

# Core Collapse & Neutron Star Mergers

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**Caltech**

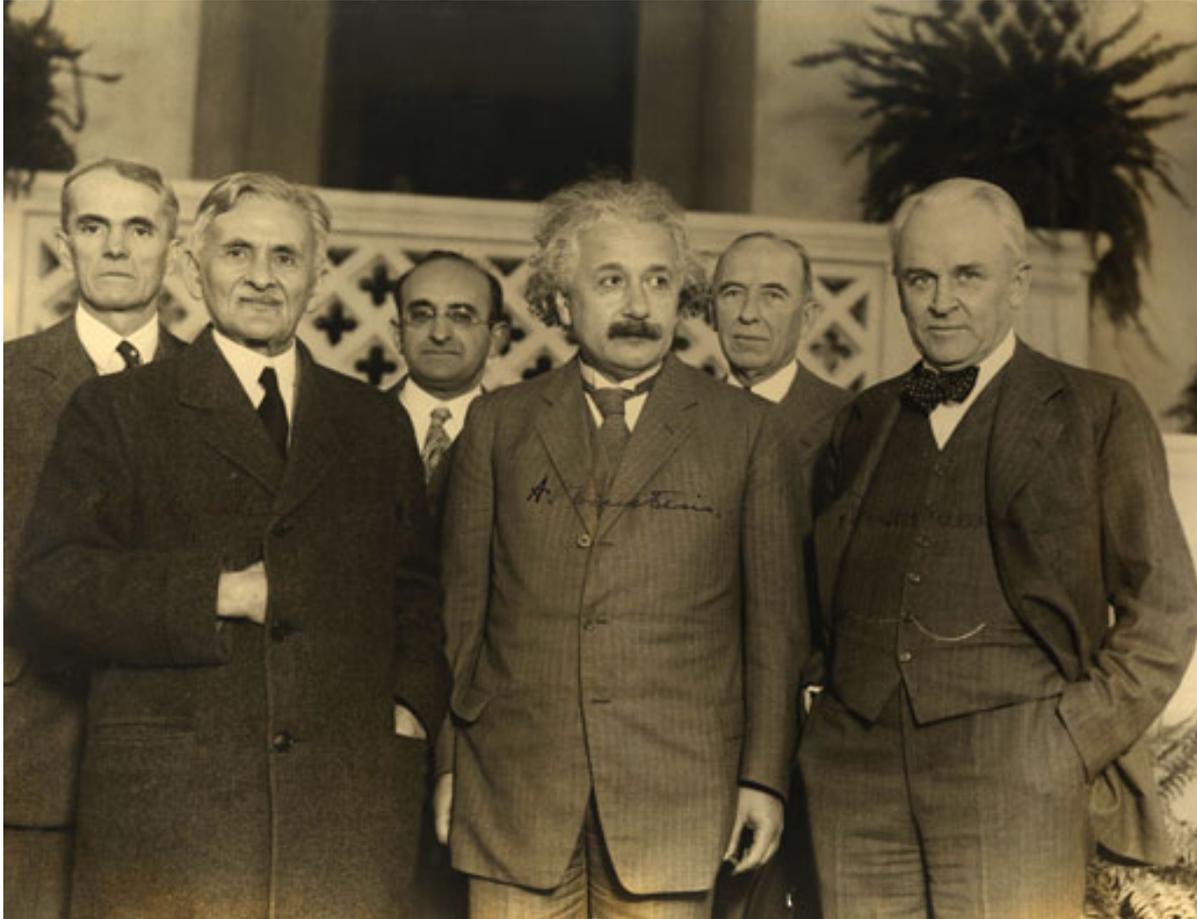


# Lecture Plan

- Lecture 1 (yesterday)
  - Core collapse supernovae (CCSNe), the nuclear equation of state, and neutron star structure.
  - Numerical relativity, general-relativistic hydrodynamics, and neutron star merger simulations with the `Einstein Toolkit`.
- “Workshop” (yesterday afternoon)
  - Neutron star structure calculations
  - Black hole formation in stellar collapse
  - Neutron star merger simulations
- Lecture 2 (now!)
  - LIGO and Gravitational-Wave Astronomy
  - Phenomenology of neutron star mergers.
  - Extreme core collapse events and the CCSN-LGRB relationship.
  - Gravitational waves from core-collapse supernovae.



