## SPATIAL SEARCHES IN ASTRONOMY DATABASES MULTI-DIMENSIONAL INDEXING FOR SIMULATIONS AND OBSERVATIONS

## Storing Simulations

$\square$ Millennium Run (MPA)

- 10 billion particles, 64 snapshots
- FoF groups and merger trees
$\square$ Millennium XXL
- 300 billion particles
$\square$ MultiDark - Bolshoi
$\square$ Turbulence simulations (JHU)
- $1024^{4}$ grid, 27TB


## Storing Simulations

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## Observing Simulations

$\square$ Comparison to real observations
$\square$ Lots of spatial searches
$\square$ In the database?


## Sky Coverage

$\square$ For precise window function
$\square$ Virtual surveys


## Outline

$\square$ Query shapes in SQL
$\square$ Indexing with space-filling curve
$\square$ Combine for spatial searches
$\square$ Periodic boxes
$\square$ Celestial sphere


## Databases

$\square$ Which one to use depends on the task
$\square$ Sqlite, MySQL, PostGRES, DB2, Oracle, SQL Server

- Free "express versions" of the big ones, too
$\square$ Customization is a must
$\square$ There is always something missing
- Extend by loading your libraries


## Query Shapes

Geometric primitives

$\square$ Sphere, Box, Cone...

## Query Shapes

$\square$ IShape interface
TopoPoint Contains(Point p);
TopoShape GetTopo(Box b);
Box GetBoundingBox();
$\square$ Geometric primitives
$\square$ Sphere, Box, Cone...

## Query Shapes

$\square$ IShape interface
TopoPoint Contains(Point p);
TopoShape GetTopo(Box b);
Box GetBoundingBox();
$\square$ Composites

- Intersect, Union, Difference...


## Query Shapes

## $\square \mathrm{In}$ SQL <br> $\square$ UDT

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```
/* Sphere */
|eclare @s Sphere = Sphere::New (1,2,3,10);
    -- Check if a point is inside
-select @s.ContainsPoint (1,2,3), @s.ContainsPoint (99,0,0);
    go
    /* Box */
\square \mp@code { d e c l a r e ~ @ b ~ B o x ~ = ~ B o x : ~ : ~ N e w ~ ( 0 , 0 , 0 , 1 0 , ~ 1 0 , ~ 1 0 ) ; }
select @b.ContainsPoint (1,2,3), @b.ContainsPoint (99,0,0);
Lselect @b.ToString(); -- string representation
    go
```

    /* String Representation */
    $\square$ declare @x Box $=$ 'BOX $[0,0,0,10,10,10] '$
$L_{\text {select }}^{6}$ (x.ContainsPoint $(1,2,3)$, @x.ContainsPoint $(99,0,0)$;
go

## Query Shapes

$\square$ Generic
$\square$ UDT
Boolean
$\square$ Methods

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```
/* Generic Shapes */
\squaredeclare @a Shape = 'BOX [0,0,0, 10,10,10]';
    select @a.ContainsPoint (1,2,3), @a.ContainsPoint (99,0,0)
select @a.ToString();
    go
```

    /* Boolean Algebra */
    $\square$ declare @s1 Shape $=$ 'BOX $[0,0,0,10,10,10] ' ;$
declare @s2 Shape $=$ 'SPHERE $[0,0,0,5]$ ';
declare @sU Shape $=$ Shape: : NewUnion (@s1, @s2);
declare @sI Shape $=$ Shape: : NewIntersection (@s1, @s2);
declare @sD Shape $=$ Shape: : NewDifference (@s1, @s2);
select @sU.ToString() union all
select @sI.ToString() union all
select @sD.ToString();
go

