The University of California High-Performance AstroComputing Center

#### International Summer School on AStro-Computing: Galaxy Simulations

### Introduction

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### What we will do:

- Lectures on different codes: what they can do, how to use them, how to understand results, algorithms ...
- Physics of galaxy formation: how galaxies form, how star formation affects them, different aspects and physical processes
- Projects:
  - use codes to make small runs
  - analyze results of more realistic simulations

Dark Matter is the backbone for formation of galaxies.

Filamentary distribution of dark matter is mirrored by baryons









### Milky Way formation: DM



Madau, Diemand, Kuhen





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Ceverino & Klypin 2007

z=3.5 Major progenitor of MW. 45 pc resolution Face-on view

#### 400 kpc proper



Cold Flow regime

Slice of temperature

#### Galaxies in simulations look like real ones



Agertz, Teyssier, Moore 2010

### Codes:

Туре	Name	Main features	Largest runs
AMR	Enzo	Block splitting, PPM hydro sover MPI parallelization, Shock capturing, C++ and Fortran	64G particles 1000 processors
	ART	Cell splitting, MUSCLE hydro MPI+OpenMP parallelization, Shock capturing all possible combinations of F77/F90/C	N-body: 8G particles, I 3824 processors Hydro: 10-200pc
	RAMSES	Cell splitting MPI parallelization, Shock capturing F90	64G particles (Horizon run), 20000 processors
TREE	gasoline/ PKDgrav	Tree, MPI, C	IG particles
	GADGET-2	Tree-PM, MPI, C	N-body: 300G particles, 14K cores Hydro: 1G particles, 200-300 pc
analysis	Sunrise	Radiative transfer, AMR	

#### **ENZO:** block splitting

Distributed hierarchy

Grid zones



Norman & Bryan 98

*Figure 2.* 1D Zeldovich pancake test problem. 3-level solution (symbols) is overlaid on 256 zone uniform grid solution (solid line).

### ART/RAMSES: cell splitting







### ART/RAMSES: cell splitting





### ART/RAMSES: cell splitting



### Adaptive Refinement:

Mesh is refined where the density exceeds a given threshold. Other quantity (such as jumps in pressure) can be used as additional condition for refinement. Refinement field defines how refinement is done.

Each cell can be split into 8 new cells, each having twice smaller size. This is ideal for tracing anisotropic structures such as filaments.

Adjacent cells can differ not more than by one level

Time-step decreases by factor two with each level

ARTístic family



### ARTístic family

#### ART N-body code



ARTistic family



ARTístic family



### History:

Ø Particle-Mesh (PM): 1980, Klypin & Shandarin Adaptive Mesh Refinement (AMR) with irregular mesh: 1996, Khokhlov N-body ART: 1997, Kravtsov, Klypin, Khokhlov Hydro OpenMP: 2000 Kravtsov, Khokhlov Hydro MPI: 2005 Rudd, Kravtsov Radiative Transfer: 2004–5, Gnedin, Kravtsov

### ART: gravity

Poisson equation  $\nabla^{2}\phi = \rho$   $\phi_{i,j,k}^{n+1} = \phi_{i,j,k}^{n} + \frac{\Delta\tau}{\Delta^{2}} \left(\sum_{nb=1}^{6} \phi_{nb}^{n} - 6\phi_{i,j,k}^{n}\right) - \rho_{i,j,k}\Delta\tau$   $\phi_{i,j,k}^{n+1} = \frac{1}{6} \left(\sum_{nb=1}^{6} \phi_{nb}^{n} - 6\phi_{i,j,k}^{n}\right) - \frac{\Delta^{2}}{6}\rho_{i,j,k}$ 

