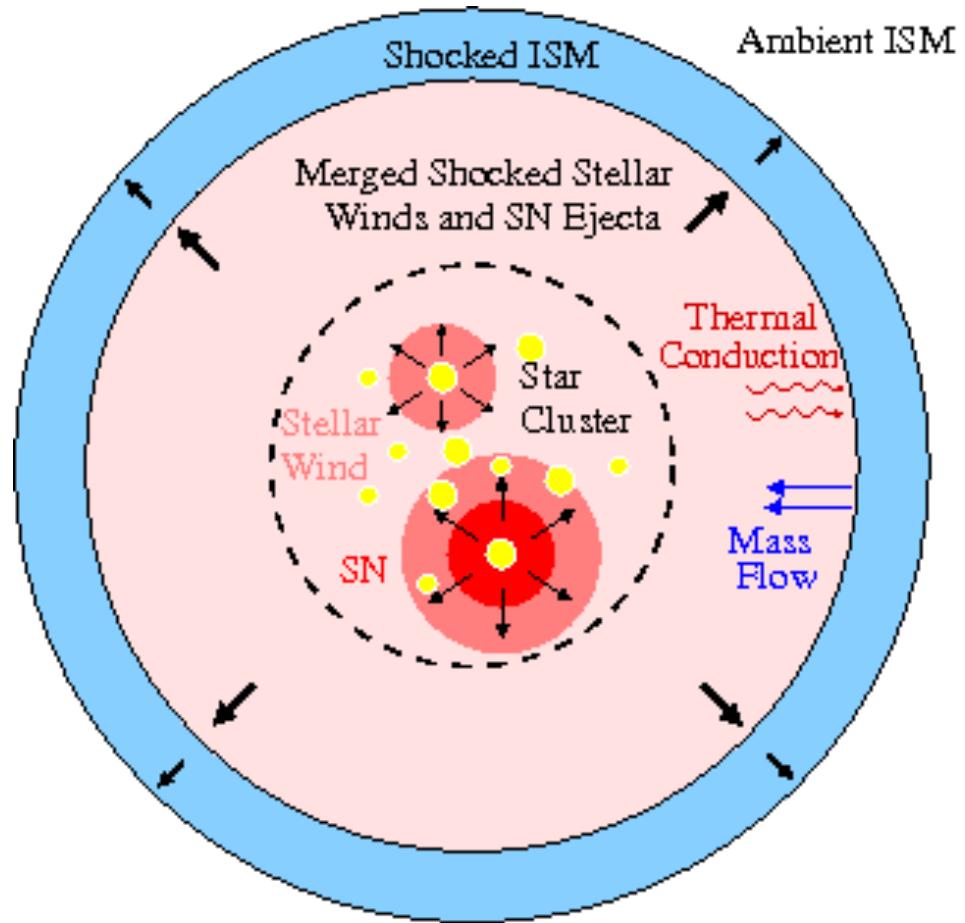
Superbubbles efficient

Ideal self-similar PDS solution

- Thermal Energy: $E_{th} = 0.45 L t$
- Kinetic Energy: $E_k = 0.20 L t$
- Shell radiative losses: $0.35 L t$

Limiting factor: Radiative Cooling of bubble determined by bubble temperature $\sim E_{th}/M_b$ and density M_b/R^3