# Gravitational Waves



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$$G^{\mu\nu} = \frac{8\pi G}{c^4} T^{\mu\nu}$$

# Gravitational Waves

$$G^{\mu\nu} = \frac{8\pi G}{c^4} T^{\mu\nu}$$

linearize

$$g_{\mu\nu} \approx \eta_{\mu\nu} + h_{\mu\nu}$$

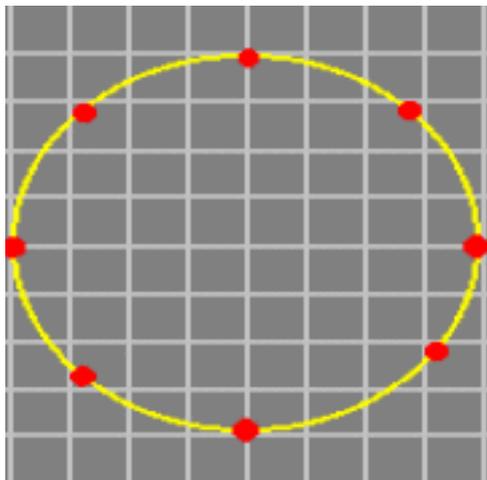
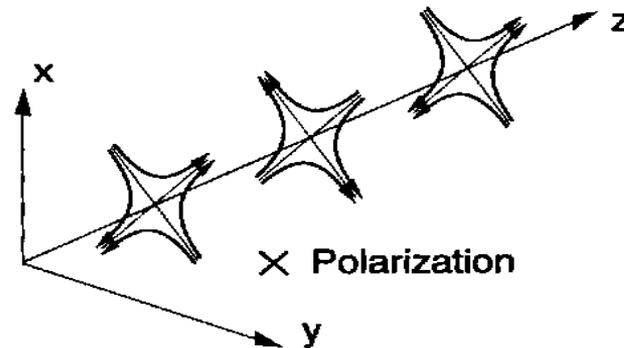
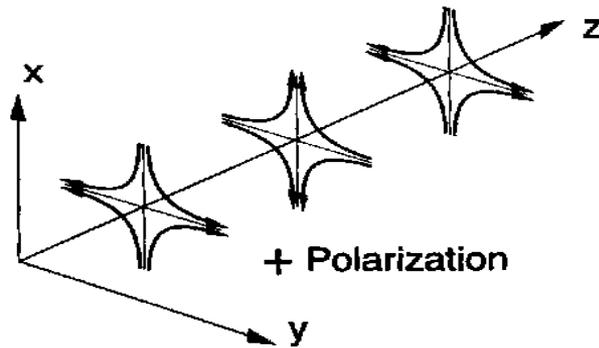
flat space metric  $\nearrow$  metric perturbation  $\nearrow$

$$\square h^{\mu\nu} = \left( -\frac{\partial^2}{\partial t^2} + \nabla^2 \right) h^{\mu\nu} = -\frac{16\pi G}{c^4} T^{\mu\nu}$$

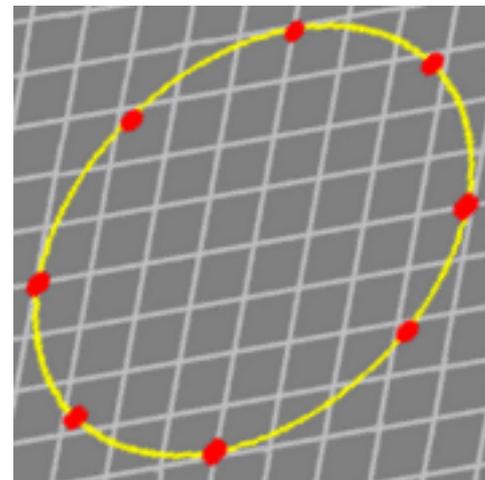
inhomogeneous wave equation  $\rightarrow$  gravitational waves (GWs)

# Gravitational Waves

In transverse-traceless gauge (TT) all gauge degrees of freedom fixed:



“+ Polarization”



“x Polarization”

