

Selected Stories



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**Chapter I: *Halo concentration,*
in which we discover three stages of halo
*formation***

The Bolshoi simulation

ART code

250Mpc/h Box

ΛCDM

$s_8 = 0.82$

$h = 0.70$

8G particles

1kpc/h force resolution

$1e8 M_{\text{sun}}/h$ mass res

dynamical range 262,000

time-steps = 400,000

NASA AMES

supercomputing center

Pleiades computer

13824 cores

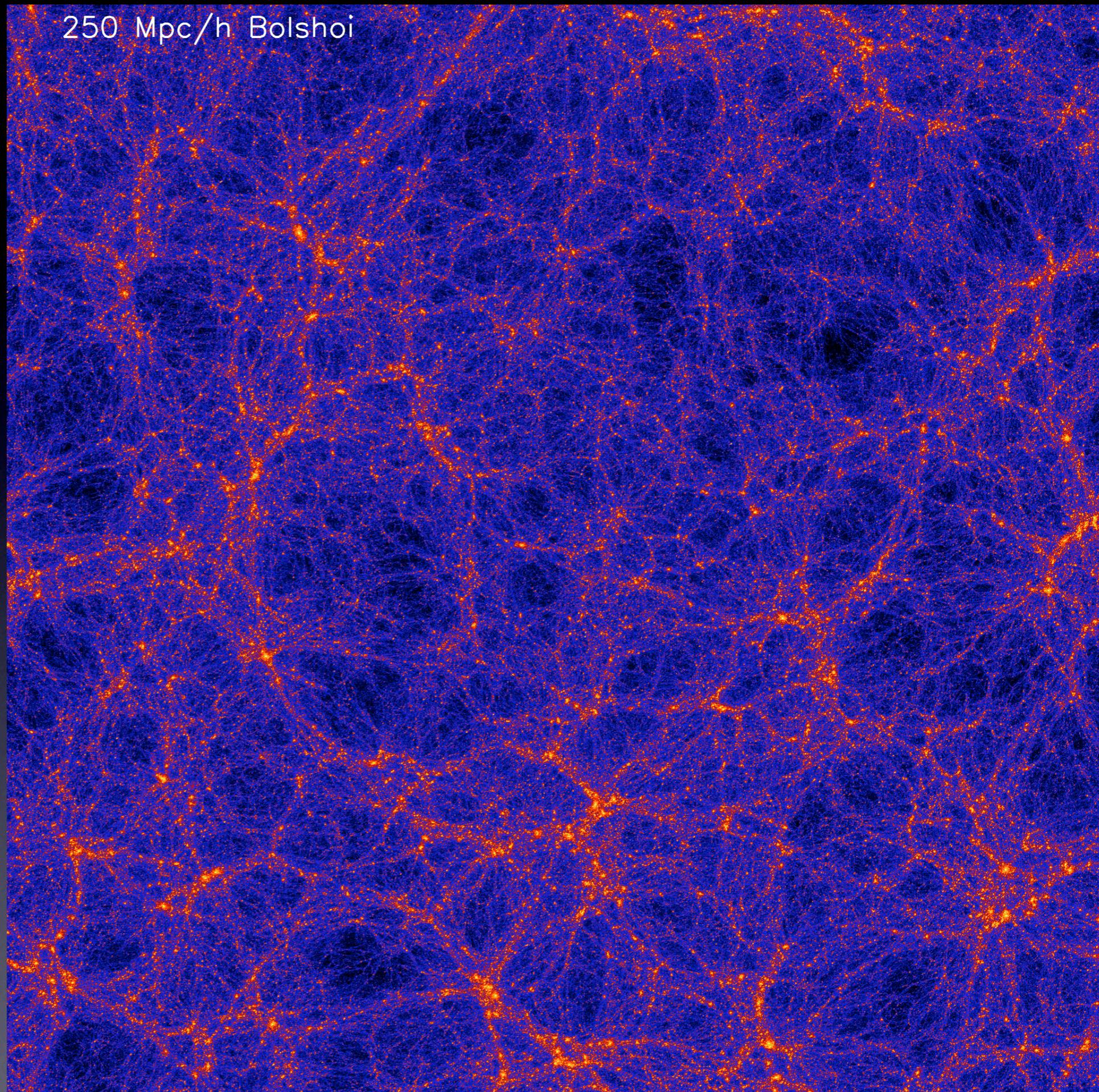
12TB RAM

75TB disk storage

6M cpu hrs

18 days wall-clock time

250 Mpc/h Bolshoi



Halo Concentration: $C = R_{\text{vir}}/R_s$

Why it is important

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Why it is important

Basic property of DM halos: you need it if you do anything with DM halos.

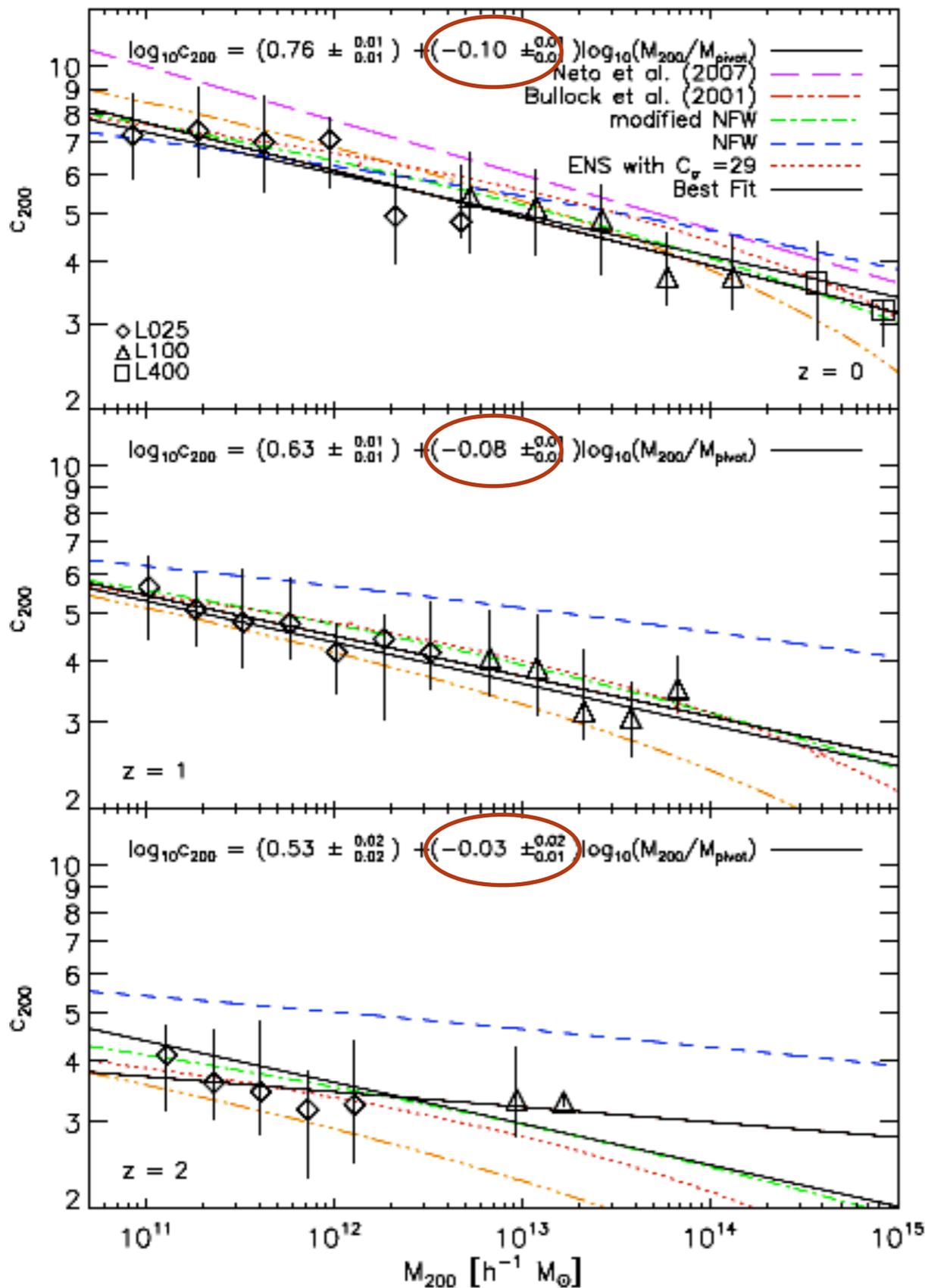
Basic property of DM halos: you need it if you do anything with DM halos.

Tells us how halos formed.

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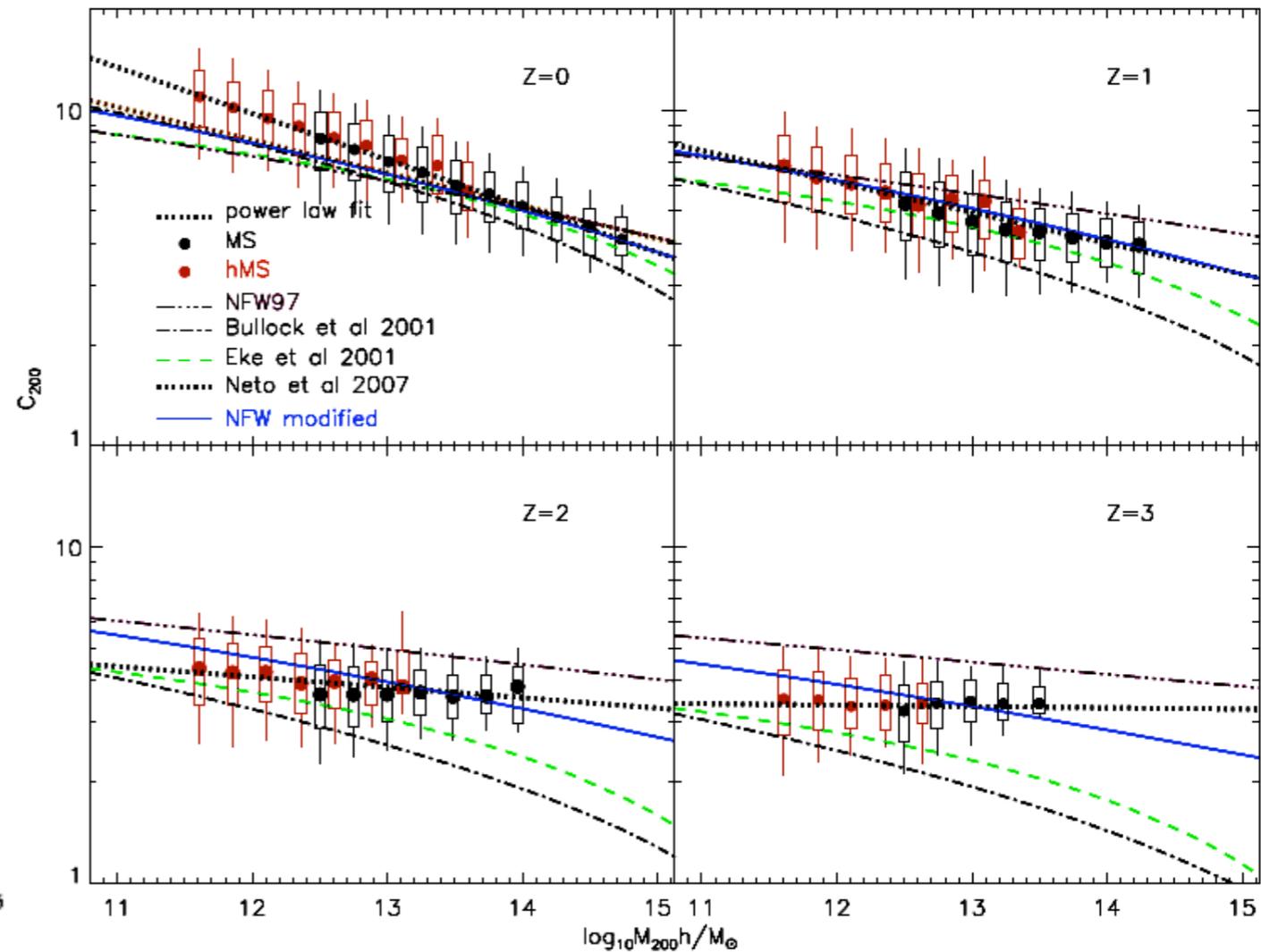
Need high-quality data



