# Observing the Universe(s)

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• The CMB is a 2D projection of a 3D field.



 Different realizations of the random field can give the same CMB.



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• Measuring the power spectrum in a perfect world:



$$C_{\ell} = \frac{1}{2\ell+1} \sum_{m=-\ell}^{\ell} a_{\ell m} a_{\ell m}^*$$

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• There are a finite number of data points in principle.

**Cosmic Variance** 

• Measuring the power spectrum in our world: foregrounds.



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- Astrophysical sources vary significantly with frequency, the CMB does not -- can use maps from different frequencies.



• The measured signal is not completely statistically isotropic-need to understand precisely.







• We observe fluctuations from 10 e-folds in the CMB.

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Can we do better?

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- e.g. we don't see the actual galaxies that the fluctuations in the CMB grow into.

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today







time 1

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 $\mathcal{P}(t=0)$   $\mathcal{P}(t_1)$   $\mathcal{P}(t_2)$   $\mathcal{P}(t_3)$ 

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- With more projections, we can better test our theory of initial conditions and evolution for *probability distributions*.
- Hopefully realized in measurements of the 21cm hydrogen line.

• Finite number of linear modes to measure.

$a^2 - 0$	radiation	matter	dark energy
$c_s = 0$	$\frac{\delta\rho}{\bar{\rho}} \propto \log(a)$	$\frac{\delta\rho}{\bar{\rho}} \propto a$	$rac{\delta  ho}{ar ho} \propto { m const.}$

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can't separate things to arbitrarily large distances

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There is a biggest black hole, and therefore a biggest apparatus and a finite number of states. can't make an arbitrarily large or complicated apparatus

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Any detector is being bombarded by Hawking radiation
# A Finite Amount of information

• Another consequence of a cosmological constant: maximum precision for any conceivable experiment.



Any detector has a finite lifetime

## In Practice

• How do we compare data with theory?



• Test the fit to data, repeat.

Pr(data|model)

• Important part: include other datasets!

## In Practice



6 parameter model still works best!!!

#### Eternal Inflation: is this our universe?





 An infinite number of individually infinite universes in an infinite expanding background?

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non-unique vacuum state

(possible in standard model)

(common in BSM physics)

(inevitable in string theory)

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Thursday, 4 July, 13

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accelerated expansion (observed: dark energy) (inferred: inflation)

### **Observational Tests of Eternal Inflation**

#### Strong theoretical motivation, but is eternal inflation experimentally verifiable?

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 Strong theoretical motivation, but is eternal inflation experimentally verifiable?

Our bubble does not evolve in isolation....



The collision of our bubble with others provides an observational test of eternal inflation.

Aguirre, MCJ, Shomer

#### Making predictions and testing models









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- The outcome is fixed by the potential and kinematics.



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- To study what happens, need full GR.
  - We want to find the post-collision cosmology: GR.
  - Huge center of mass energy in the collision.
  - Non-linear potential, non-linear field equations.



• Numerical simulations with full GR: full dynamics.

$$ds^{2} = -\alpha(x, z)dz^{2} + a(x, z)dx^{2} + z^{2}dH_{2}^{2} \qquad \phi(x, z)$$





1.8 × 10<sup>-10</sup>

• Numerical simulations with full GR: full dynamics.

$$ds^{2} = -\alpha(x, z)dz^{2} + a(x, z)dx^{2} + z^{2}dH_{2}^{2} \qquad \phi(x, z)$$

0.010

• 2 types of bubbles from false vacuum.

0.005

0.000

 $\phi_A \phi_B \phi_C$ 

-0.005

1.5

2.0

2.5



Numerical simulations with full GR: full dynamics.

 $ds^{2} = -\alpha(x, z)dz^{2} + a(x, z)dx^{2} + z^{2}dH_{2}^{2}$   $\phi(x, z)$ 



- 2 types of bubbles from false vacuum.
- Slow roll inflation inside one, starting near  $\phi_C$  .



Colliding identical bubbles.



- After the collision, fields linearly superpose: potential key.
- Dynamics necessary!



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 Colliding different bubbles.  $\phi_C$  $\phi_B$  $\phi_{\Delta}$ X

Colliding different bubbles.



Colliding different bubbles.



Colliding different bubbles.



Inflation does not end, there are new perturbations!























Symmetry+causality: effects confined to a disc.



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Generic signature (thanks inflation!):

$$\frac{\Delta T(\mathbf{\hat{n}})}{T} \simeq f(\mathbf{\hat{n}}) + \delta_{\Lambda CDM}(\mathbf{\hat{n}})$$

f : analytic arguments and numerics

Feeney, MCJ, Mortlock, Peiris Chang, Kleban, Levi Gobetti & Kleban





Symmetry+causality: effects confined to a disc.

• Generic signature (thanks inflation!):










 Counting only collisions whose disc of influence is smaller than the whole sky:



$$N \simeq \frac{16\pi\lambda}{3H_F^4} \left(\frac{H_F^2}{H_I^2}\right) \sqrt{\Omega_c}$$

also Kleban et. al.





 The collisions are very nearly isotropic, and the distribution of disc sizes on the CMB sky relatively flat:





• The model:





• The model:





• The model:









 $\bar{N}_s$ 

m

The model: generic signature  $V^{(\phi)} = \int_{\phi} \int$ 

expected number of collisions

parameters characterizing each collision

 $\Pr(N_s, \mathbf{m})$  How many of each type do I expect to find?

#### Collisions (exaggerated) + CMB + instrumental noise



#### Collisions (realistic) + CMB + instrumental noise



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Lambda-CDM: very successful at describing the CMB power spectrum.





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• Are there anomalies?