## Query Shapes

## $\square$ Generic <br> $\square$ UDT

## Boolean

/* Generic Shapes */
$\square$ declare @a Shape $=$ 'BOX $[0,0,0,10,10,10]^{\prime} ;$
select @a.ContainsPoint $(1,2,3)$, @a.ContainsPoint $(99,0,0)$ select @a.ToString();
go

```
/* Using the parser */
\squaredeclare @u Shape, @i Shape, @d Shape;
Gselect @u = 'UNION [BOX[0,0,0,2,2,2], SPHERE[0,0,0,2]]', 2);
    @i ='INTERSECTION [BOX[0,0,0,2,2,2], SPHERE[0,0,0,2]]',
    @d = 'DIFFERENCE [BOX[0,0,0,2,2,2], SPHERE[0,0,0,2]]';
```

Lselect @sD.ToString();
ISSAC at HiPACC
go

## Indexing Tables

$\square$ Better performance of queries

- Instantaneous range searches
- Fast JOINs
$\square$ Syntax

$$
\begin{gathered}
\text { CREATE INDEX ix_Name ON Table } \\
\text { (X ASC, ...) INCUDE (V, ...) }
\end{gathered}
$$

## Multi-Dimensional

$\square$ Map the space to a simple index
$\square$ Different kinds of Space-Filling Curves
$\square$ Morton's Z-curve
$\square$ Peano-Hilbert Curve

## Peano-Hilbert Curve

## $\square$ Hierarchical space filling

First Order


## Peano-Hilbert Curve

## $\square$ Hierarchical space filling

First Order


Second Order
012
H1H1H1H1H11H


## Peano-Hilbert Curve

## $\square$ Hierarchical space filling

First Order


Second Order


## Third Order



## Peano-Hilbert Curve

## $\square$ Hierarchical space filling

First Order


Second Order
012



Third Order


## The Hilbert Curve

## Also others...

$\square$ Morton Z-order
$\square$ Simple bit interleave


Second Order
O 12
H1H1H1+1H1+1H


The Z-Order Curve
$\square$ Which one to use?
$\square$ Statistical analyses

- Correlation fn

First Order


## Second Order





## Divide and Conquer



## Covers for Shapes

## $\square$ Inside approximation $\square$ Outside overshoot



## Covers for Shapes

$\square$ Inside approximation
$\square$ Outside overshoot
$\square$ They are Key ranges

| Level 0 |
| :---: | :---: | :---: |
| Level 1    <br> 2 3   <br> 0 1   <br> 10 11 14 15 <br> 8 9 12 13 <br> 2 3 6 7 <br> 0 1 4 5 |

## Covers for Shapes

## $\square$ Inside approximation

$\square$ Outside overshoot
$\square$ They are Key ranges

| Level 0 | Level 1 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 11 14 15  <br> 2 3    <br> 0 9 12 13  <br> 2 3 6 7  <br> 0 1 1 4 5 |  |  |  |

Key between 0 and 3

## Covers for Shapes

## $\square$ Inside approximation

$\square$ Outside overshoot
$\square$ They are Key ranges

| Level 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 3   <br> 0    <br> 0 11 14 15 <br> 8 9 12 13 <br> 2 3 6 7 <br> 0 1 4 5 |

## Covers for Shapes

## $\square$ Inside approximation

$\square$ Outside overshoot
$\square$ They are Key ranges

| Level 0 Level 1 | Level 2 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 10 11 14 15  <br> 2 3 9 12 13 <br> 0 1 3 6 7 <br> 0 1 4 5  |  |  |  |

## Covers for Shapes

## $\square$ Inside approximation

$\square$ Outside overshoot
$\square$ They are Key ranges


## Periodic Boundaries

$\square$ Infinite with periodicity
$\square$ Have to search all boxes


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## Searching in SQL

$\square$ Key filter
$\square$ By Cover
$\square$ ShiftX,-Y,-Z $\square$ Where?

```
    /* Peano-Hilbert Cover */
\square \mp@code { G e l e c t ~ * ~ f r o m ~ f S i m u l a t i o n C o v e r ( ~ s i m s . M i l l i M i l ( ) , }
    'SPHERE[0,10,10,5]' ,5);
    go
```