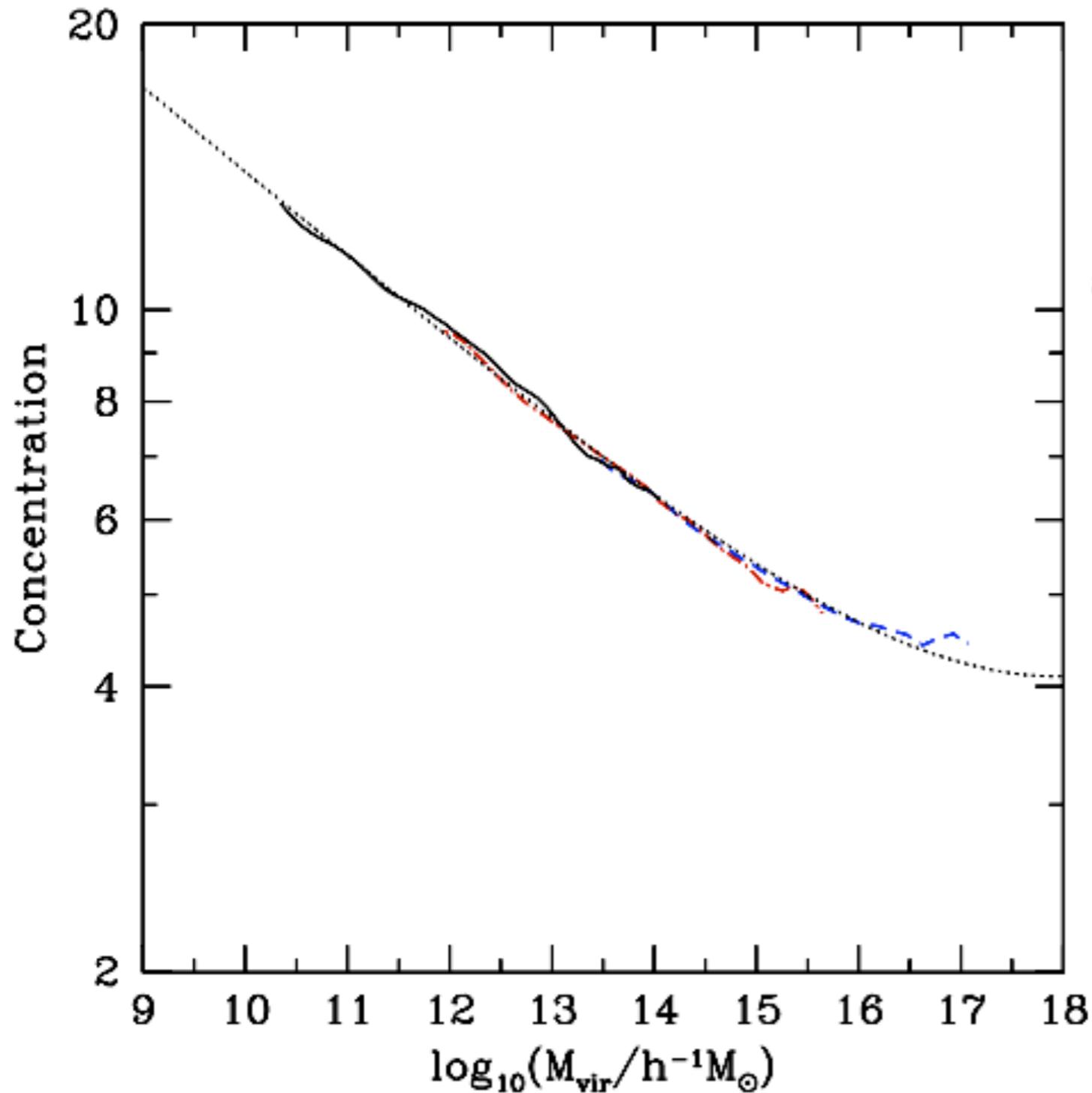
Duffy et al 2007

At $z=0$ $C(M)$ is almost a power law
 Slope gets shallower at high z

Gao et al 2008



Klypin et al 2010



$$c(M_{\text{vir}}) = 9.35 \left(\frac{M_{\text{vir}}}{10^{12} h^{-1} M_{\odot}} \right)^{-0.09}$$

and for subhalos:

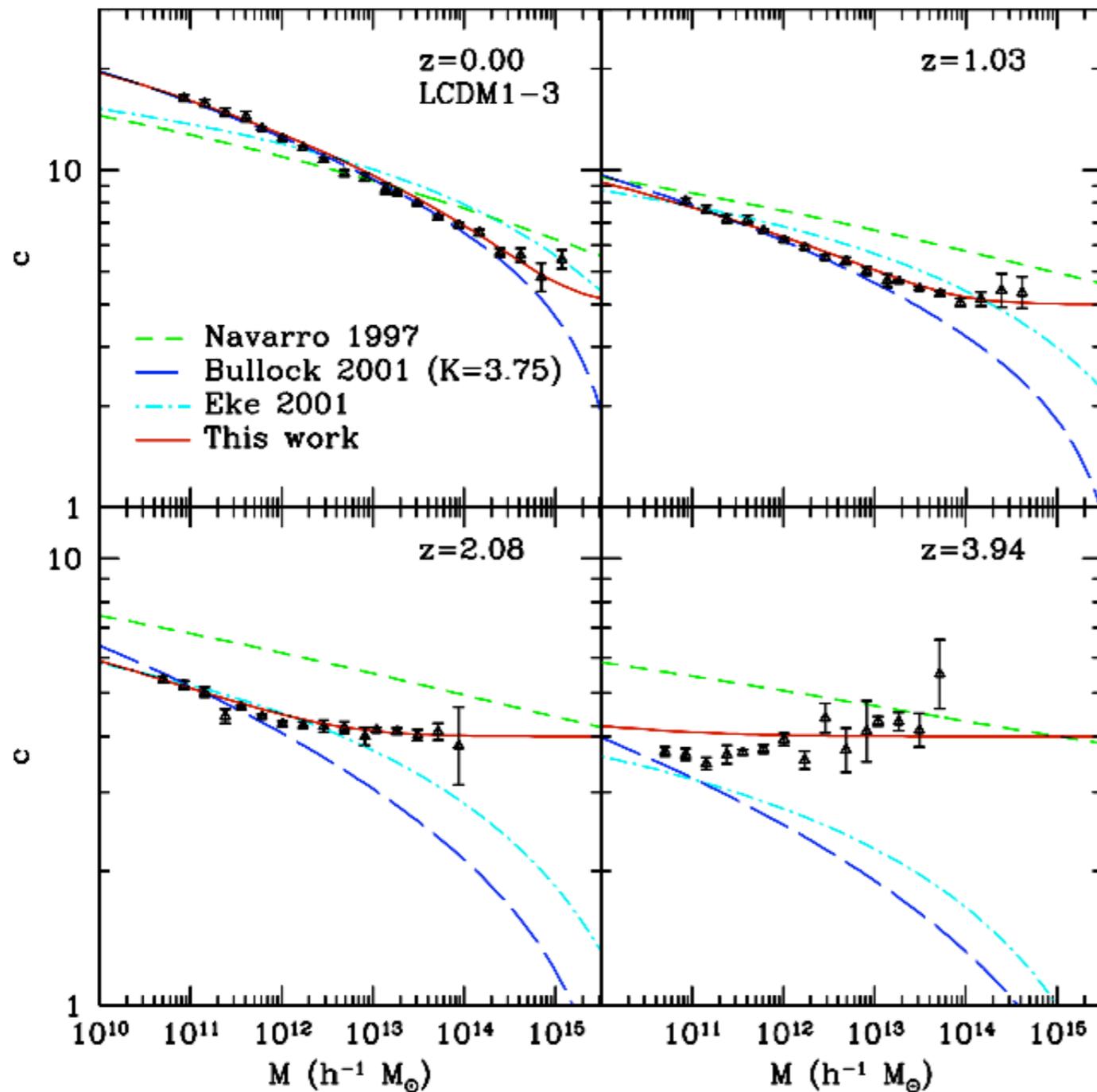
$$c(M_{\text{sub}}) = 12 \left(\frac{M_{\text{sub}}}{10^{12} h^{-1} M_{\odot}} \right)^{-0.12}$$

**Concentration at $z=0$
for $\sigma_8=0.82$**

Halo Concentration: flattening at high redshifts

First noticed by Wechsler et al 2003: $C_{\text{vir,min}} = 4.1$

Also: Zhao et al 2003, Zhao et al 2009

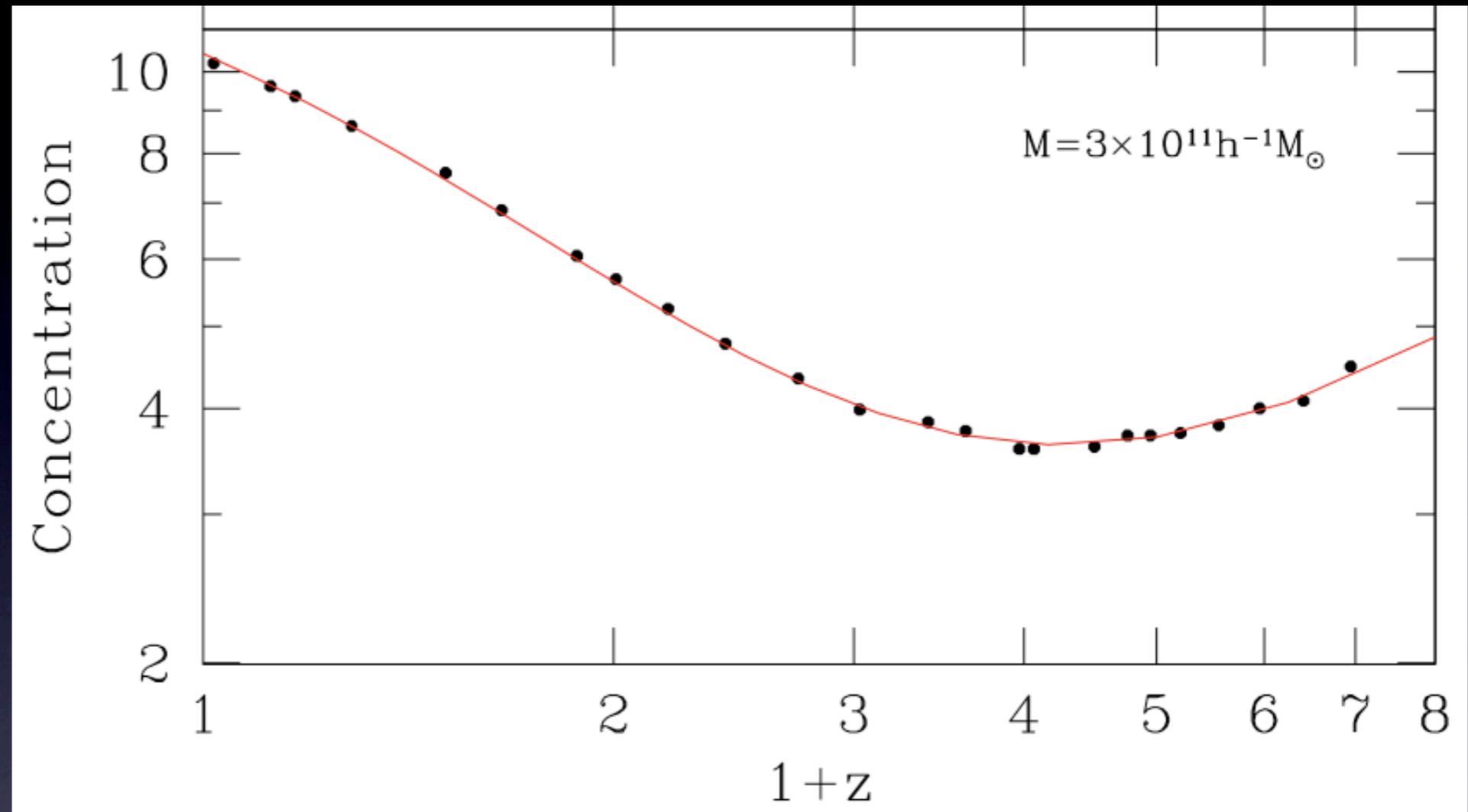


Flattening in $C(M)$ separates two regimes:

- fast growth of mass with nearly constant concentration
- slow growth accretion, increasing concentration

Halo Concentration: evolution with redshift

After initial decline the concentration flattens and then starts to increase again