<http://www.johnstonsarchive.net/relativity/pictures.html>

# Gravitational Wave Emission

- GWs are to lowest-order **quadrupole waves**.
- Emitted by **accelerated aspherical bulk mass-energy motions**.
- Slow-motion weak-field quadrupole approximation:

$$h_{jk}^{TT}(t, \vec{x}) = \left[ \frac{2G}{c^4} \frac{1}{|\vec{x}|} \ddot{I}_{jk}(t - \frac{|\vec{x}|}{c}) \right]^{TT}$$

→ *dimensionless GW "strain" (displacement)*     
 → *mass quadrupole moment*     
 ← *"Transverse-Traceless Gauge"*

$\frac{G}{c^4} \approx 10^{-49} \text{ s}^2 \text{ g}^{-1} \text{ cm}^{-1}$

First Numerical Estimate:  $M \equiv$  "aspherical mass"

$$I_{jk} = \int \rho x_j x_k d^3x \quad \frac{d^2}{dt^2} I \sim \mathcal{O}(Mv^2) \quad h \sim \frac{2G}{c^4 D} Mv^2$$

$$M = 1M_{\odot} \quad v = 0.1c$$

$$D = 10 \text{ kpc} \quad \longrightarrow \quad h \sim 10^{-19}$$

# Gravitational Wave Emission

- **GWs** are **very weak** and **interact weakly with matter**.
  - No human-made sources.

# Gravitational Wave Emission

- GWs are **very weak** and **interact weakly with matter**.

- **Caltech**



GW generator,  
TAPIR group,  
Caltech



# Gravitational Wave Emission

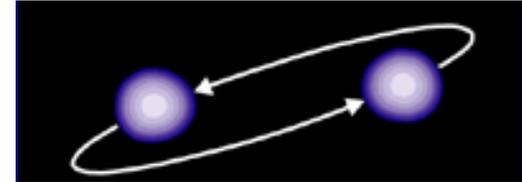
- **GWs** are **very weak** and **interact weakly with matter**.
  - No human-made sources.
  - **Bad**: *Very hard to detect.*
  - **Good**: *Travel from source to detectors unscathed by intervening material.*

# Astrophysical GW Sources

- **Coalescing binaries:**

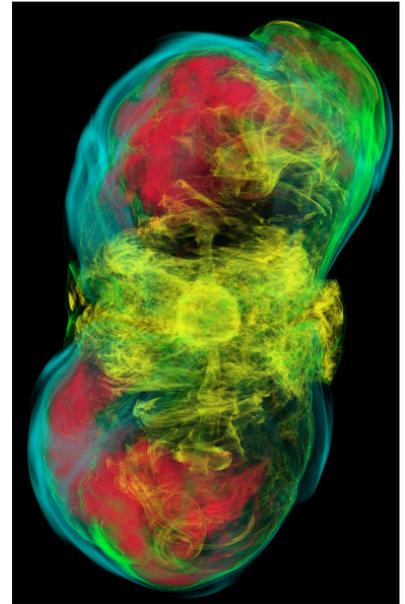
NS/NS, NS/BH  $h \approx 10^{-22}$  @ 100 Mpc

BH/BH ( $2 \times 30 M_{\text{Sun}}$ )  $h \approx 10^{-22}$  @ 1 Gpc



- **Core-collapse supernovae:**

convection, rotation etc.  $h \approx 10^{-22}$  @ 10 kpc

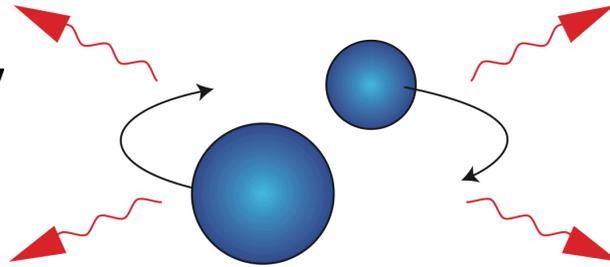


- **Other:**

- Spinning NSs with mountains.
- Glitching pulsars.
- Bursting soft-gamma repeaters.
- Cosmological background, cosmic string cusps.
- At low frequencies: double WDs, supermassive BH-BH binaries.

# Key GW Sources: Coalescing Binaries

Consider a circular binary of point particles.