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- Are there anomalies?
- Frequentist statistics: how discrepant is the data assuming the null hypothesis?

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- Frequentist statistics: how discrepant is the data assuming the null hypothesis?

Bayesian model selection: does one model fit the data better than another?

• The goal:  $P(Model, \Theta \mid data)$ 



#### How should I bet?

Bayes' Theorem:

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How should I bet?

 $P(\text{Model}, \Theta \mid \text{data}) = \frac{P(\Theta)P(\text{data} \mid \text{Model}, \Theta)}{P(\text{data} \mid \text{Model})}$ 

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$$P(\text{data} | \text{Model}) = \frac{P(\text{data} | \text{Model})}{P(\text{data} | \text{Model})}$$

- Theory prior:  $P(\Theta) \qquad \int P(\Theta)d\Theta = 1$
- Likelihood:  $P(\text{data} | \text{Model}, \Theta)$

• Evidence (model averaged likelihood):  $P(\text{data} \mid \text{Model})$ 

$$P(\text{data} | \text{Model}) = \int d\Theta P(\Theta) P(\text{data} | \text{Model}, \Theta)$$

 The likelihood is used to quantify how consistent data is with a set of model parameters.

 $P(\text{data} | \text{Model}, \Theta)$ 

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$$P(\text{data} | \text{Model}, \Theta) \xrightarrow{\text{exclusion plots}} P(\text{data} | \text{Hode}, \Theta) \xrightarrow{\text{exclusion plots}}$$

N= 50 60 λφ<sup>4</sup> • • m<sup>2</sup>φ<sup>2</sup> • Ο

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 This does NOT tell us how we should rank competing theories trying to describe the same data.

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• To do so, we can apply Bayes' theorem at the level of Models:

$$P(\text{Model} \mid \text{data}) = \frac{P(\text{Model})P(\text{data} \mid \text{Model})}{P(\text{data})}$$

 Let's say I have a model that fits the data fairly well, should I introduce a more complicated model that might fit it even better?  Let's say I have a model that fits the data fairly well, should I introduce a more complicated model that might fit it even better?

• We can decide by looking at the evidence ratio:

 $\frac{P(\text{Model 1} \mid \text{data})}{P(\text{Model 0} \mid \text{data})} = \frac{P(\text{Model 1})P(\text{data} \mid \text{Model 1})}{P(\text{Model 0})P(\text{data} \mid \text{Model 0})} = \frac{P(\text{data} \mid \text{Model 1})}{P(\text{data} \mid \text{Model 0})}$ 

#### Bayesian model selection

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 The evidence naturally implements Occam's razor: the simpler model should be favored. Tension between volume of parameter space and goodness of fit.

$$P(\text{data} | \text{Model}) = \int d\Theta P(\Theta) P(\text{data} | \text{Model}, \Theta)$$

# Is This Significant?



- Model I: Lambda CDM.
- Model 2: Stephen Hawking's creation, signed copy.

 $\frac{\Pr(\text{Model 1}|\text{data})}{\Pr(\text{Model 2}|\text{data})} = \frac{\Pr(\text{Model 1})}{\Pr(\text{Model 2})} \frac{\Pr(\text{data}|\text{Model 1})}{\Pr(\text{data}|\text{Model 2})}$ 

• What any good Bayesian wants:



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• A convenient theory label:  $\bar{N}_s\,$  .  $\Lambda {\rm CDM}$  is specified by  $\,\bar{N}_s=0\,$  .

The expected number of detectable features.











- To calculate this, need to test for:
  - Arbitrary number of templates
  - Arbitrary position on the sky
  - Arbitrary amplitude, shape, and size (lying within prior  $\Pr(N_s, \mathbf{m})$ )


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#### Implementing the exact calculation is impossible.

- Solution:
  - Locate candidate features with a blind analysis.



- Solution:
  - Locate candidate features with a blind analysis.
  - Find an approximation to the probability by integrating only over the regions of parameter space where the contribution is large.



- Filter the CMB (wavelet decomposition, optimal filtering)
- Judge significance of features against expectations from LCDM.
- Calibrate with simulations that don't contain collisions.

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- Blind search for candidates:
  - Keep candidates that lie above threshold:



• For one candidate:



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Evidence ratio in the blob: how much better does one describe the data by adding a template?

• For one candidate:



Evidence ratio in the blob: how much better does one describe the data by adding a template?

- Pixel-based likelihood  $L_b(\mathbf{d}|\mathbf{m})$  contains: CMB cosmic variance, beam, and spatially varying noise.
- Flat prior on amplitude and shape, prior on size and position from theory.



• The general expression for  $N_b$  candidates:



# WMAP7 W-Band (94 GHz)



#### The WMAP7 W-Band data.....

# WMAP7 W-Band (94 GHz) : Candidates



# WMAP7 W-Band (94 GHz) : Posterior



The data does not support the bubble collision hypothesis.

# WMAP7 W-Band (94 GHz) : Posterior



The data does not support the bubble collision hypothesis.

From the shape of the posterior, we can rule out

$$N_s < 1.6$$
 at  $68\%$  CL



Check for signals in other datasets.

### Polarization signal



Czech et. al. Kleban et. al.



Check for signals in other datasets.





Czech et. al. Kleban et. al.

#### Planck res. with noise



### corroborating evidence?

### $\bar{N}_s < 1.6$ at $68\%~{\rm CL}$

### • What region of theory space have we constrained?

Novel connection between numerical relativity and observational cosmology!

### $\bar{N}_s < 1.6$ at $68\%~{\rm CL}$

- What region of theory space have we constrained?
- Numerical simulations are needed to connect the potential to the template!