Hot bubble mass (M_b) set by thermal conduction rate into bubble

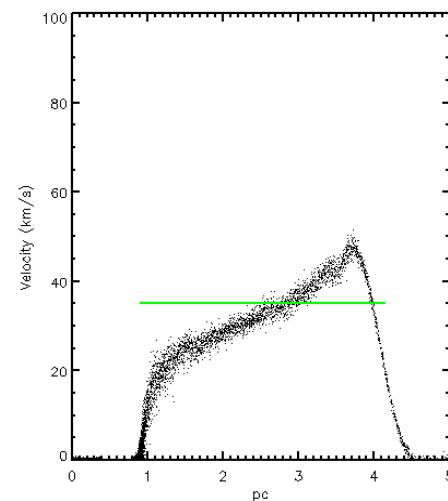
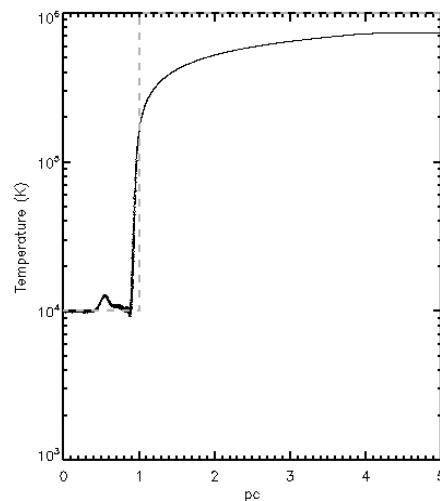
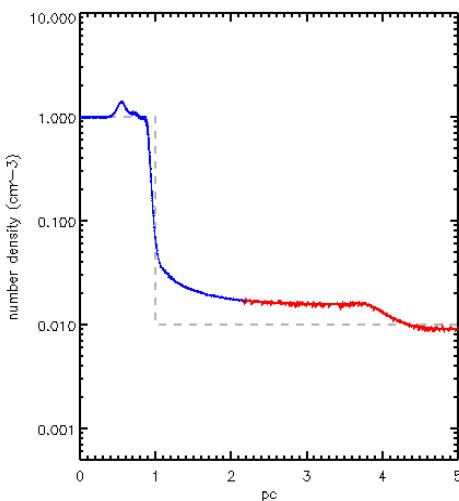


MacLow & McCray 1988, Weaver et al 1977, Silich et al 1996

Thermal Conductivity

$$\frac{\partial E}{\partial t} = \nabla \kappa_{Cond} \nabla T \quad \kappa_{Cond} = 6 \times 10^{-7} T^{5/2} \text{ (cgs)}$$

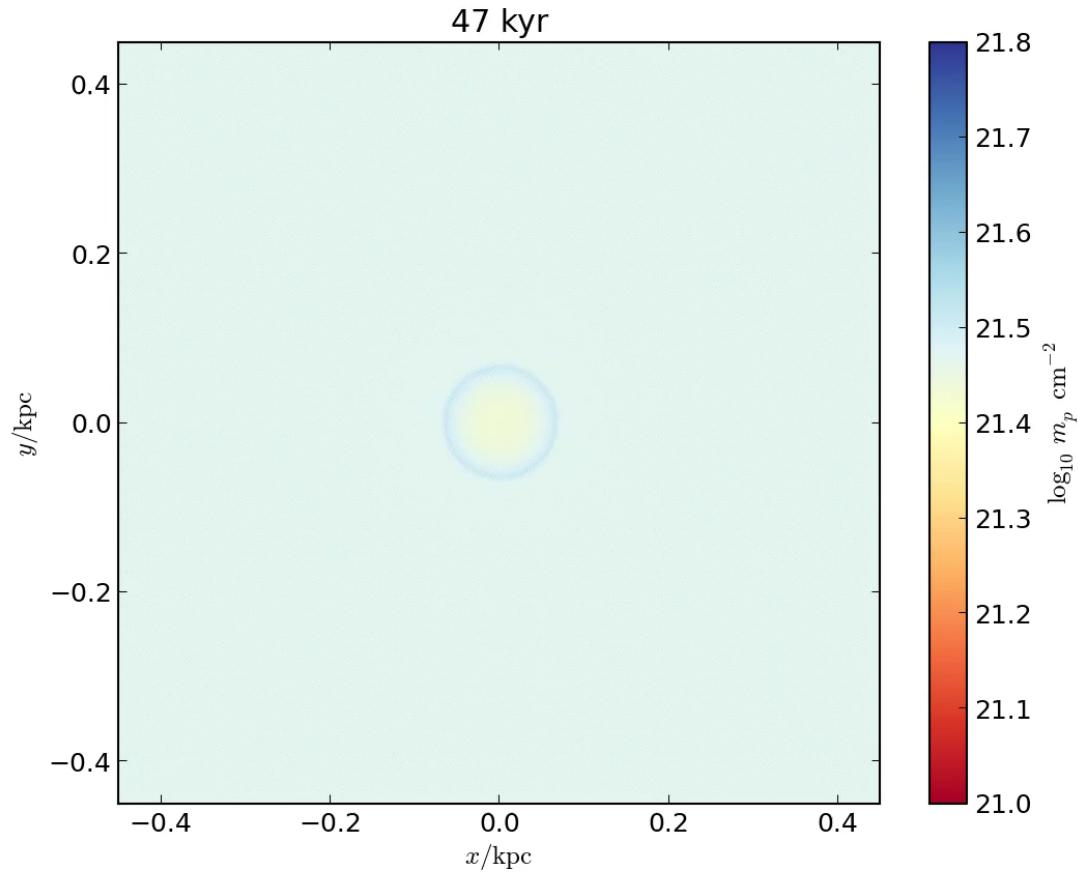
- Self regulating Energy flux $\sim T^{7/2}/L$
- Translates into mass flow from shell until bubble T is lowered to \sim few 10^6 K (Bubble energy, metals conserved)