Diffusion equation with fake time: stationary solution is the Poisson equation



### ART: time-stepping

### equations $\frac{dp}{dt} = -\nabla_x \phi$ , $\frac{dx}{dt} = \frac{p}{a^2}$ $\nabla_x^2 \phi = 4\pi G a^2 (\rho - \overline{\rho})$ $\frac{d\tilde{p}}{da} = -f(\Omega_M, \, \Omega_\Lambda, \, a)\tilde{\nabla}\tilde{\phi} \,,$ $\frac{d\tilde{x}}{da} = f(\Omega_M, \, \Omega_\Lambda, \, a) \, \frac{\tilde{p}}{a^2} \,,$ $\tilde{\nabla}^2 \tilde{\phi} = \frac{3\Omega_M}{2a} \left( \tilde{\rho} - 1 \right) \,.$

$$f(\Omega_M, \Omega_\Lambda, a) = \frac{1}{\sqrt{1 + \Omega_M(1/a - 1) + \Omega_\Lambda(a^2 - 1)}}$$

dimensionless variables

$$\begin{split} x &= x_0 \, \tilde{x} \,, \quad t = \tilde{t} / H_0 \,, \quad \phi = \tilde{\phi} (x_0 \, H_0)^2 \,, \\ p &= \tilde{p} (x_0 \, H_0) \,, \quad \rho = \tilde{\rho} \, \frac{3 H_0^2}{8 \pi G} \frac{\Omega_M}{a^3} \,, \end{split}$$



Fefinement



Time

Fefinement



Time

Fefinement



Time

Fefinement



Time

Fefinement



Time

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Time

Fefinement



Time



Time



Time


Time



Time



Time



Time



Time



Time



Time



Time



Time



Time



Time



Time



Time

- Scale of the time-step is defined by the time-step at the zero-level mesh
- On each subsequent level of refinement the time-time step decreases by factor two.
- For a particle moving with a constant speed the fraction of a cell, which it crosses per one time-step is independent on the level of refinement at which the particle moves.
- Courant condition": particles should not move more than a fraction of a cell per step. It is a global (refinement level independent) condition
- In practice, maximum particle displacement is 0.1-0.2 of a cell.

### **Equations**

$\begin{split} \frac{\partial \tilde{\rho}}{\partial \tilde{t}} + \tilde{\nabla} \tilde{\rho} \tilde{\mathbf{v}} &= 0, \\ \frac{\partial \tilde{\mathbf{v}}}{\partial \tilde{t}} + (\tilde{\mathbf{v}} \cdot \tilde{\nabla}) \tilde{\mathbf{v}} &= -\frac{\tilde{\nabla} \tilde{P}}{\tilde{\rho}} - \tilde{\nabla} \tilde{\phi}, \\ \frac{\partial \tilde{E}}{\partial \tilde{t}} + \tilde{\nabla} \cdot \left[ (\tilde{E} + \tilde{P}) \tilde{\mathbf{v}} \right] &= -\tilde{\rho} \tilde{\mathbf{v}} \cdot \tilde{\nabla} \tilde{\phi} + \tilde{\rho} \tilde{H} (2\tilde{\varepsilon} - 3\tilde{P}/\tilde{\rho}) + (\tilde{\Gamma} - \tilde{L}), \end{split}$	
물리가 지갑 지금은 것이야? 여름이 많이 한다.	$ ilde{ abla}^2  ilde{\phi} = 6 a  ilde{\delta},$
	$ ilde{arepsilon} = rac{1}{\gamma-1} rac{ ilde{P}}{ ilde{ ho}},$
$\tilde{t}_0 \equiv \frac{2}{H_0} \frac{1}{\sqrt{\Omega_0}},$	
$v_0 \equiv rac{r_0}{t_0},$	
$ ho_0 ~\equiv~ {3H_0^2\over 8\pi G}\Omega_0,$	
$\phi_0 \;\; \equiv \;\; rac{r_0^2}{t_0^2} = v_0^2,$	Units: r <sub>0</sub> = cell size at zero level
$P_0 \equiv  ho_0 v_0^2,$	
$arepsilon_0 ~\equiv~ rac{P_0}{ ho_0} = v_0^2,$	

dimensionless variables

 $ilde{\mathbf{r}} \equiv a^{-1} rac{\mathbf{r}}{r_0},$  $d\tilde{t} \equiv a^{-2}\frac{dt}{t_0},$  $ilde{
ho} ~\equiv~ a^3 ~ rac{
ho}{
ho_0},$  $ilde{\mathbf{v}} \equiv a \; rac{\mathbf{v}}{v_0},$  $ilde{\phi} ~\equiv~ a^2 ~rac{\phi}{\phi_0},$  $egin{array}{rcl} ilde{P} &\equiv& a^5 \; rac{P}{P_0}, \ ilde{arepsilon} &\equiv& a^2 \; rac{arepsilon}{arepsilon_0}, \end{array}$ 