$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$

$$M = m_1 + m_2$$

$$r_1^i(t) = \frac{\mu a}{m_1} \{\cos \theta, \sin \theta, 0\} \quad a = |r_1| + |r_2| \text{ (semi-major axis)}$$

$$r_2^i(t) = \frac{\mu a}{m_2} \{-\cos \theta, -\sin \theta, 0\}$$

$$\theta = \omega t = 2\pi f_{\text{orb}} t = 2\pi \frac{t}{P_{\text{orb}}} \quad \omega = \sqrt{\frac{GM}{a^3}}$$

Now evaluate:

$$I_{jk} = \int \rho x_j x_k d^3 x \quad h_{jk}^{TT}(t, \vec{x}) = \left[ \frac{2}{c^4} \frac{G}{|\vec{x}|} \ddot{I}_{jk} \left( t - \frac{|\vec{x}|}{c} \right) \right]^{TT}$$

# GWs from Coalescing Binaries

$$\begin{aligned} I_{xx} &= \int d^3x (\rho x^2) = m_1 x_1^2 + m_2 x_2^2 \\ &= \left( \frac{\mu^2 a^2}{m_1^2} m_1 + \frac{\mu^2 a^2}{m_2^2} m_2 \right) \cos^2 \omega t \\ &= \mu^2 a^2 \left( \frac{1}{m_1} + \frac{1}{m_2} \right) \cos^2 \omega t \\ &= \mu a^2 \cos^2 \omega t = \frac{1}{2} \mu a^2 (1 + 2 \cos 2\omega t) \end{aligned}$$

# GWs from Coalescing Binaries

Similarly, obtain the other components:

$$I_{ij} = \frac{1}{2} \mu a^2 \begin{pmatrix} \cos 2\omega t & \sin 2\omega t & 0 \\ \sin 2\omega t & -\cos 2\omega t & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

Second time derivative:

$$\ddot{I}_{ij} = 2\mu a^2 \omega^2 \begin{pmatrix} -\cos 2\omega t & -\sin 2\omega t & 0 \\ -\sin 2\omega t & \cos 2\omega t & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

For observer at distance  $D$  along the  $z$  axis already in TT gauge:

$$h_{ij}^{TT} = \frac{4G}{c^4} \frac{\mu a^2 \omega^2}{D} \begin{pmatrix} -\cos 2\omega t & -\sin 2\omega t & 0 \\ -\sin 2\omega t & \cos 2\omega t & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

# GWs from Coalescing Binaries

$$h_+ = -\frac{4G}{c^4} \frac{\mu a^2 \omega^2}{D} \cos 2\omega t$$

$$h_\times = -\frac{4G}{c^4} \frac{\mu a^2 \omega^2}{D} \sin 2\omega t$$

$$\frac{dE_{\text{GW}}}{dt} = P = \frac{G}{c^5} \langle \ddot{I}_{ij} \ddot{I}_{ij} \rangle$$

time average  
over a cycle



Radiated energy must come from orbital energy -> also change of angular momentum. Change of orbital separation:

$$\left\langle \frac{da}{dt} \right\rangle = -\frac{64}{5} \frac{G^3}{c^5} \frac{m_1 m_2 M}{a^3} \quad a(t) = \left( \frac{256}{5} \frac{G^3}{c^5} \mu M^2 \right)^{\frac{1}{4}} (t_c - t)^{\frac{1}{4}}$$

# GWs from Coalescing Binaries

Coalescence time:

$$\tau_{\text{merge}} = a_0^4 \frac{5}{256} \frac{c^5}{G^3} \frac{1}{\mu M^2} \quad m_1=m_2=1.4 M_{\odot}$$

$$a_0 = 10^6 \text{ km} \quad \rightarrow \tau_{\text{merge}} \sim 120 \times 10^6 \text{ yrs.}$$

$$a_0 = 1000 \text{ km} \quad \rightarrow \tau_{\text{merge}} \sim 3700 \text{ s}$$

$$a_0 = 100 \text{ km} \quad \rightarrow \tau_{\text{merge}} \sim 370 \text{ ms}$$

(but: Newtonian estimates!)