High-Res
SPH
conductivity
simulation

Gasoline
(method
similar to
Jubelgas et al
2004)

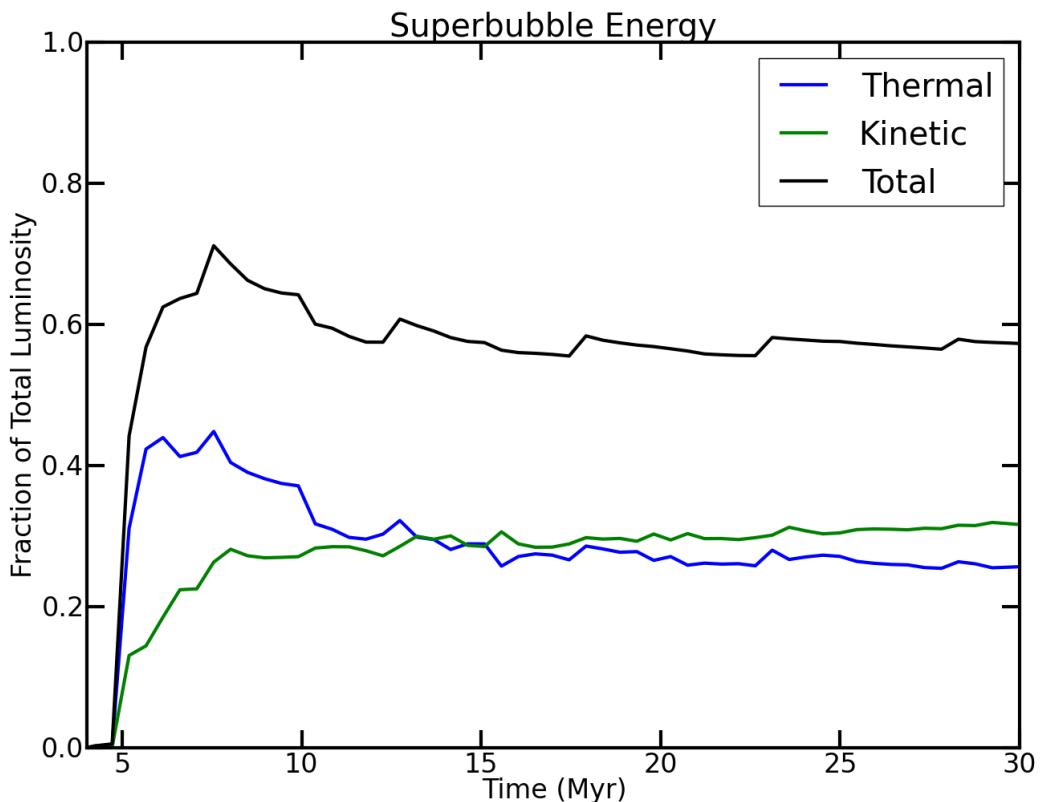
Super bubble Simulation



Super bubble Simulation

- SPH: 750 Msun/particle – similar to galaxy sim
- 3×10^4 Msun star cluster in 1 H/cc,
solar metallicity cooling
- 40 star particles
- 10 gas ejecta