With a Artic to the shifts

## ART: test of strong shock solution



#### Heitmann et al 2008

# Code comparison: evolution of perturbations

64Mpc/h box 256\*\*3 particles





ART vs Gadget on cosmological simulations

z=2 correlation function of halos with Vcirc > 270km/s

overmerging in Millennium runs (blue)

Comparison of P(k) evolution in ART and Gadget-2 codes. This is for **1Gpc/h** box with **1G particles**. The same initial conditions were used for the runs. The Gadget run and the plot was produced by Ch.Wagner. The vertical line is the Nyquist frequency of particles. Gadget suppresses the growth of fluctuations at high frequencies by 5-20%. The difference gets smaller at low redshifts and practically undetected at z < 1.



# Stellar-dynamics: formation of a barred isolated (not cosmological) galaxy:

# Code comparison: pretty good



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 $\rho_{\rm gas}$  is the gas density

au star formation timescale.

 $\tau$  should be in the range 2-20 Myr.

$$\frac{du}{dt} + p\nabla \cdot \mathbf{v} = \Gamma - \Lambda$$

where u is the internal energy per unit volume  $\Gamma$  is the heating rate due to stellar feedback,  $\Gamma = \rho_{*,young}\Gamma'$ The cooling rate  $\Lambda = n_H^2 \Lambda'$ ,

### **Conditions for star**

formation (Cen & Ostriker 92):

- (I) contracting flow
- (2) cooling time less than dynamic time
- (3) Jeans unstable
- (4) spread energy over 27 cells

### Resolution: 200 pc.

GALAXY SIZE PROBLEM AT z = 3: SIMULATED GALAXIES ARE TOO SMALL M. Ryan Joung1, Renyue Cen1, and Greg L. Bryan 2009

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Figure 3. Rotation velocity curves for the three galaxies labeled "1," "2," and "3" in Figure 1. The solid curves represent rotation velocities due to all the matter within a given galactocentric radius, while the dotted curves show those due to stellar mass only. The virial masses of the three galaxies are  $8 \times 10^{11}$ ,  $4 \times 10^{11}$ , and  $1 \times 10^{11} M_{\odot}$ , respectively.

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With this resolution none of the conditions are justified or even relevant. Apply those conditions to our Galaxy: they would not work.

V<sub>cir</sub> (km s<sup>-1</sup>)

This is an example of misplaced physical arguments: good arguments applied on wrong scales. They are fine for sub-pc scales of individual stars, not for a large chunk of a galaxy.

<u>As the result of unrealistic feedback</u> <u>conditions modeled "galaxies" are totally</u> unrealistic.



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## What are the observational constraints?

- Fraction of baryons: much lower than previously estimated
- Flat rotation curves
- Disk size appropriate for galaxies
- Reasonable Bulge/Disk ratios
- Star formation prescriptions

# Baryon Fractions and outflows



This is what happens when 1/2 of baryons are in galaxies: no way to fit observations

Conclusions: most of baryons must be expelled from galaxies. This argues for a strong feedback. Metallicites of QSO absorption lines point in the same direction

Abundance-matching: mass in stars and cold gas inside virial radius of dark matter halos required in order to produce observer Luminosity Function in r-band Trujillo et al 2010

Fraction of 'cold' baryons is very small: at best 1/5 of cosmological baryons inside virial radius.