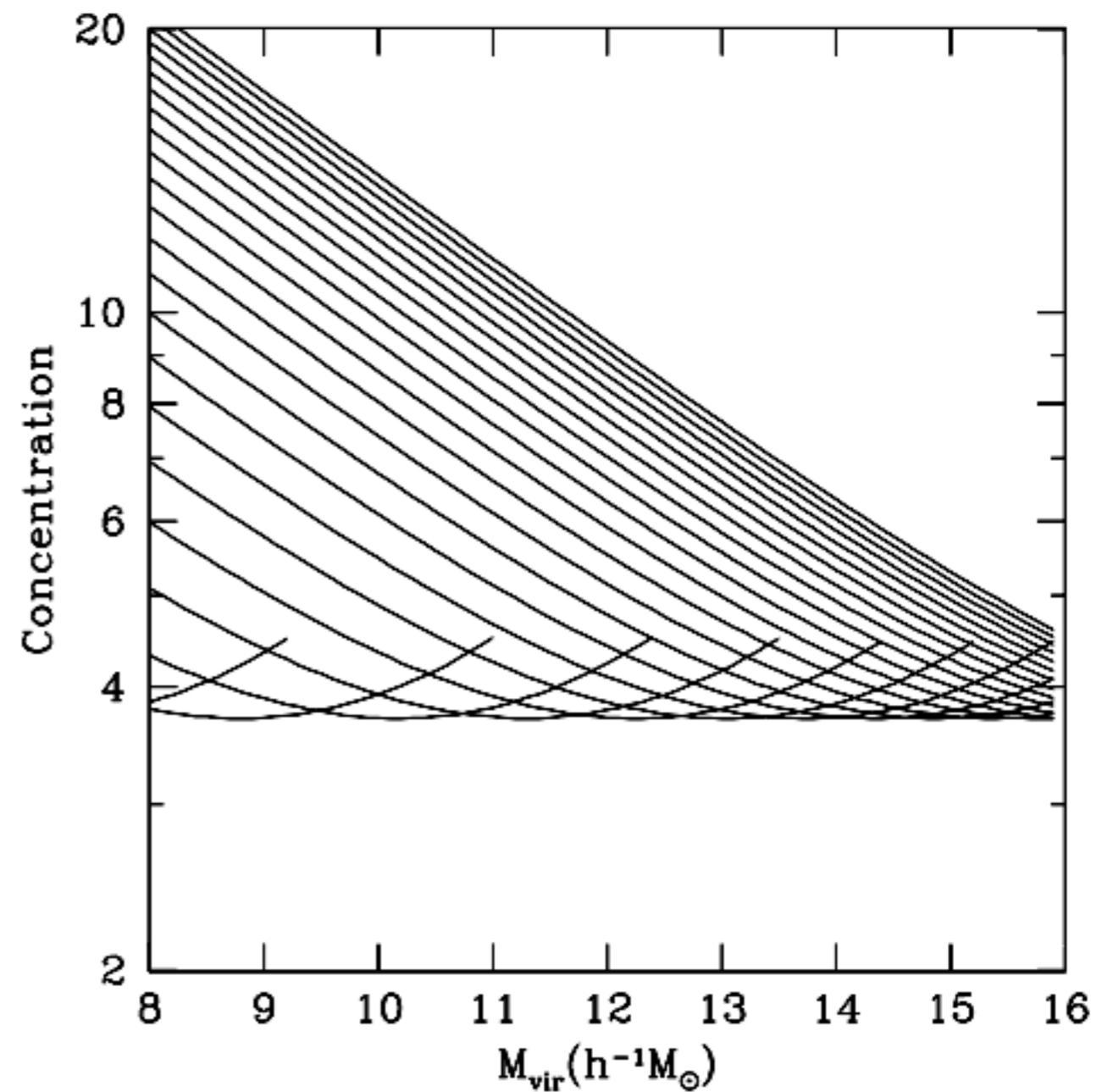
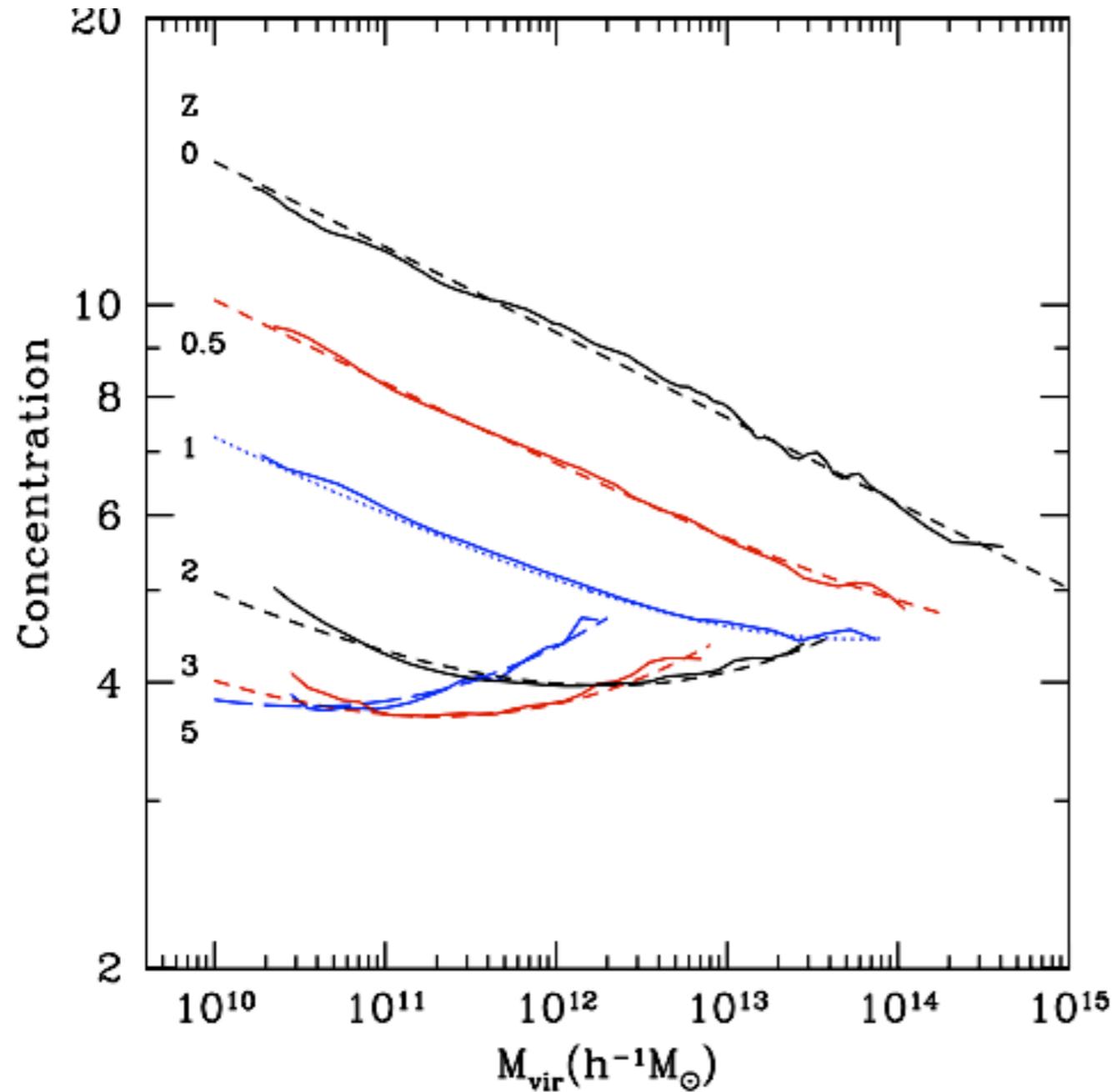


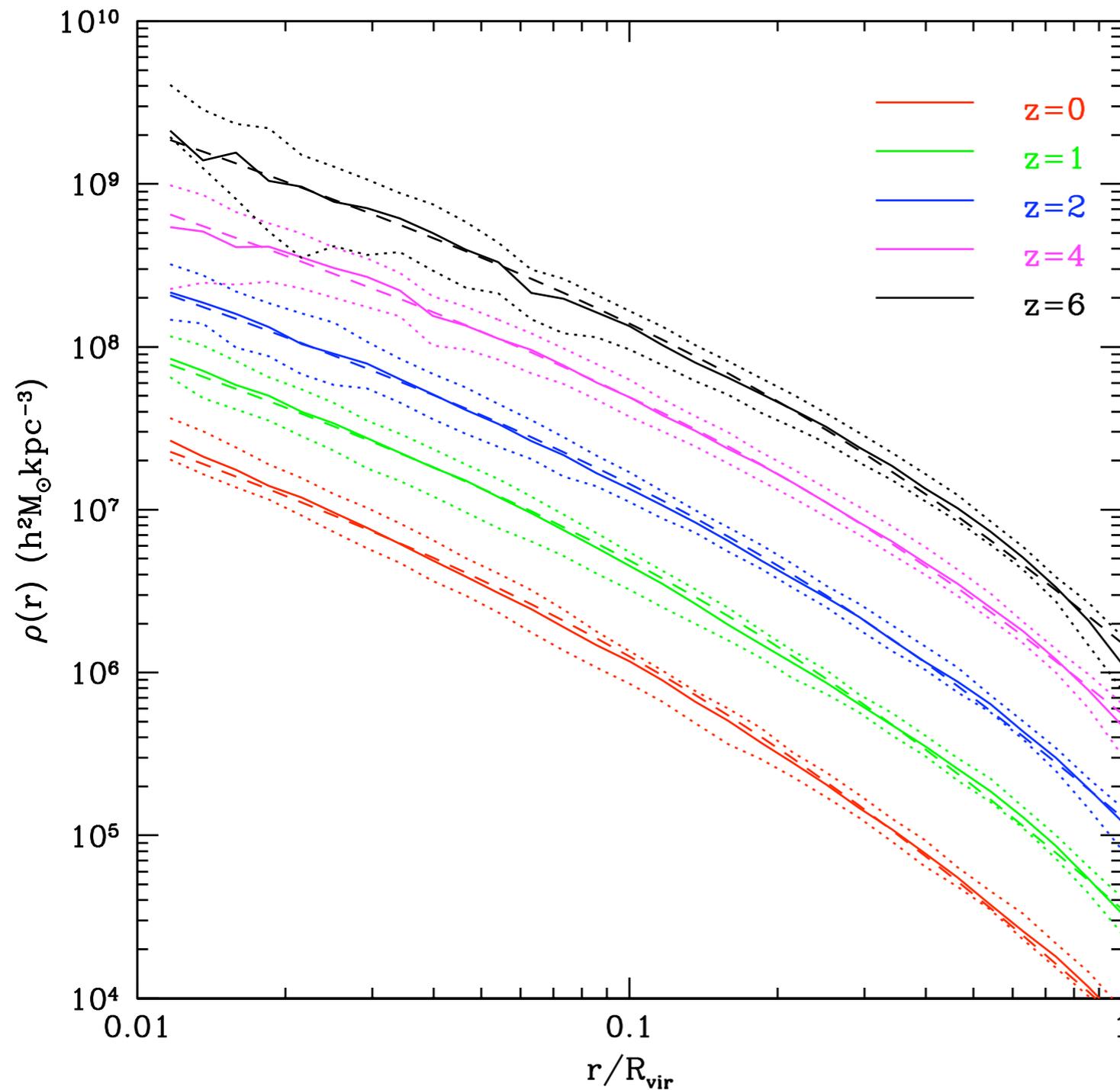
$$c(M_{\text{vir}}, z) = c_0(M_{\text{vir}}) \left[\delta^{3/2}(z) + \kappa(\delta^{-1}(z) - 1) \right], \quad (14)$$

here $\delta(z)$ is the linear growth factor of fluctuations normalized to be $\delta(0) = 1$ and κ is a free parameter

$$c(M_{\text{vir}}, z) = 9.2 \delta^{1.3}(z) \left(\frac{M_{\text{vir}}}{10^{12} h^{-1} M_{\odot}} \right)^{-0.09} \\ \times \left[1 + 0.013 \left(\frac{M_{\text{vir}}}{10^{12} h^{-1} M_{\odot}} \delta(z)^{-\frac{1.3}{0.09}} \right)^{0.25} \right]$$

Halo Concentration: medians depend only on the amplitude of perturbations and mass: no explicit dependance on accretion history





Density Profiles of rare peaks: they look normal though many of them are mergers and fast accretors

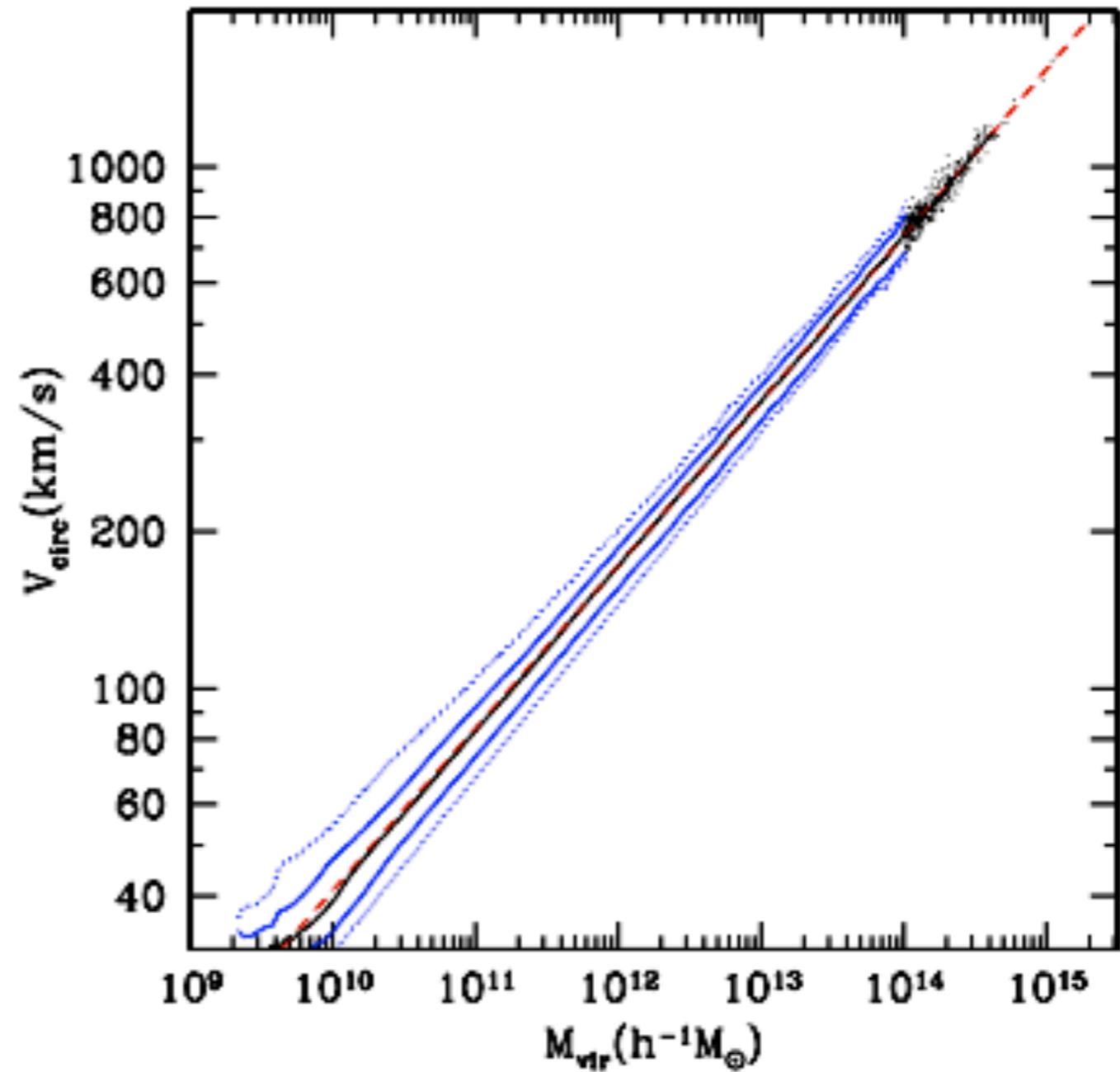
$z=0$: $M=2e14$ ($s=0.7866074$); $c=5.42$
 $z=1$: $M=5e13$ ($s=0.6688836$); $c=4.30$
 $z=2$: $M=2e13$ ($s=0.5335957$); $c=3.48$
 $z=4$: $M=2e12$ ($s=0.4940273$); $c=2.79$
 $z=6$: $M=5e11$ ($s=0.4215051$); $c=2.90$