Super bubble Simulation



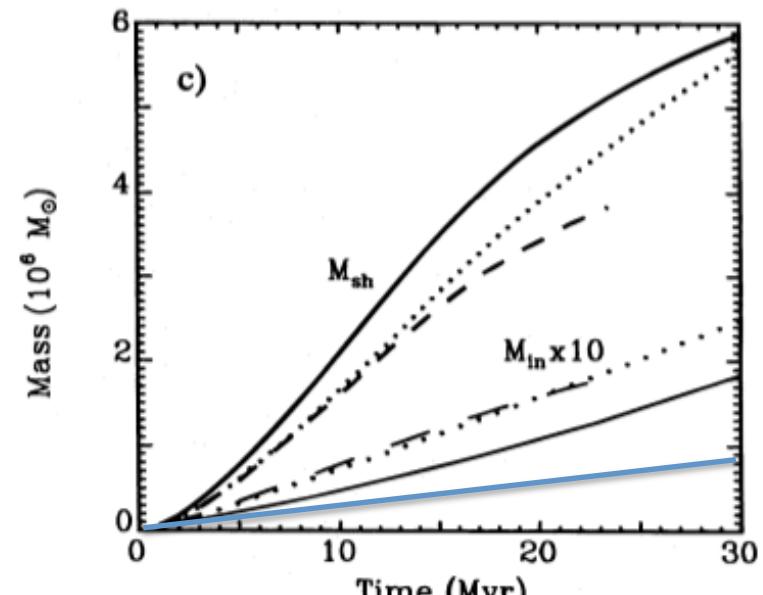
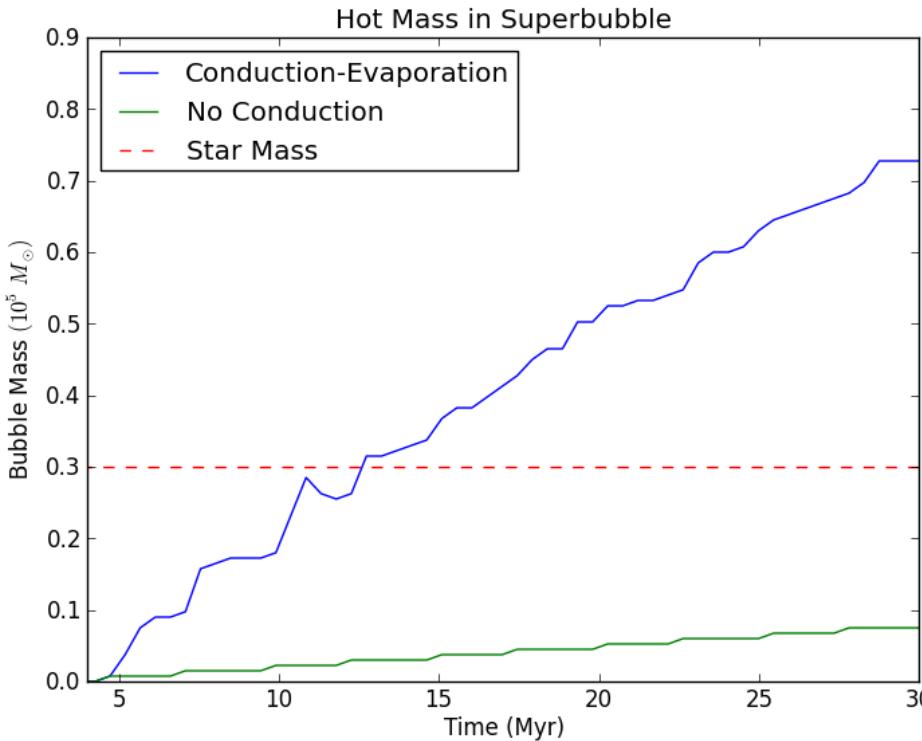
> 50% Feedback
efficiency
After 30 Myr !