Here is the usual argument why LCDM should predict acceptable (in general terms) disk lengths:

- typical spin parameter (measure of rotation) of dark matter halos is  $\lambda = 0.03$
- assume that baryons and dark matter rotate in the same way
- Virial radius of a Milky-Way-size galaxy is 300 kpc
- In order to get to  $\lambda = 1$  (rotationally supported), baryons need to shrink
  - by a factor of 30
- This gives a disk of 10 kpc as observed.

This heuristic argument works as long as most of baryons end up in the central galaxy.

It badly fails if - as required by observations - only a small fraction of baryons fall to the central galaxy.

In this case one expects that only the baryons, which collapsed at high redshifts turn into stars. Indeed, disk of our MW galaxy is very old and was in place more than 10 Gyrs ago.

The angular momentum of the gas, which came into MW at high z was small and cannot produce an extended observed disk.

Conclusions: significant gas outflow or mixing must have happened.

Physics

It is easy to get lost in the forest of feedback schemes unless we pay attention to physics: how the prescription affects motion of gas in a forming galaxy.

It is also very easy to argue that other's pet prescription does not work.

$$\frac{d\rho_{*,\text{young}}}{dt} = \frac{\rho_{\text{gas}}}{\tau}$$

 $\rho_{\rm gas}$  is the gas density  $\tau$  star formation timescale.

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- Runaway stars: stars migrate away from GMCs and deposit energy in low-density environment



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 Runaway stars: stars migrate away from GMCs and deposit energy in low-density environment

Science english	russian-english	situation
blast-waves	no cooling	Most of energy of SF is lost inside GMC.Archaic model of ISM. GMC are not disrupted by SNs
galactic winds	kicking out particles	It should happen, but this approximation is a bit too rough
semi analytical models	curse	nothing wrong, but needs imagination

# Bulgeless dwarf galaxies and dark matter cores from supernova-driven outflows

F. Governato<sup>1</sup>, C. Brook<sup>2</sup>, L. Mayer<sup>3</sup>, A. Brooks<sup>4</sup>, G. Rhee<sup>5</sup>, J. Wadsley<sup>6</sup>, P. Jonsson<sup>7</sup>, B. Willman<sup>9</sup>, G. Stinson<sup>6</sup>, T. Quinn<sup>1</sup> & P. Madau<sup>8</sup>

Strong feedback can produce a realistic model of dwarf galaxy.

Blast-wave = no cooling feedback



#### The formation of disk galaxies in a $\Lambda \text{CDM}$ universe

Oscar Agertz<sup>1\*</sup>, Romain Teyssier<sup>1,2</sup> and Ben Moore<sup>1</sup>

We argue that previous attempts to form disk galaxies have been unsuccessful because of the universal adoption of strong feedback combined with high star formation efficiencies. Unless extreme amounts of energy are injected

We show that a low efficiency of star-formation more closely models the sub-parsec physical processes, especially at high redshift. We highlight the successful formation of extended disk galaxies with scale lengths  $r_{\rm d} = 4 - 5$  kpc, flat rotation curves and

 $\Delta t = 50 \,\mathrm{Myr}.$ 

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<u>1977</u>). To allow for this to take place, we turn off cooling  $\Delta t = 50 \text{ Myr.}$ in the cells containing young stars to allow for the blastwave to grow and be resolved by few cells, hence converting

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# Our implementation

Kravtsov ART hydro code: Physical processes included:



Runaway stars: massive stars move with exp(-v/17km/s)

#### Ceverino & Klypin 2007



Fig. 1.— Rate of energy losses per unit mass from a single stellar population. Top panel shows the results from the STARBURST99 code, assuming a Miller-Scalo IMF for a mass range  $(0.1-100) M_{\odot}$ .

$$\frac{d\rho_{*,\text{young}}}{dt} = \frac{\rho_{\text{gas}}}{\tau}$$

au =2-20 Myrs

Effective  $\tau$  =150-1000 Myrs

Mass consumption rate per free-fall time averaged over gas "molecular" gas (n>30cm<sup>-3</sup>) is 0.03

# Growth of a disk after a major merger



The disk grows in mass and size after a merger

# Conclusions: You are coming to the galaxy formation in right time: so much is unknown and so much is expected