Courtesy of A.Cuesta

Halo Concentration: different ways

$$V_{max} - M_{vir}$$

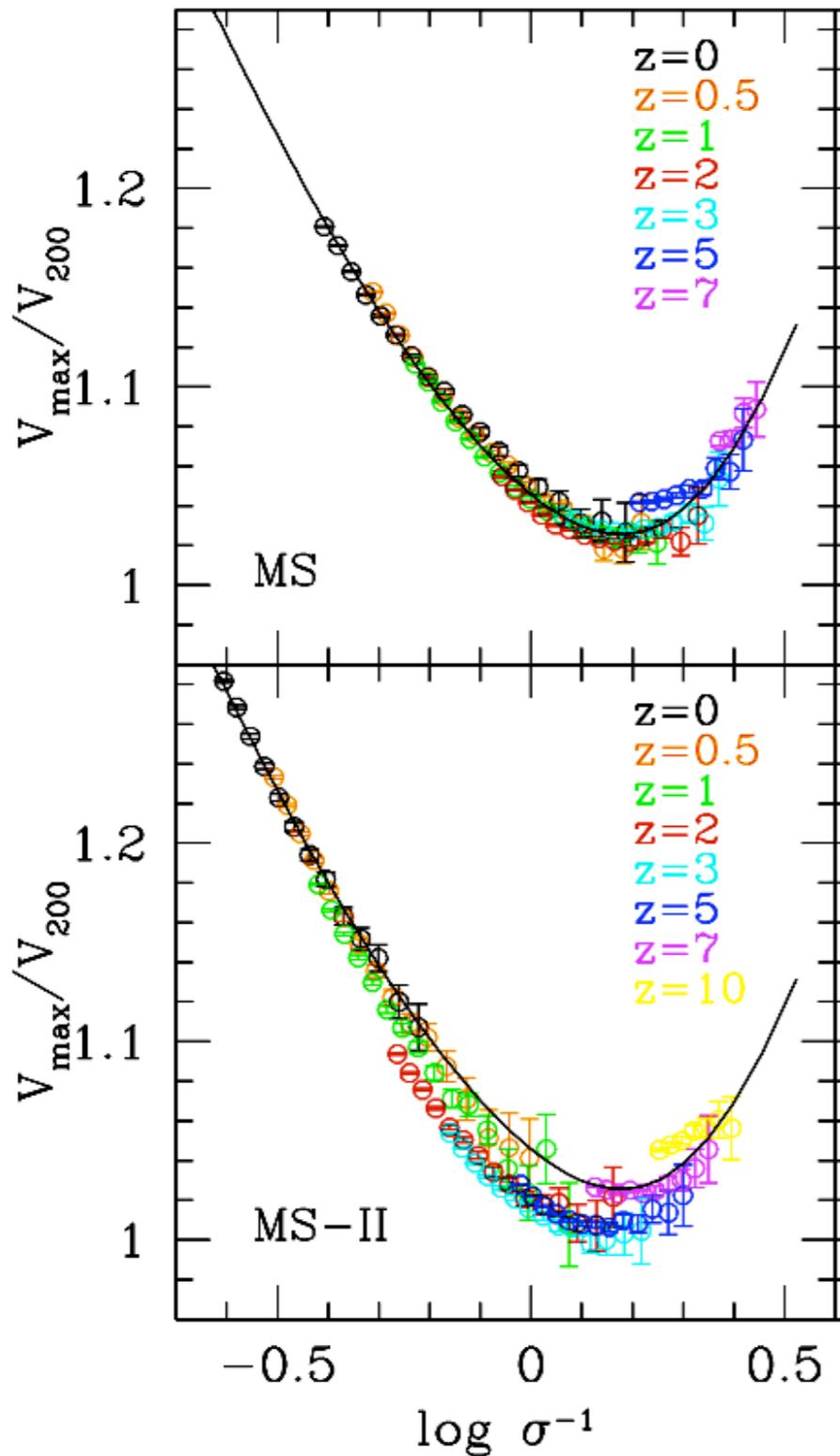
$$V_{max}/V_{200}$$



Mass inside R_s as function of R_s

Halo Concentration: evolution with time

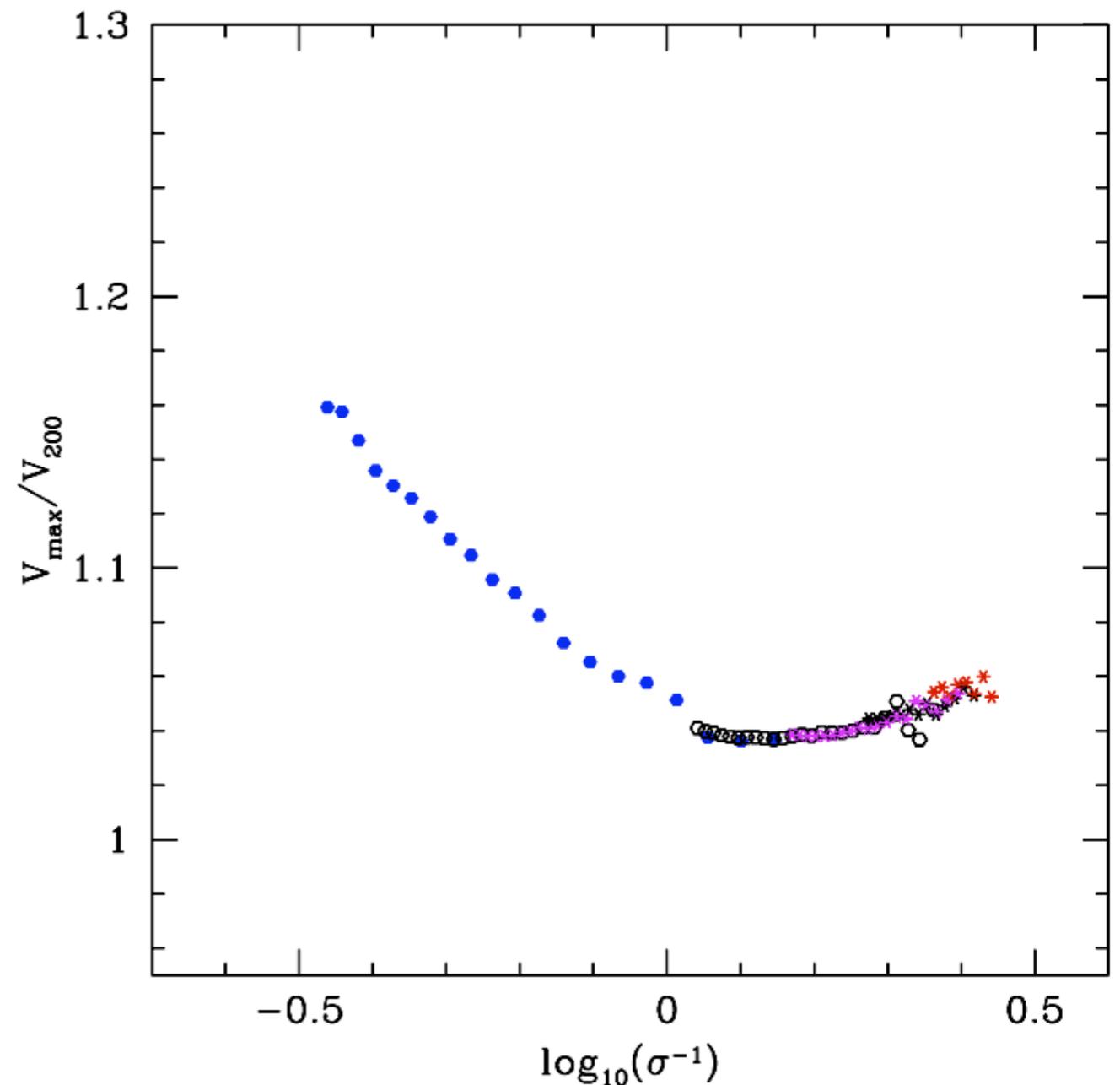
Gadget: Millennium runs



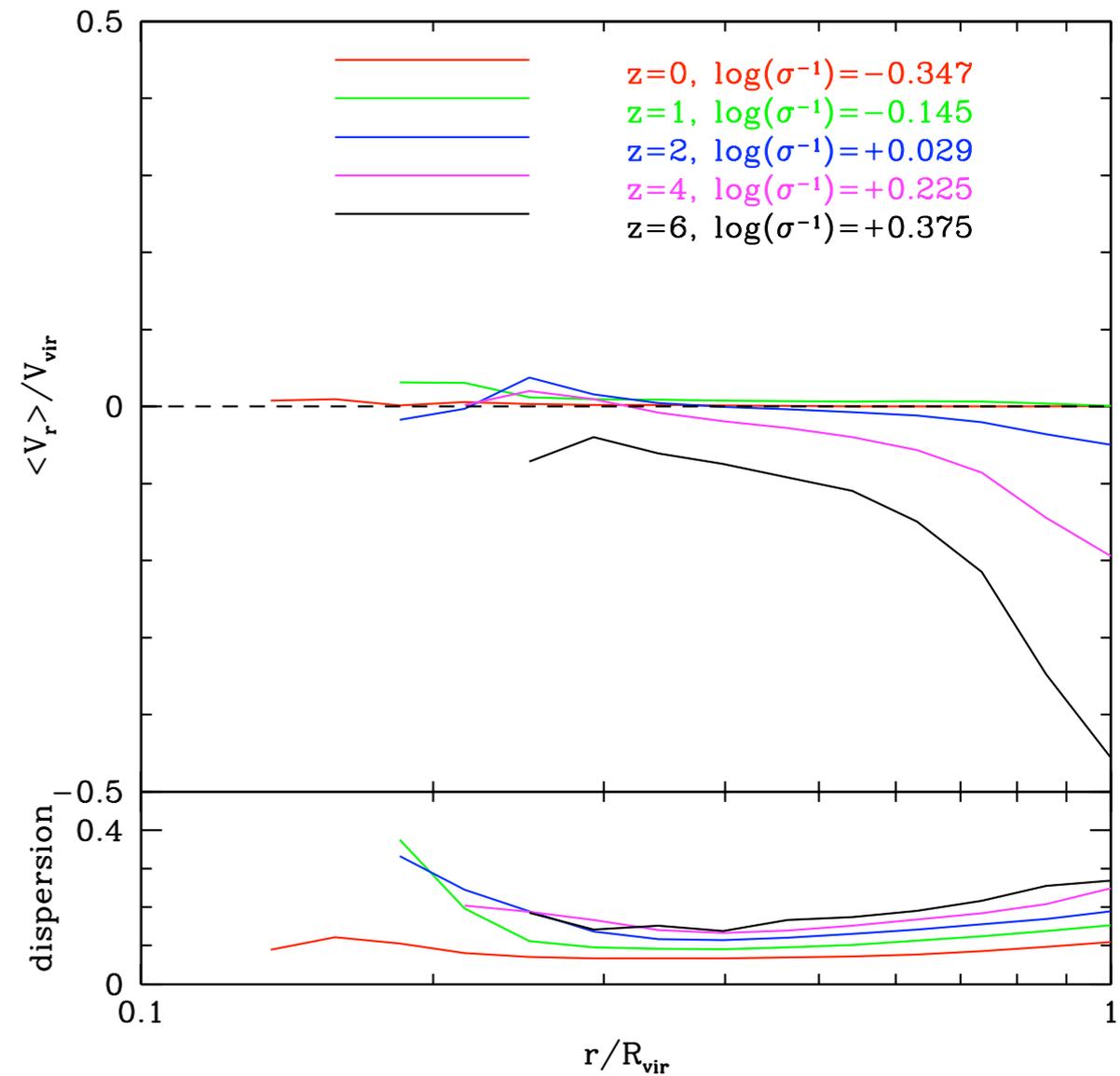
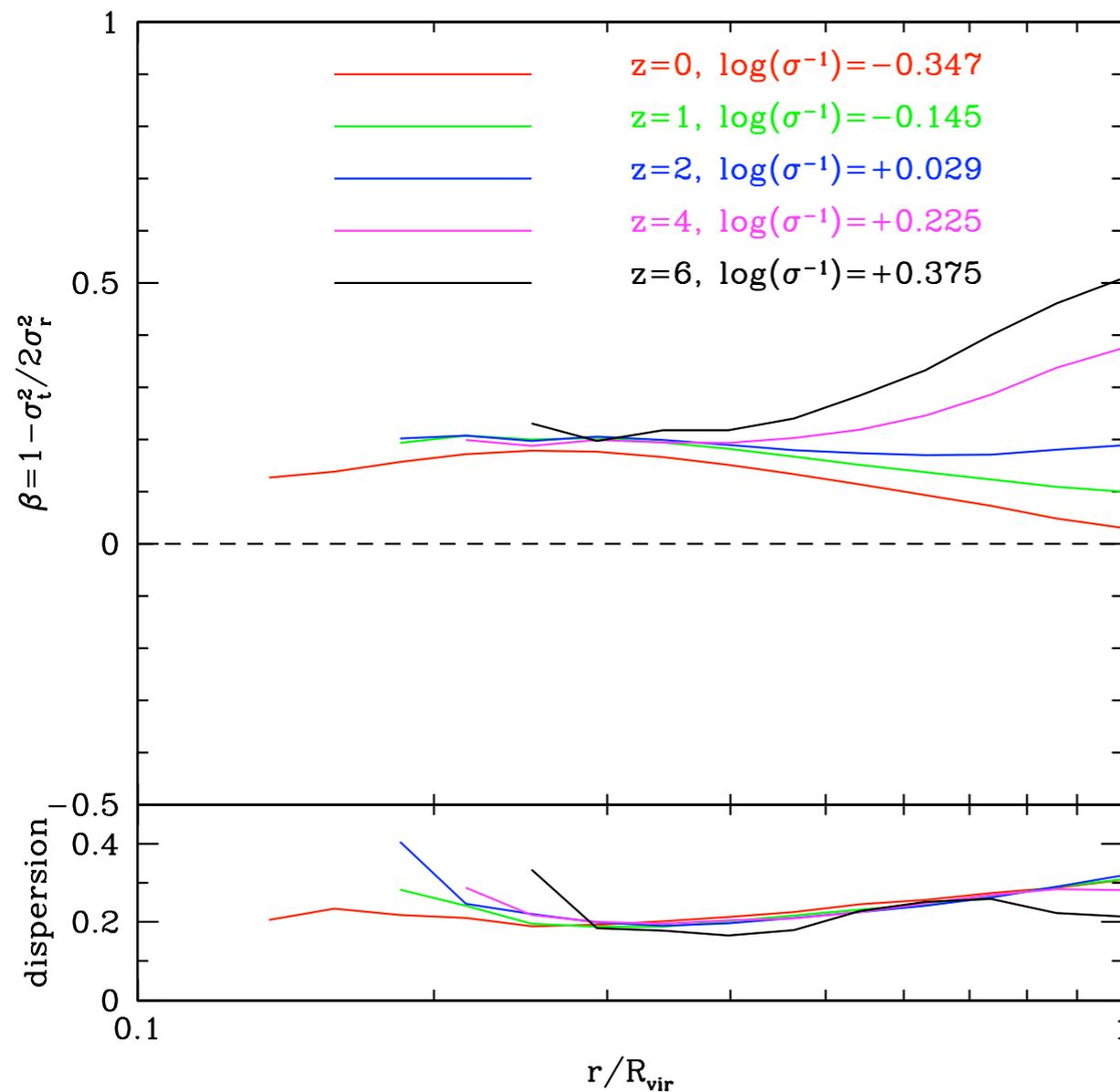
Upturn is in all the simulations. Average concentration depends only on mass.