Compare: < 10%
for one SN, e.g.
Chevalier '74

Note: Thermal Energy of bubble, KE of shell + bubble

Mass loading

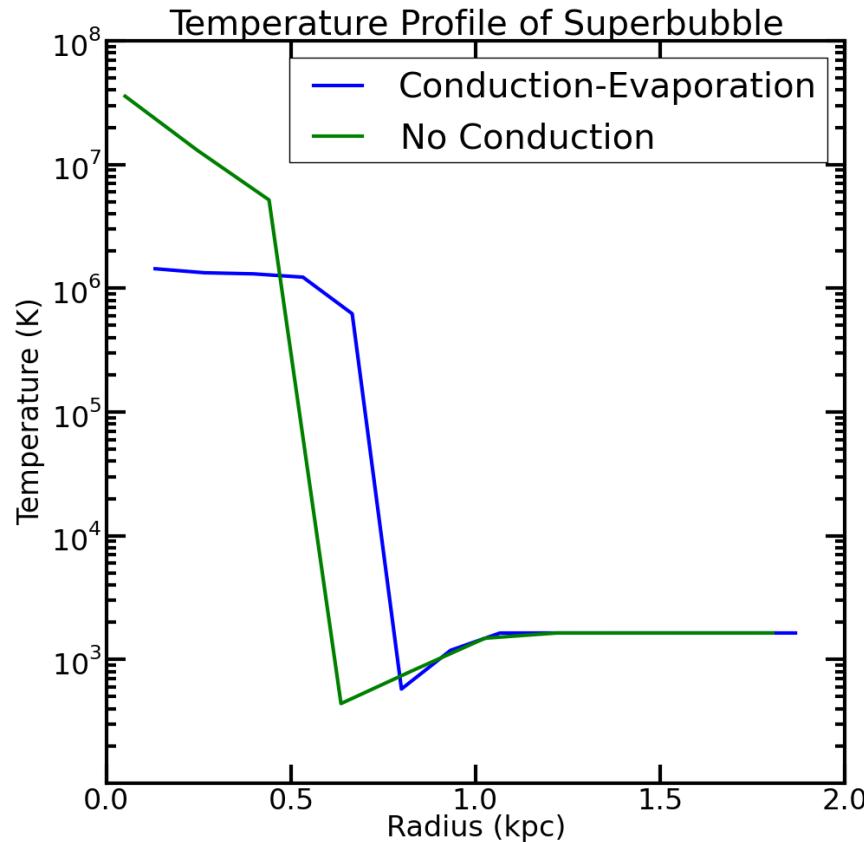
- ~ 100 shell particles evaporated into bubble
- Mass loading $3\text{-}6 M_*$



Silich et al 1996

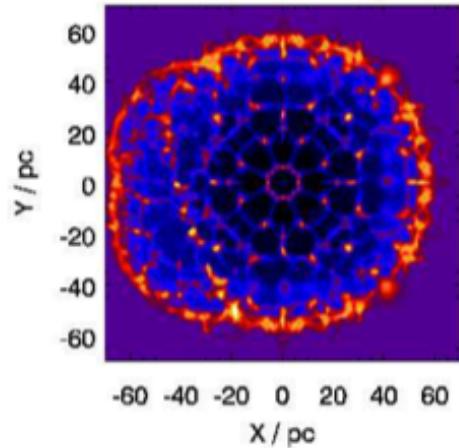
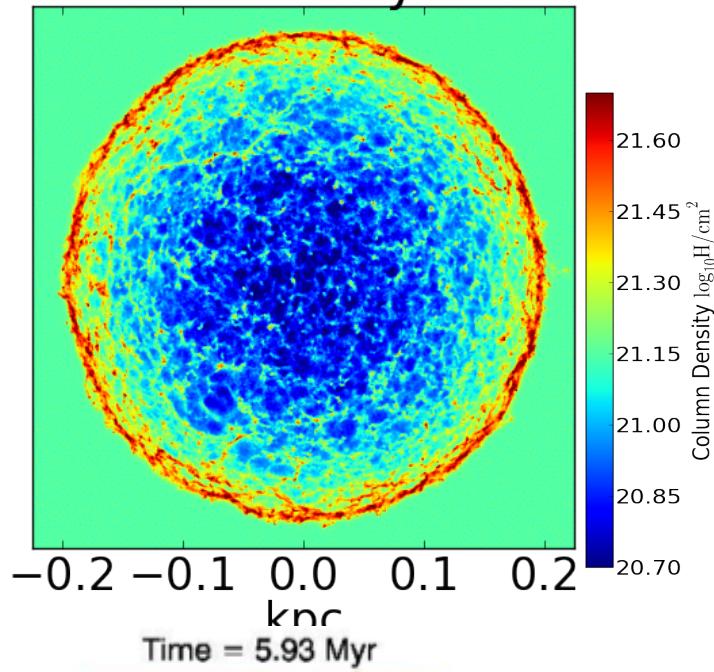
Mass loading