# GW Frequency Evolution

Frequency evolution:

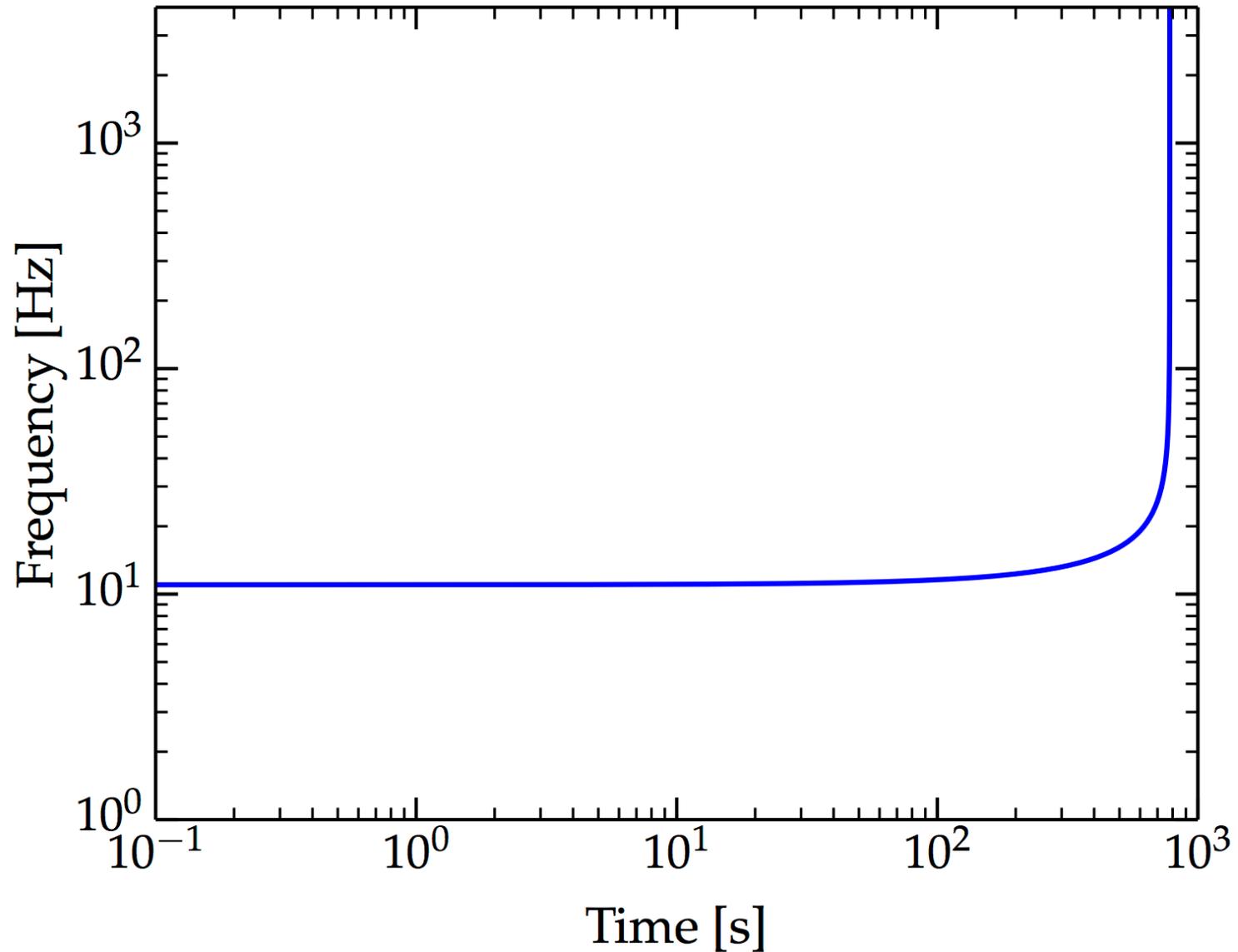
$$\dot{a} = -\frac{64}{5} \frac{G^3}{c^5} \frac{\mu M^2}{a^3}$$
$$f = 2 \frac{\omega}{2\pi} = \frac{1}{\pi} (GM)^{\frac{1}{2}} a^{-\frac{3}{2}}$$