$\sigma(M)$ = amplitude of fluctuations at given mass

ART: Bolshoi (250Mpch), MultiDark (1000Mpc, 8G particles)



3 stages of halo formation



*Halos with $M_{\text{vir}} = 5 \times 10^{11} M_{\text{sun}}$ at different redshifts:
at $z=6$: large infall velocities even inside virial radius and very radial orbits*

Halo Concentration: 3 stages

- (a) *The main driving force of halo evolution is NOT the major mergers: they happen when they should happen*
- (b) *The main effect is the halo mass relative to the typical mass at given redshift: M/M_**

-  Very rare peaks: radial infall results in a high concentration. Another way looking at it: it builds dense center of halos
-  Fast accretion with less radial velocities. At the end of the stage we have the core build. Gives low concentration.
-  Slow accretion builds outer regions of halos. Velocity anisotropy declines

Halo Concentration: different perspectives

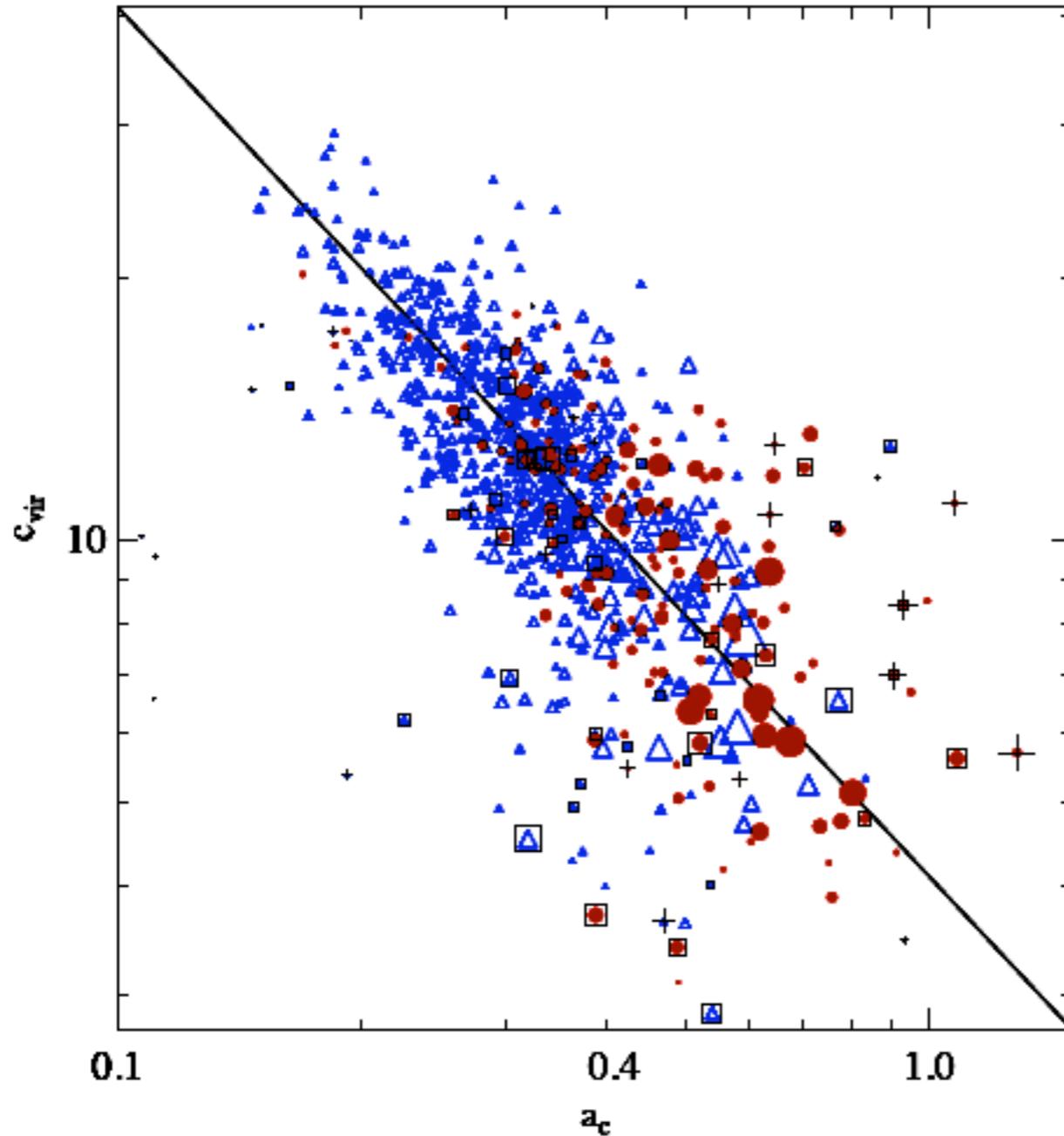


Figure 6 shows the relation between concentration and a_c for halos at $z = 0$. The concentration of a halo is strongly correlated with its characteristic formation time, and a good fit is obtained with the inverse relation:

$$c_{\text{vir}} = c_1/a_c, \quad (6)$$

where $c_1 = 4.1$ is the typical concentration of halos form-

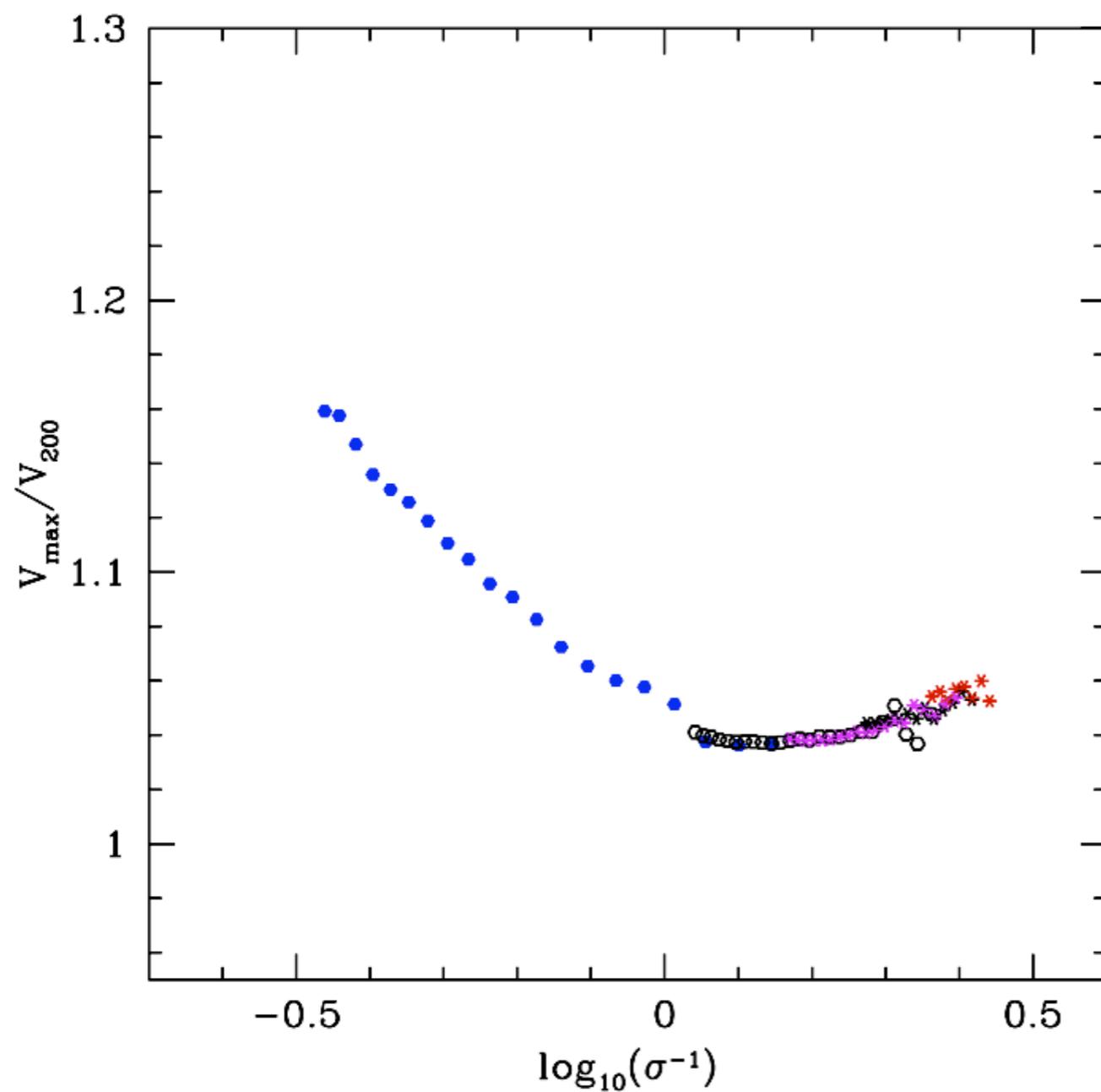
Wechsler et al 2002

Time of accretion a_c for halos more massive than $10^{12}M_{\text{sun}}$ at $z=0$