    /* Cover translates the search onto built-in index */
    $\square$ declare @s Shape $=$ 'SPHERE $[0,10,10,5]$ ';
Њwith Cover (Fullonly, KeyMin, KeyMax, Shiftx, Shifty, Shiftz)
as (
select * from fSimulationCover(sims.MilliMil(), @s, 5)
where Fullonly $=1$-- inside cover
)
select $h . H a l o I D, h . X+c . S h i f t X$ as $X$,
h. Y + C. ShiftY as $Y$,
h. Z + C.ShiftZ as Z
from MilliMil..MpaHalo h inner join Cover c
on h.PHKey between c.KeyMin and c.KeyMax
-where SnapNum $=63$

## Real!

## $\square$ E.g.,

/* Multiple searches around POI */
bwith QueryShapes (FoFID,Shape) as
select top 10 FoFID, Shape::NewSphere (X,Y, Z, 10)
from MilliMil..FoF
where SnapNum=63 order by M_TopHat200 desc
select distinct s.FoFID, g.GalaxyID, g.X+c.ShiftX as X,
g.Y+c.ShiftY as Y,
g. Z+c.ShiftZ as Z
from QueryShapes s
cross apply fSimulationCover(sims.MilliMil(),s.Shape,5) c
inner join MilliMil..DeLucia2006A g
on g.PHKey between c.KeyMin and C.KeyMax
where g. SnapNum=63
and ( (c.Fullonly=1) -- Inner cover
or
(c.Fullonly=0 -- Boundary cover and $1=$ s. Shape. ContainsPoint ( $\mathrm{g} . \mathrm{X}+\mathrm{c}$.ShiftX, g. Y + c.ShiftY, g.Z+C.ShiftZ))

## Online Interfaces





## Web Services

$\square$ Programming interfaces
$\square$ Execute SQL queries

- Most flexible
$\square$ Inject probes in simulations
- Turbulence
- Cosmology


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Sky Coverage


## No Sky Coverage?

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Figure 1. SDSS colour composite image (vri) for our prototype unusual galaxy cluster, at RA $=16^{\mathrm{h}} 23^{\mathrm{m}} 76^{\mathrm{s}}$, Dec $=+97^{\circ} 62^{\prime} 12^{\prime \prime}$, identified by Galaxy Zoo participants. North is at the top, East is to the left.

## Spherical Geometry



## Approaches to Consider

$\square$ Pixel maps
$\square$ Sensitivity, etc...
$\square$ Equations of shapes
$\square$ Spherical "vector graphics"
$\square$ And beyond...

## An Observation

$\square$ FITS header with WCS
$\square$ Image dimensions map to the geometry
$\square$ More exposures?
$\square$ No common pixel coordinate-system
$\square$ Overlapping areas

## Common Pixels

$\square$ Pre-defined pages of an atlas

- Standard in cartography
$\square$ Image pyramids of hierarchical pixels
- Including HTM, Igloo, HEALPix, SDSSPix, etc...

$\square$ Always approximate!


## Practical Implementation

$\square$ Looking at Terapixels
$\square$ We know how to work with images
$\square$ Now have commodity Internet

- We have cheap hard-drives

WorldWideTelescope.org Sky in Google Earth
$\square$ Integrated catalogs for efficiency
$\square$ How about more surveys?