$$\dot{f} = \frac{96}{5} \pi^{8/3} \frac{G^{5/3}}{c^5} \mu M^{2/3} f^{11/3}$$

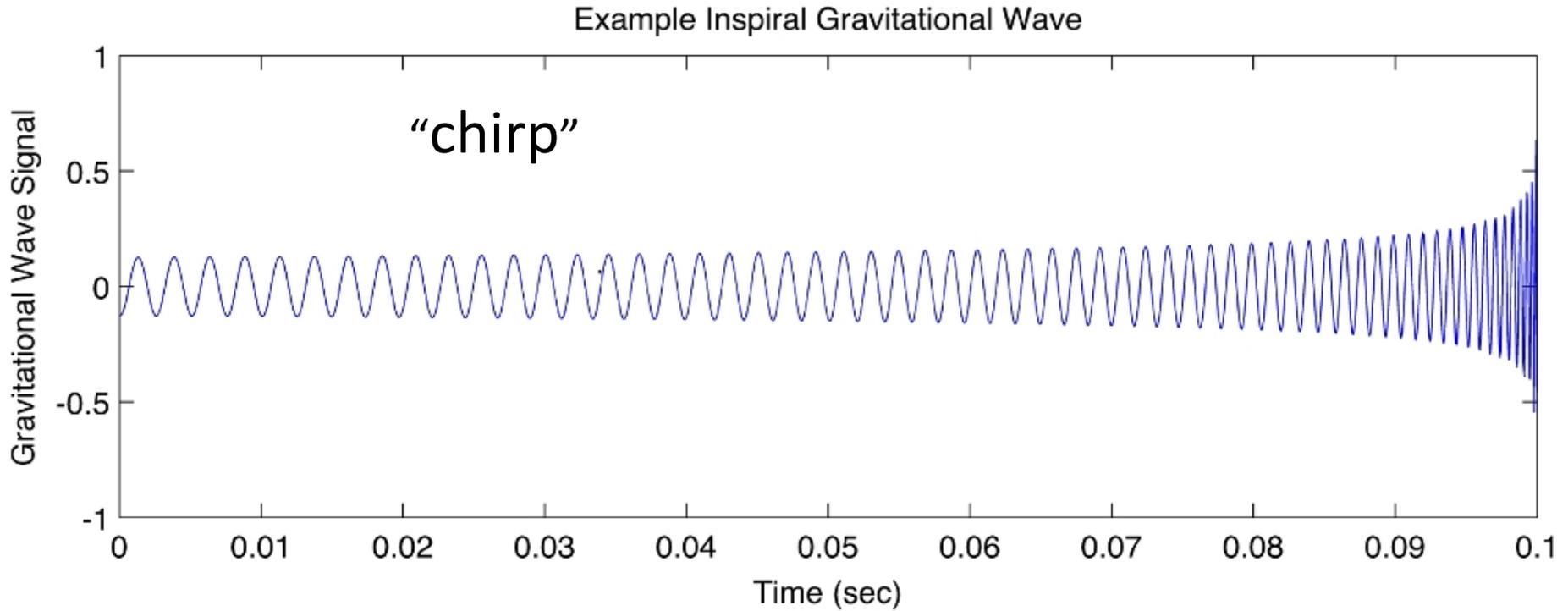
$$\dot{f} = \frac{96}{5} \pi^{8/3} \frac{G^{5/3}}{c^5} \mathcal{M}^{5/3} f^{11/3}$$