- Bubble temperature regulated at $\sim 2 \times 10^6$ K
(cf. Dalla Vecchia & Schaye 2012)

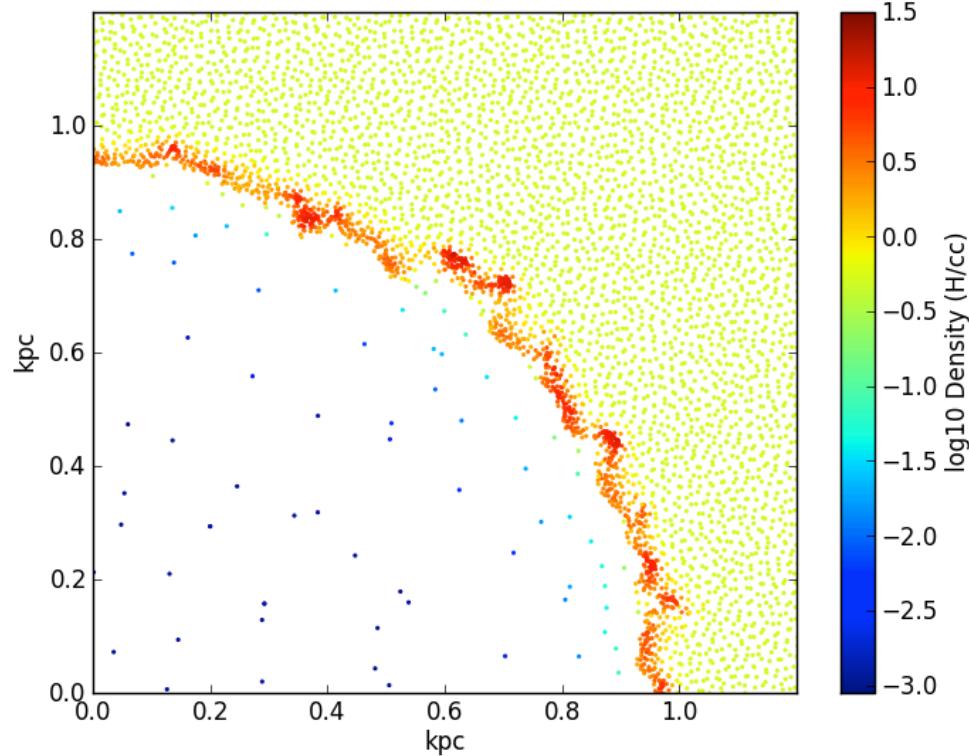


Super bubbles: Vishniac Instabilities

5.429 Myr



Nirvana simulations
3 star bubble
Krause et al 2013



Theory: Vishniac 1983
Sims: McLeod & Whitworth 2013,
Nayakshin et al 2012 (AGN)

Summary:

Super bubble Feedback

- Dalla Vecchia & Schaye (2012) showed the importance of moderate feedback mass ($T_{\text{feedback}} > 10^{6.5} \text{ K}$) for effective feedback
 - but what sets T_{feedback} ?
- Can use physical models (conduction) to determine mass loading and T_{feedback}
- No cooling shutoff
- Much more efficient than individual SN
- Future work: Combined feedback, lumpy ISM