Halo Concentration: *different perspectives*

Zhao et al 2009, Klypin et al 2010, Prada et al 2010

Evolution of halo concentration is mostly defined by M/M_*

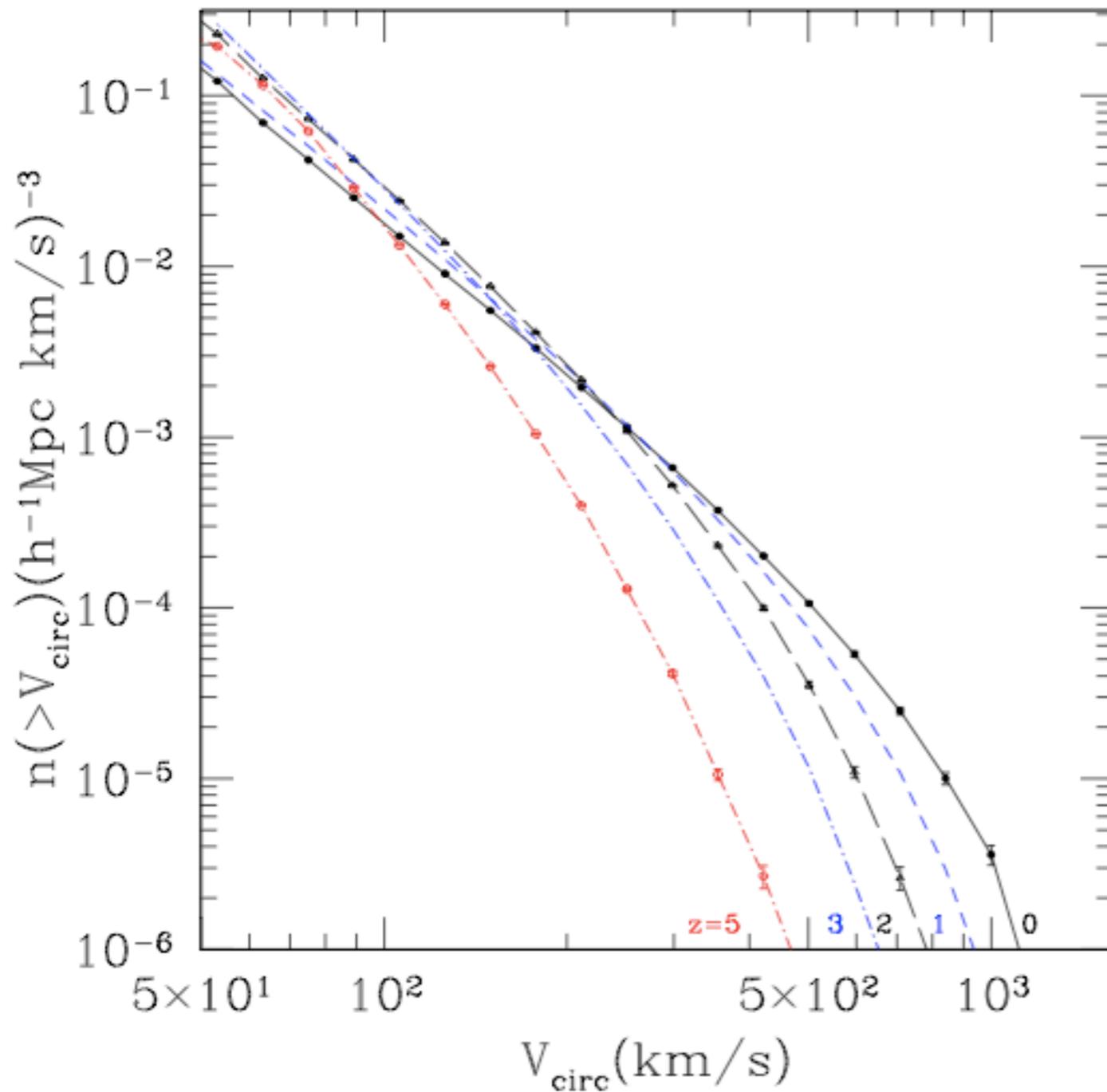


Chapter II: Satellites

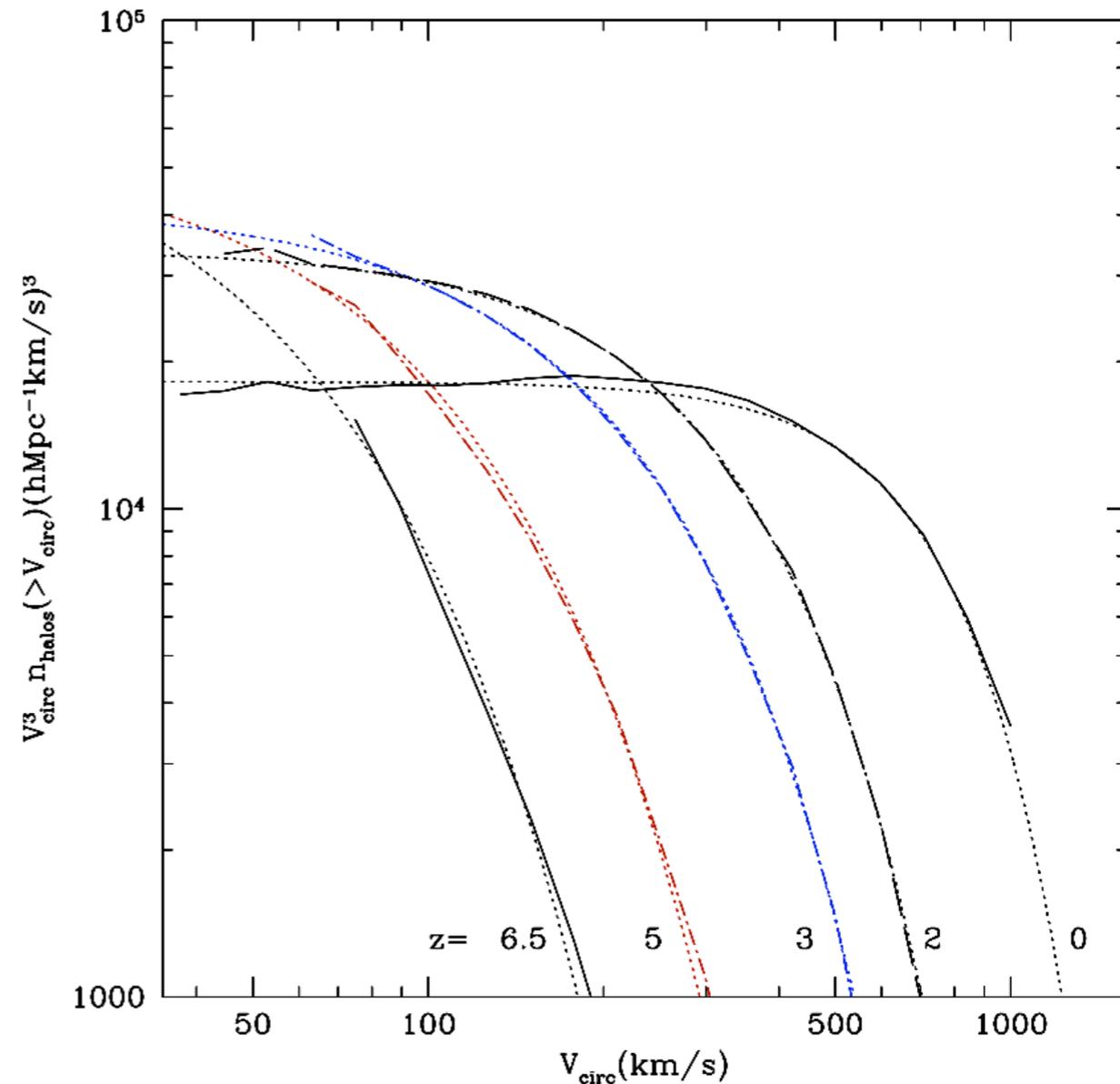
how and where they live

$$V_{\text{circ}} = \sqrt{\frac{GM(<r)}{r}} \Big|_{\text{max}}$$

Main property of halos is circular velocity



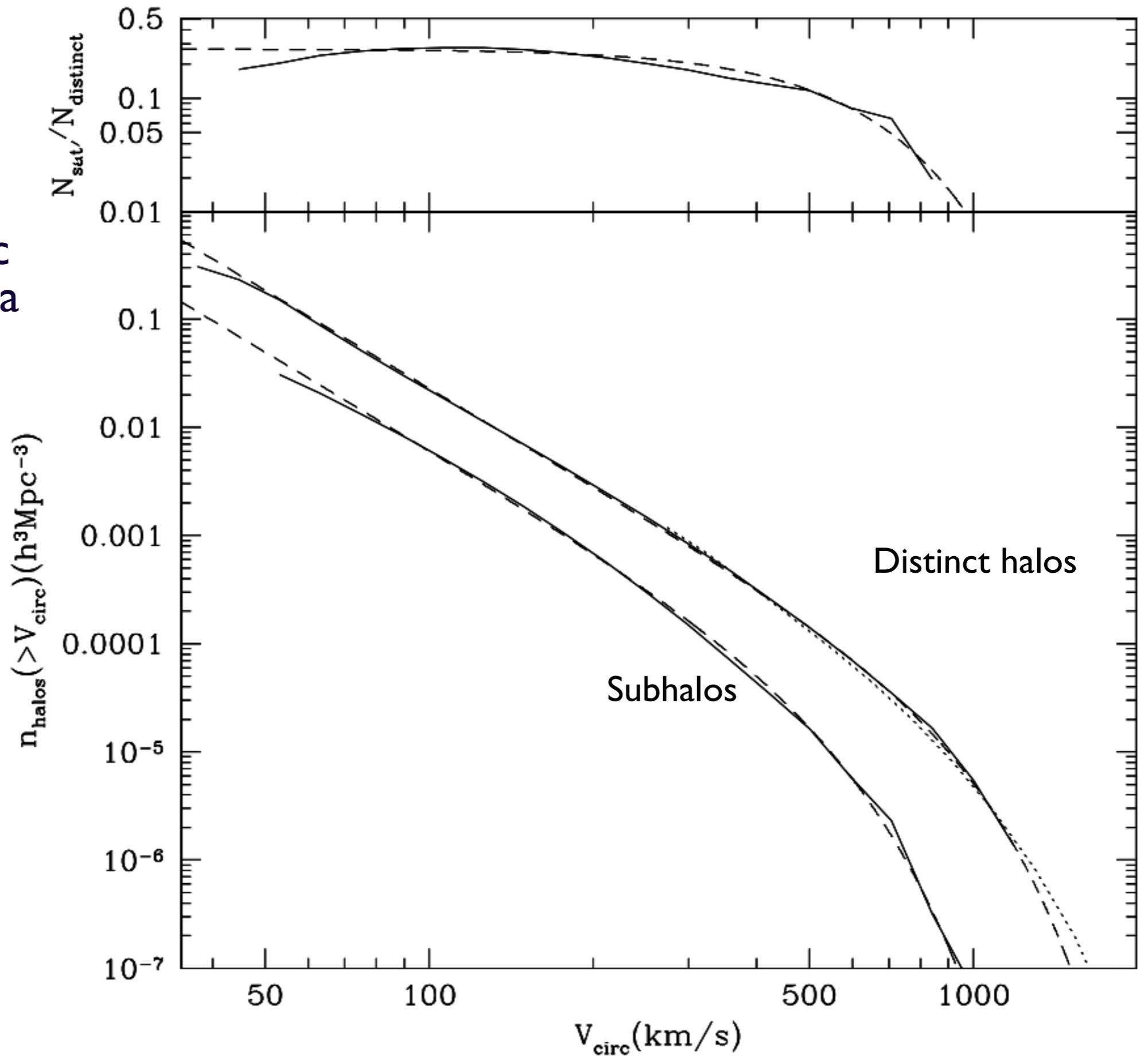
Accurate predictions for Velocity function of distinct halos