## Drawing with Equations

$\square$ Working with 3D normal vectors
$\square$ Benefits include
$\square$ No wraparound
$\square$ No projections
$\square$ No singularities


## Drawing with Equations

$\square$ Direct 3D approach
$\square$ Halfspace $\rightarrow$ Circle/Cap
$\square$ Convex $\rightarrow$ Simple shapes
$\square$ Region

- Unions of convexes
$\square$ Patches on the sphere



## Point in Region Test

$\square$ Halfspace: one side of a plane ( $\vec{n}, c$ )

- Inside, when $\vec{n} \cdot \vec{x}>c$
$\square$ Convex: a collection of halfspaces
- Inside, when inside all halfspaces
$\square$ Region: a collection of convexes
$\square$ Inside, when inside any convex


## Shape Operations

$\square$ Intersection
$\square$ Concat halfspace lists
$\square$ Union
$\square$ Concat convex lists
$\square$ Unique coverage

- Analytic area
$\square$ Boolean algebra



## Difference of Convexes is a Region

$\square$ The set of Regions is closed for the Boolean ops


## Simplification

$\square$ Eliminate redundant halfspaces

- First handle trivial combinations of constraints
$\square$ Then solve geometry on the surface - Derive Roots, Arcs, Patches
$\square$ Eliminate redundant convexes
- Some trivial cases, but...
$\square$ Make convexes disjoint
- Unique coverage, area, etc.
$\square$ Stitch together convexes
- When possible



## SphericalLib .NET

$\square$ C\# code $\sim 10$ k lines
$\square$ OS independent (Windows, Un*x w/ Mono)
$\square$ Documentation via Sandcastle
$\square$ Great performance!
$\square$ Sloan Digital Sky Survey in 10s
( $13 \times$ larger than USA in area)

## Numerical Imprecision

$\square$ Double precision calculations

- IEEE 754 standard
$\square$ Degeneracy
- When are two vectors the same?
$\square$ Spatial resolution limit
- Roughly 30 cm on Earth
$\square$ Lots of tricks from Graphics Gems


Sky coverage of the Sloan Digital Sky Survey's $5^{\text {th }}$ Data Release and the Galaxy Evolution Explorer's 2 ${ }^{\text {nd }}$ Public Release

## Region in SQL

```
DECLARE @S VARCHAR (MAX), @r VARBINARY (MAX),
    @z VARCHAR (MAX), @u VARBINARY(MAX)
SELECT @S = 'REGION CIRCLE J2000 180 0 60',
    @z = 'POLY J2000 180 0 182 0 182 2 180 2',
    @r = sph.fSimplifyString(@s),
    @u = sph.fUnion(@r,sph.fSimplifyString(@z))
SELECT sph.fGetArea(@r), sph.fGetArea(@u)
-- 3.14151290574491 6.35572804450646
/*
    SQL Server Execution Times:
        CPU time = 0 ms, elapsed time = 1 ms.
*/
```


## Footprint Services

$\square$ All about coverage

- Editor and calculator
$\square$ Online public repository
- On-the-fly visualization
- STC translator, etc...
$\square$ Web services
- Simple programming

http://voservices.net/footprint


## ASTRONOMICAL DATA ANALYSIS SOFTWARE AND SYSTEMS XVI

The Westin La Paloma Resort \& Spa Tucson, AZ, USA
15-18 October 2006






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Edited by
Richard A. Shaw, Frank Hill and David J. Bell

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## Hybrid Solutions



## Heuristic Simplification

## $\square$ Before and After



## Indexing the Sky

$\square$ Hierarchical Triangular Mesh

$\square$ Region approximation
$\square$ Fast filtering using HTM ID ranges


## Anatomy of an SDSS Region



## HTM Filtering

```
WITH Cover AS
(
    SELECT * FROM dbo.fHtmCoverRegion
            ('REGION CIRCLE J2000 180 0 10')|
)
SELECT o.ObjID
FROM PhotoObj AS o INNER JOIN Cover AS c
    ON O.HtmID BETWEEN c.HtmIDStart AND c.HtmIDEnd
```


## Summary

$\square$ Store simulations, e.g., the reference Millennium
$\square$ Simulations take 10x longer than analysis
$\square$ Databases enable fast searches
$\square$ Custom routines
$\square$ Space-filling curves
$\square$ Direct comparison of observed universe to sims