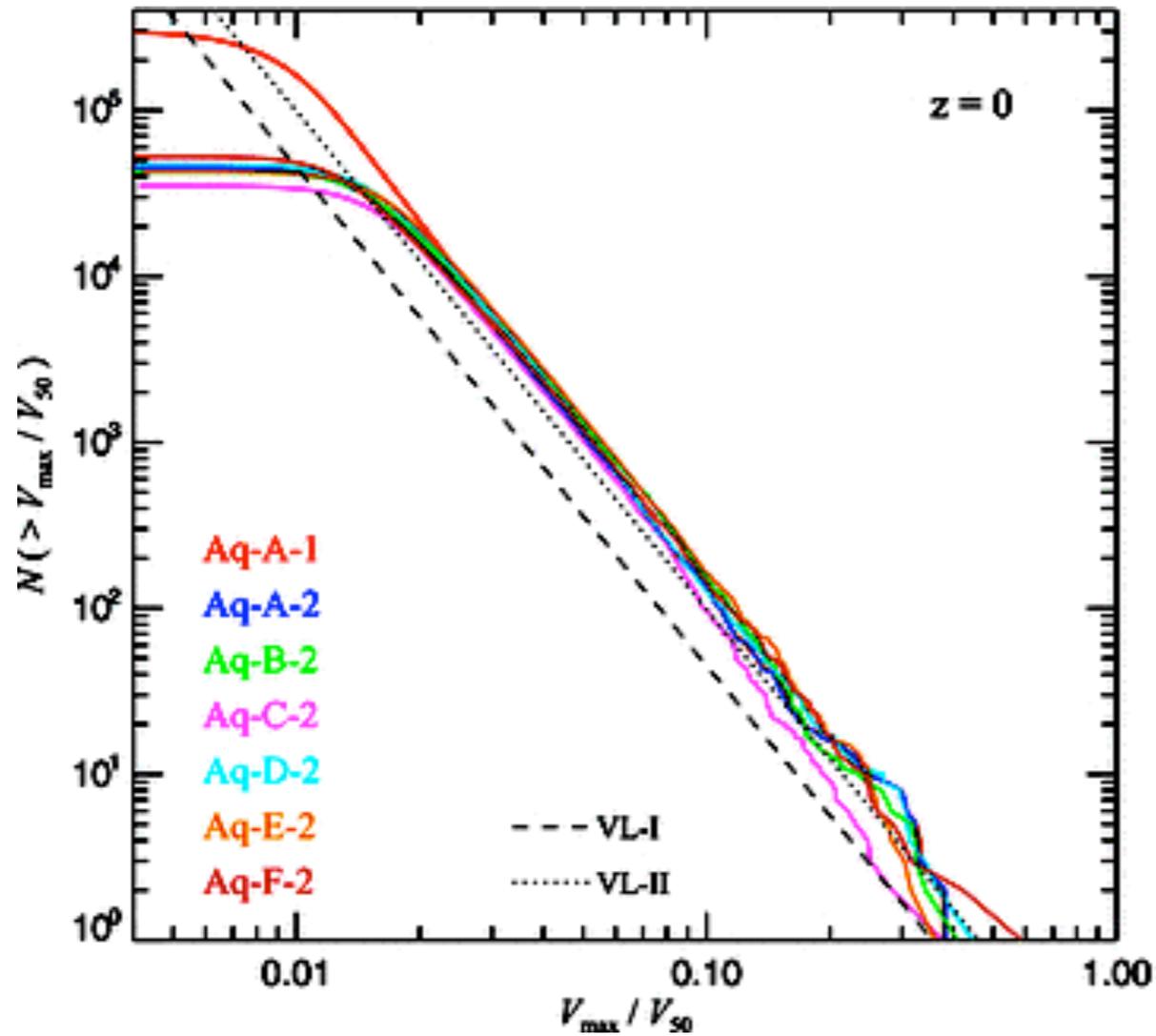


Velocity Functions

From Magellanic Clouds to Coma Cluster

250Mpc/h
8G particles
1kpc resolution





Aquarius simulation. Springel et al 2008. WMAP-I

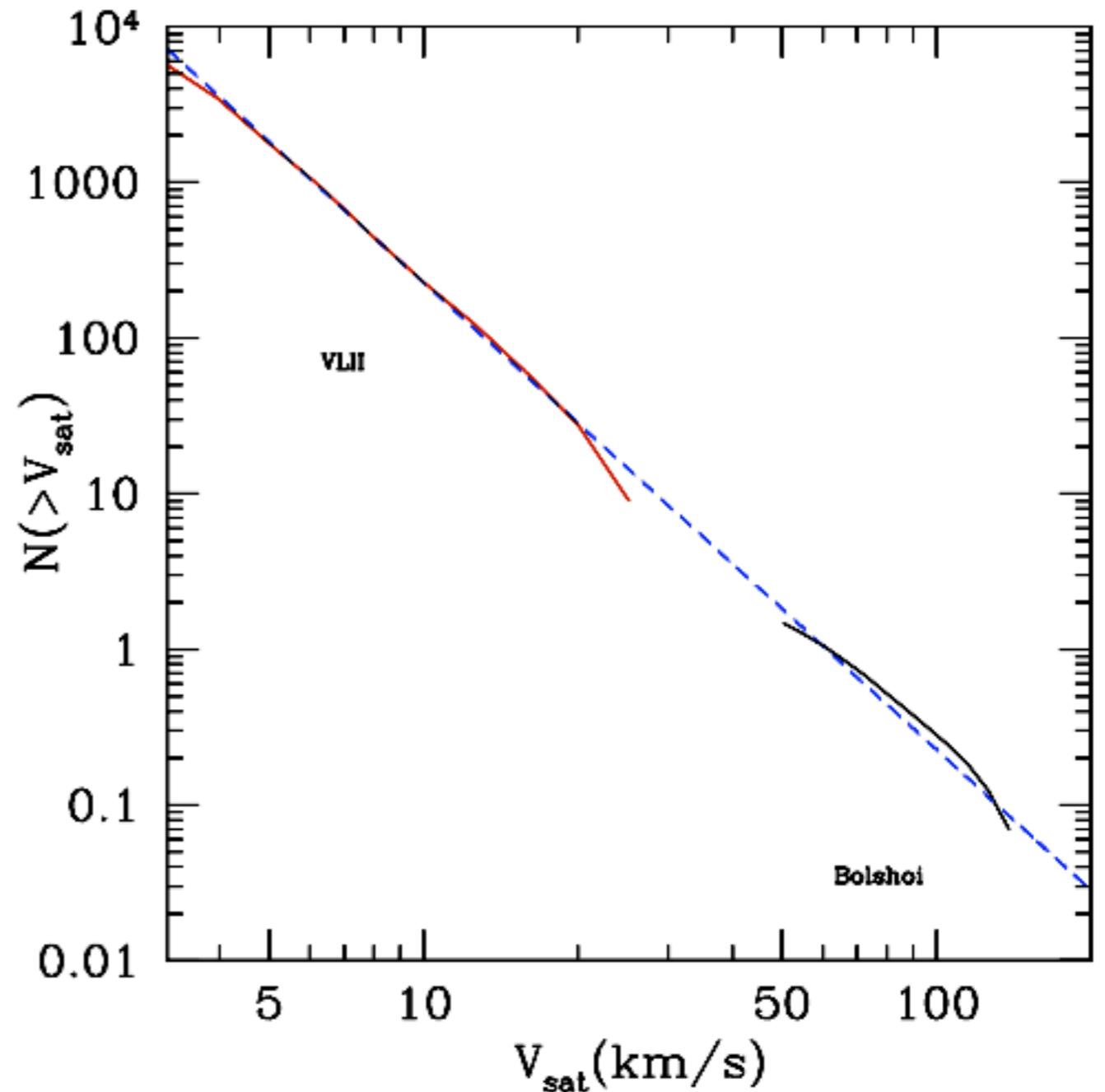


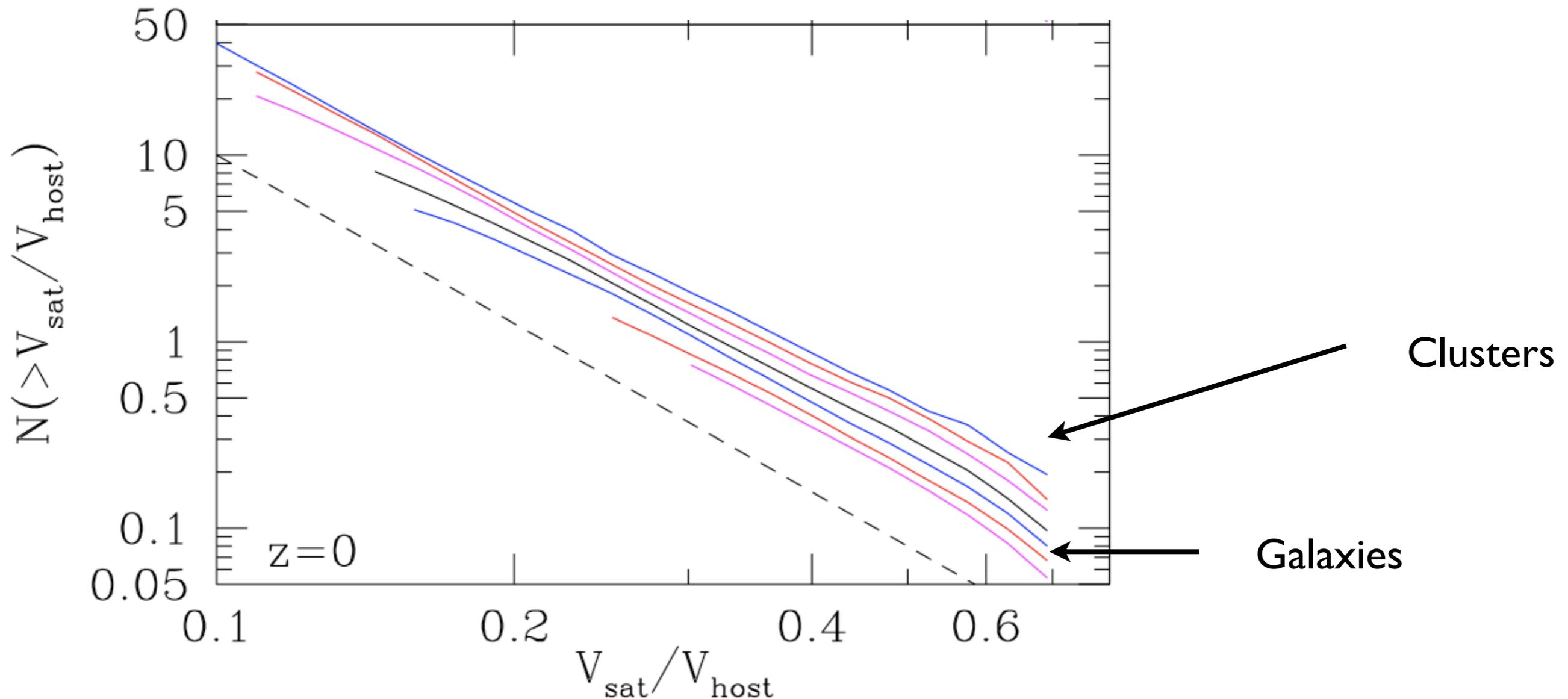
Fig. 18.— Comparison of satellite velocity functions in Via Lactea II and Bolshoi simulations for halos with $V_{\text{circ}} = 200$ kms/s and $M_{\text{vir}} \approx 1.3 \times 10^{12} h^{-1} M_{\odot}$. The dashed line is a power law with the slope -3 , which provides excellent fit to

Bolshoi and ViaLactea II. Klypin et al 2010. WMAP-7

$$n(> V) = AV^{-3}$$

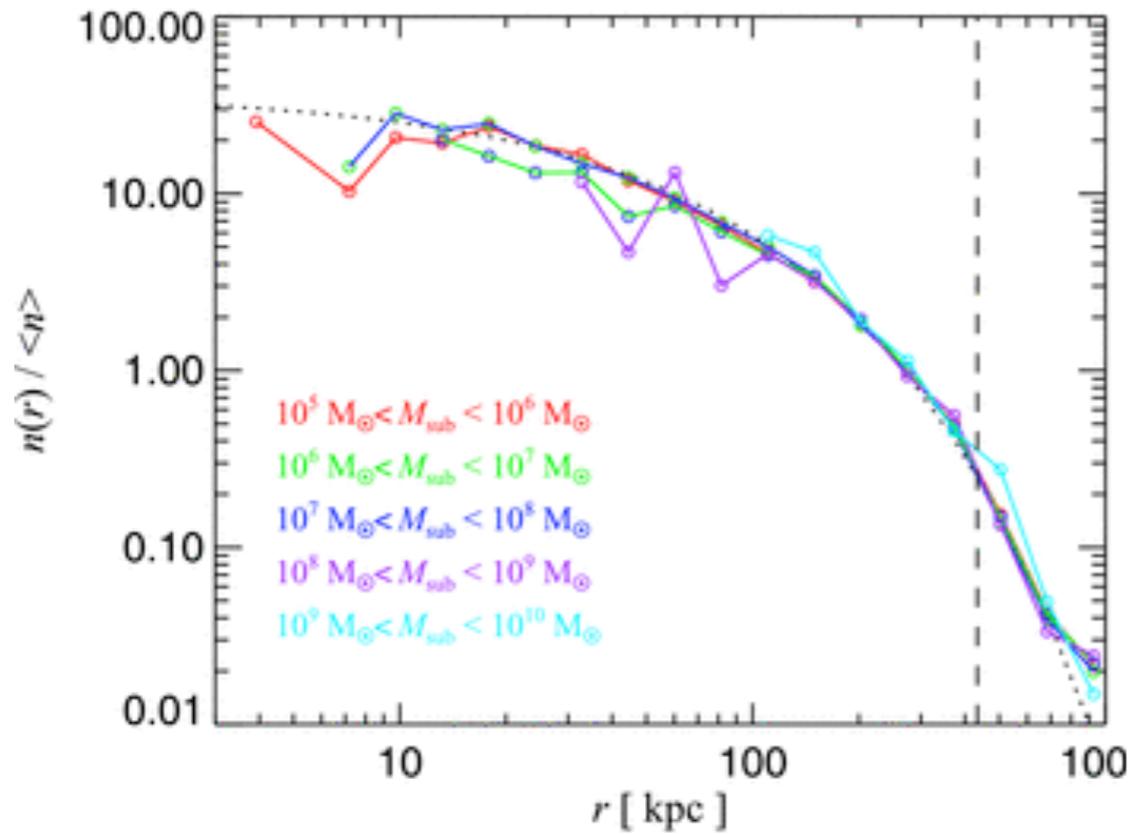
Abundance of satellites

$$N(> x) = 1.7 \times 10^{-3} V_{\text{host}}^{1/2} x^{-3},$$
$$x \equiv V_{\text{sub}}/V_{\text{host}}, x < 0.7,$$



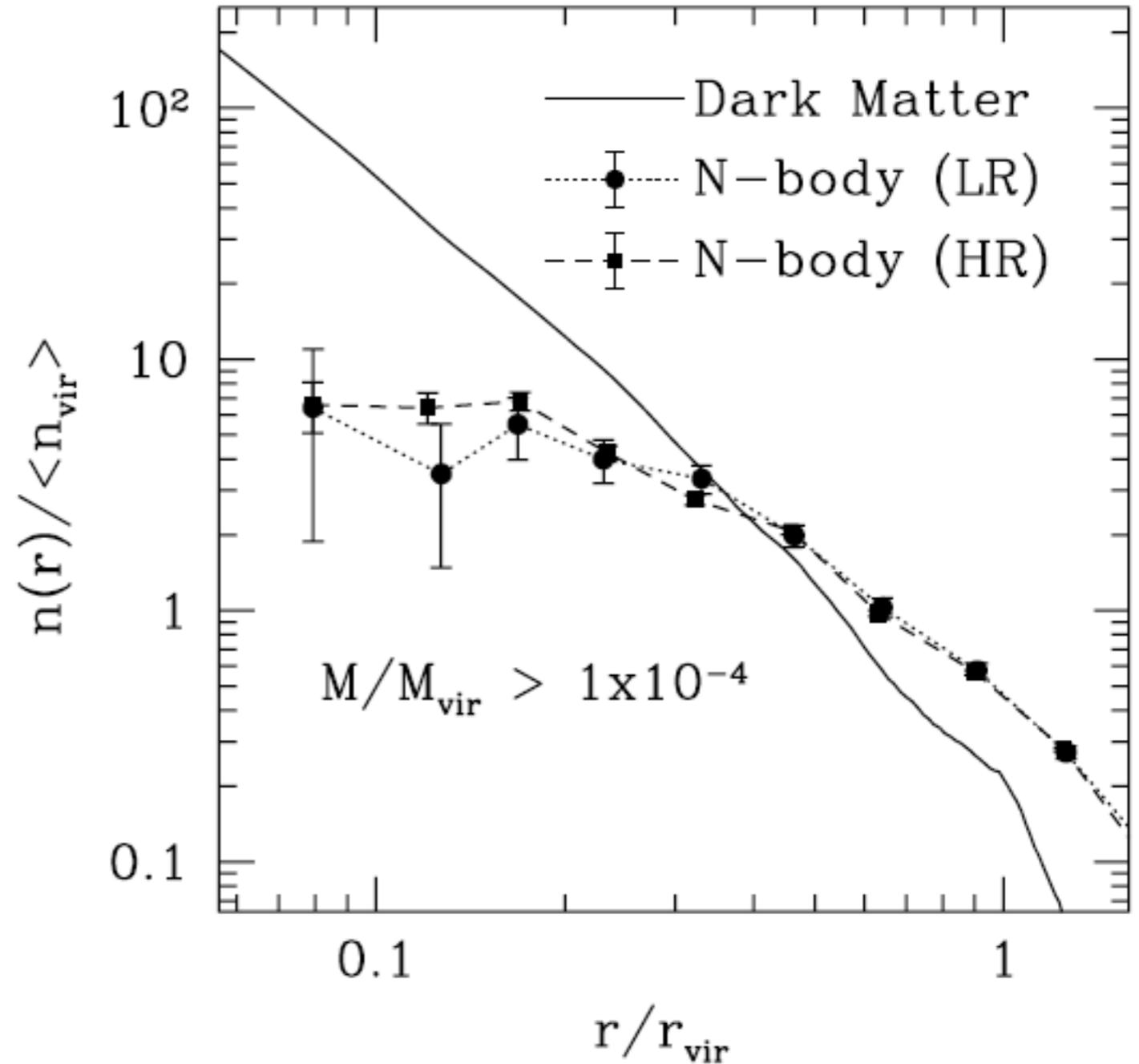
Number of satellites increases with the mass of parent halo

Number-density of satellites



Aquarius simulation. Springel et al 2008.
WMAP-I

Subhalos are selected by mass. This gives an impression of a very large core



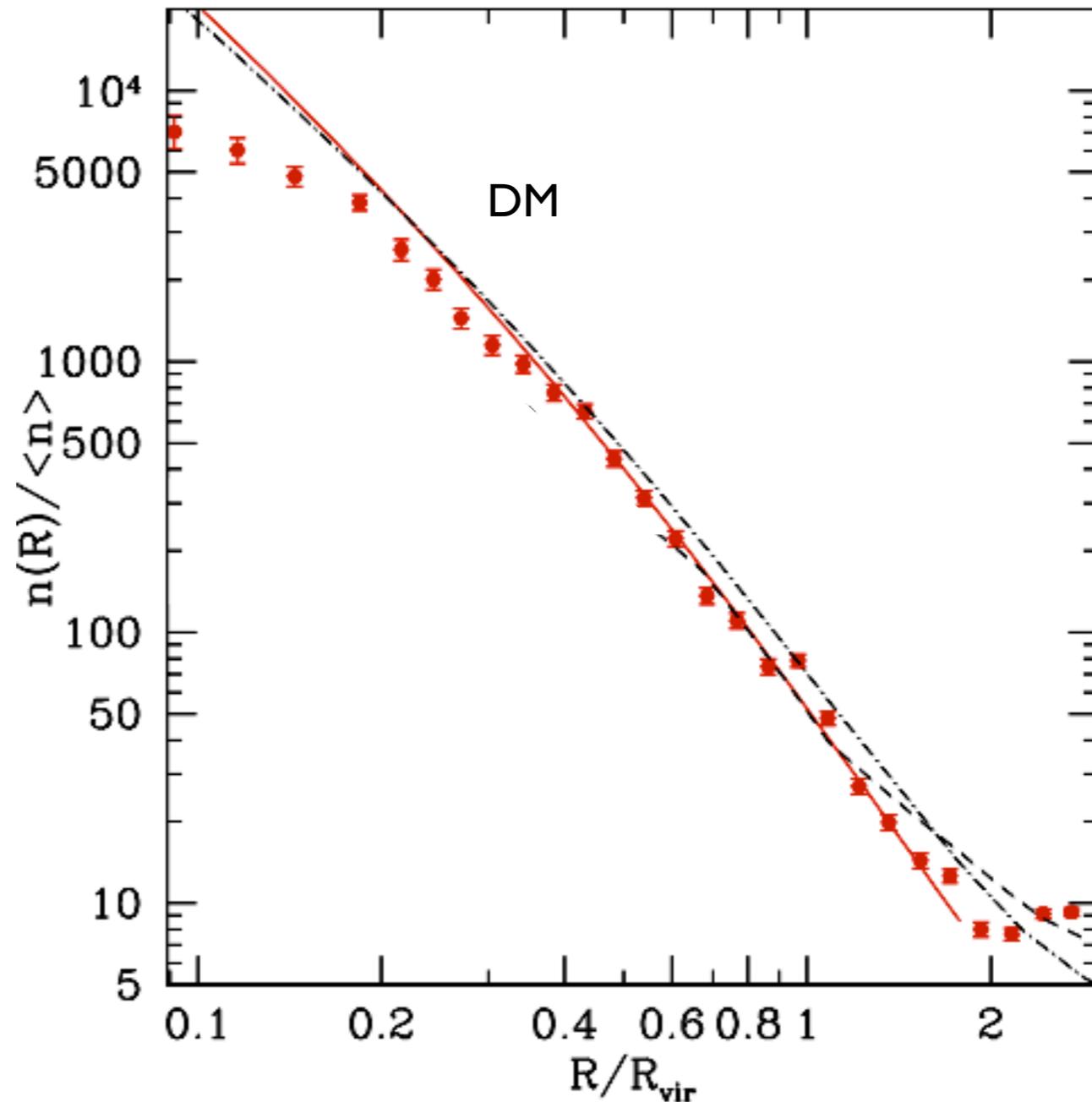
Nagai & Kravtsov 2005

Symbols are satellites in Via Lactea II simulation (1 G particle, one halo with $V_{\text{circ}} = 200 \text{ km/s}$) normalized using Bolshoi

Curves are $n(r)$ DM density profile

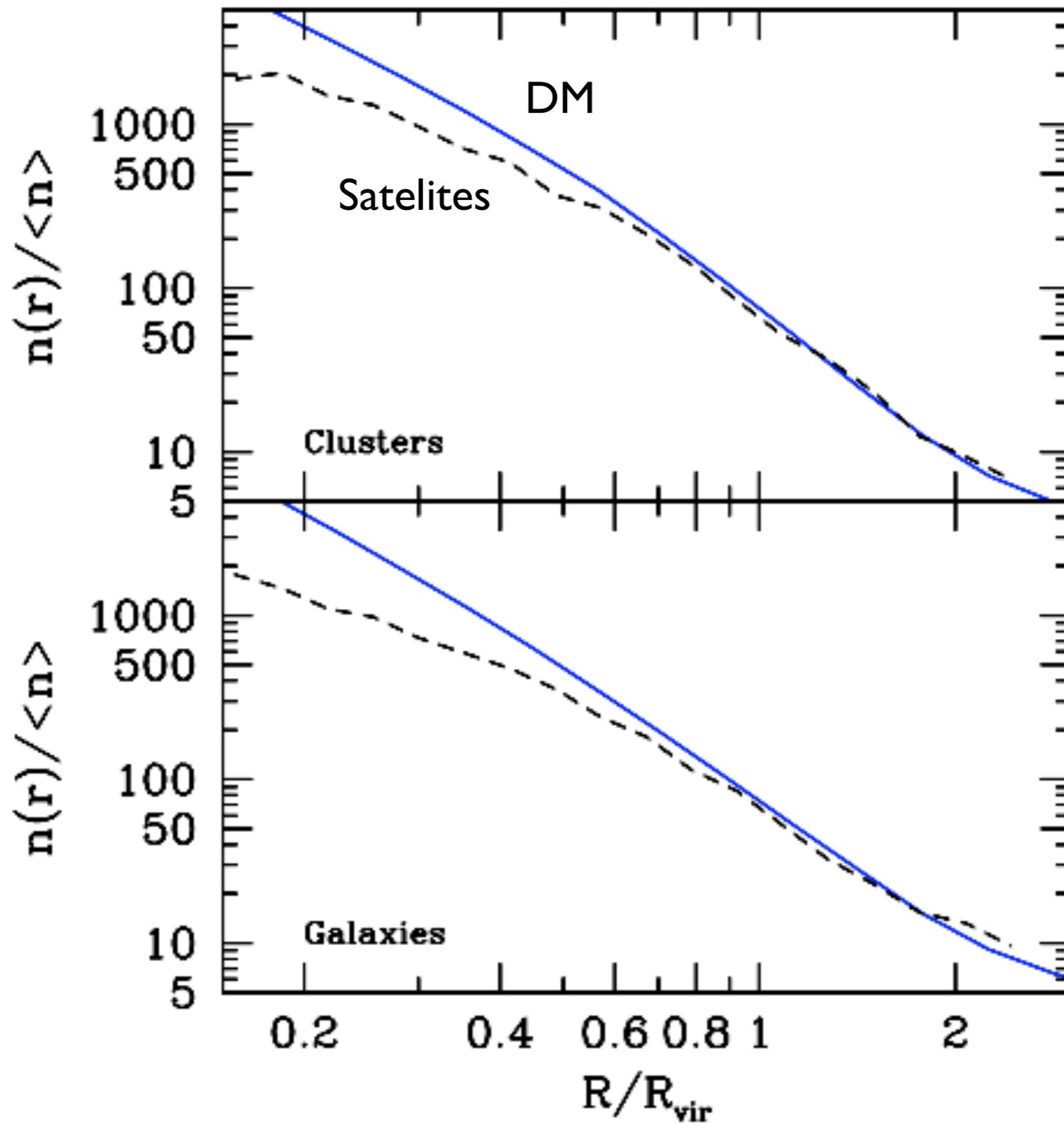
Dash - satellites in Bolshoi

Satellites tightly follow DM at $r > 0.2R_{\text{vir}}$: they are NOT ‘flatter’ distributed in the outer regions of halos.



Bolshoi and ViaLactea II. Klypin et al 2010. WMAP-7
Subhalos are selected by circular velocity.
Satellites follow Dark matter for $R = 0.2-2R_{\text{vir}}$

Number-density of satellites

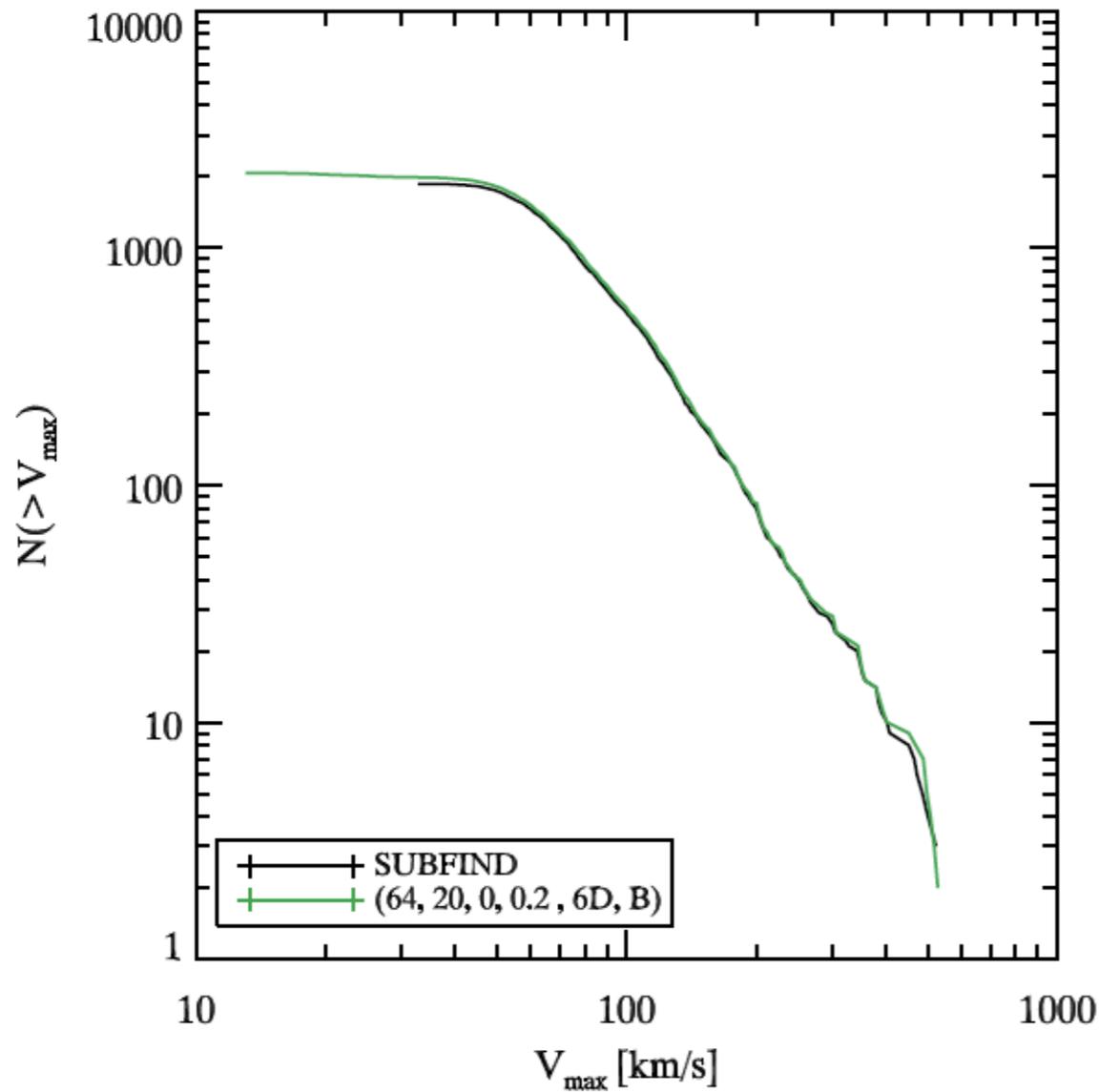


Small anti-bias in the central regions. Very little in the outer parts

Bolshoi

How good are masses of subhalos?

6D halo finder vs Subfind
the same halos and the same circular velocities



6D halo finder vs Subfind
masses are 2-3 times different

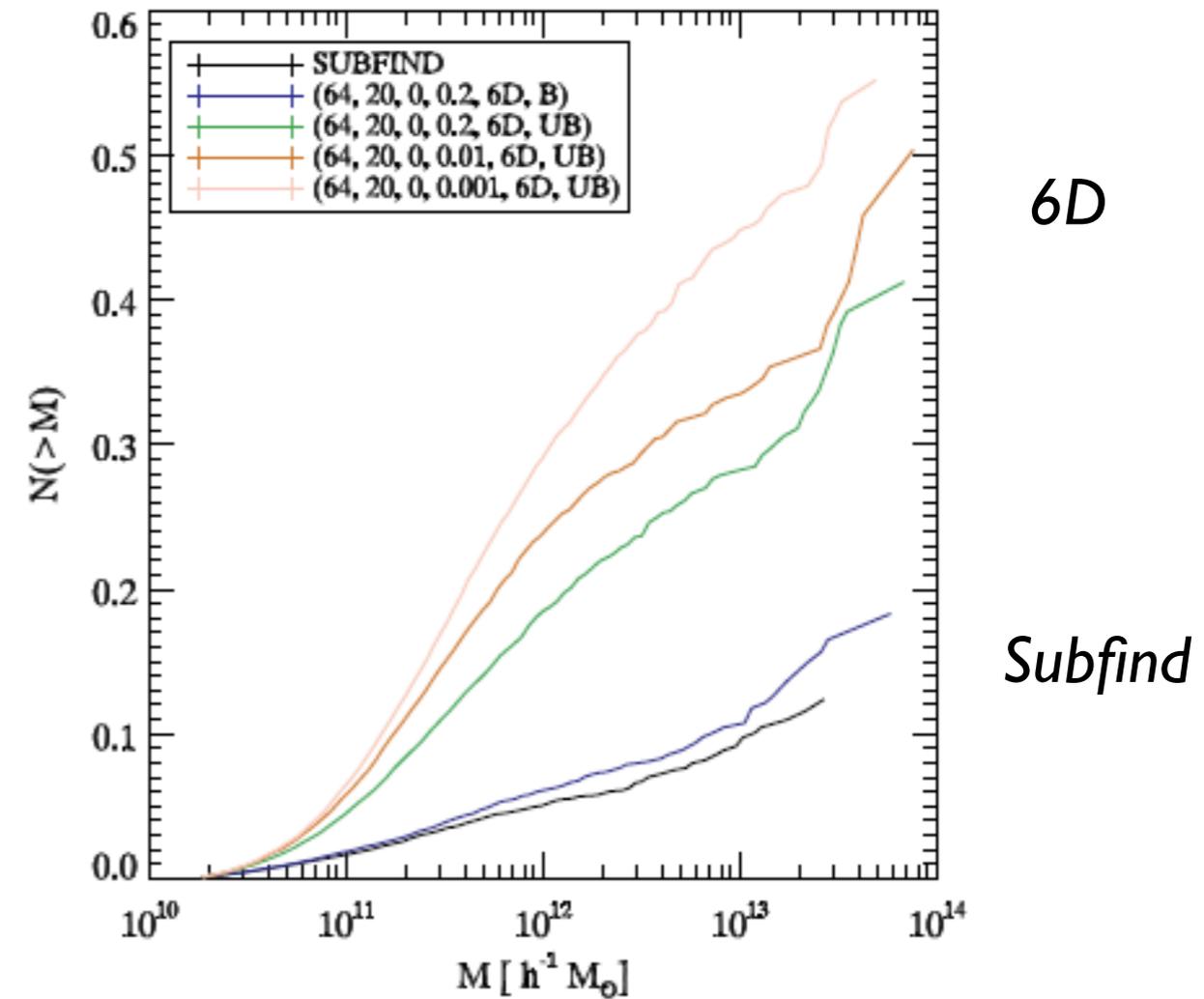


Figure 18. Cumulative mass in substructures found by SUBFIND, bound HSF method, and HSF with different choices of the connectivity parameter α .

Chapter III: Conclusions

- **Three stages for halo formation**
- **Mass accretion history is not the only (or even main) component which defines halo concentration: dynamics is different for different stages.**
- **There is no 'core' in the satellites profile**