$$\mathcal{M} = \mu^{3/5} M^{2/5} \quad \text{“Chirp Mass”}$$

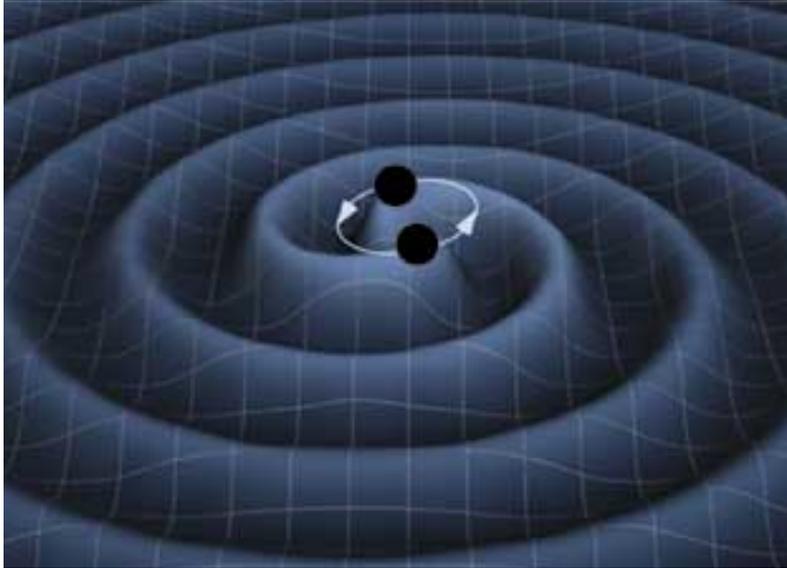
# GW Frequency Evolution



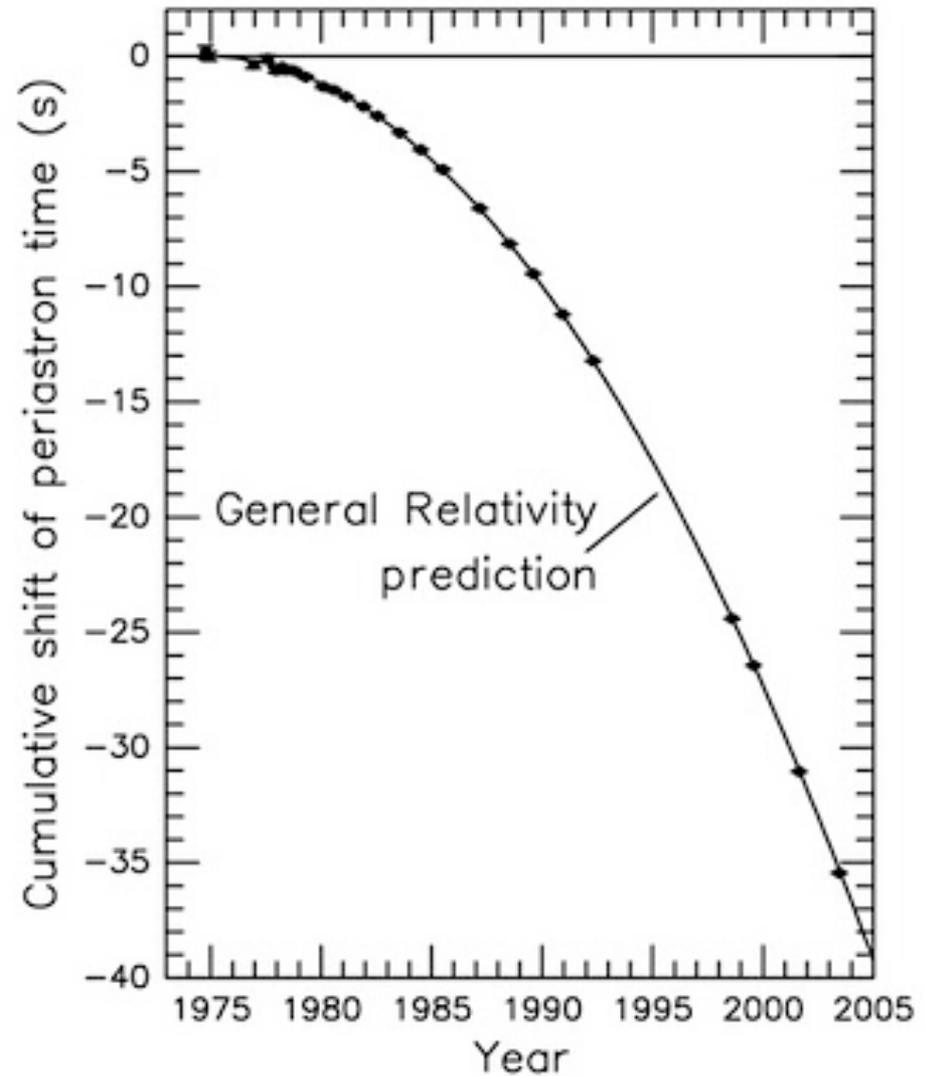
# GW Signal



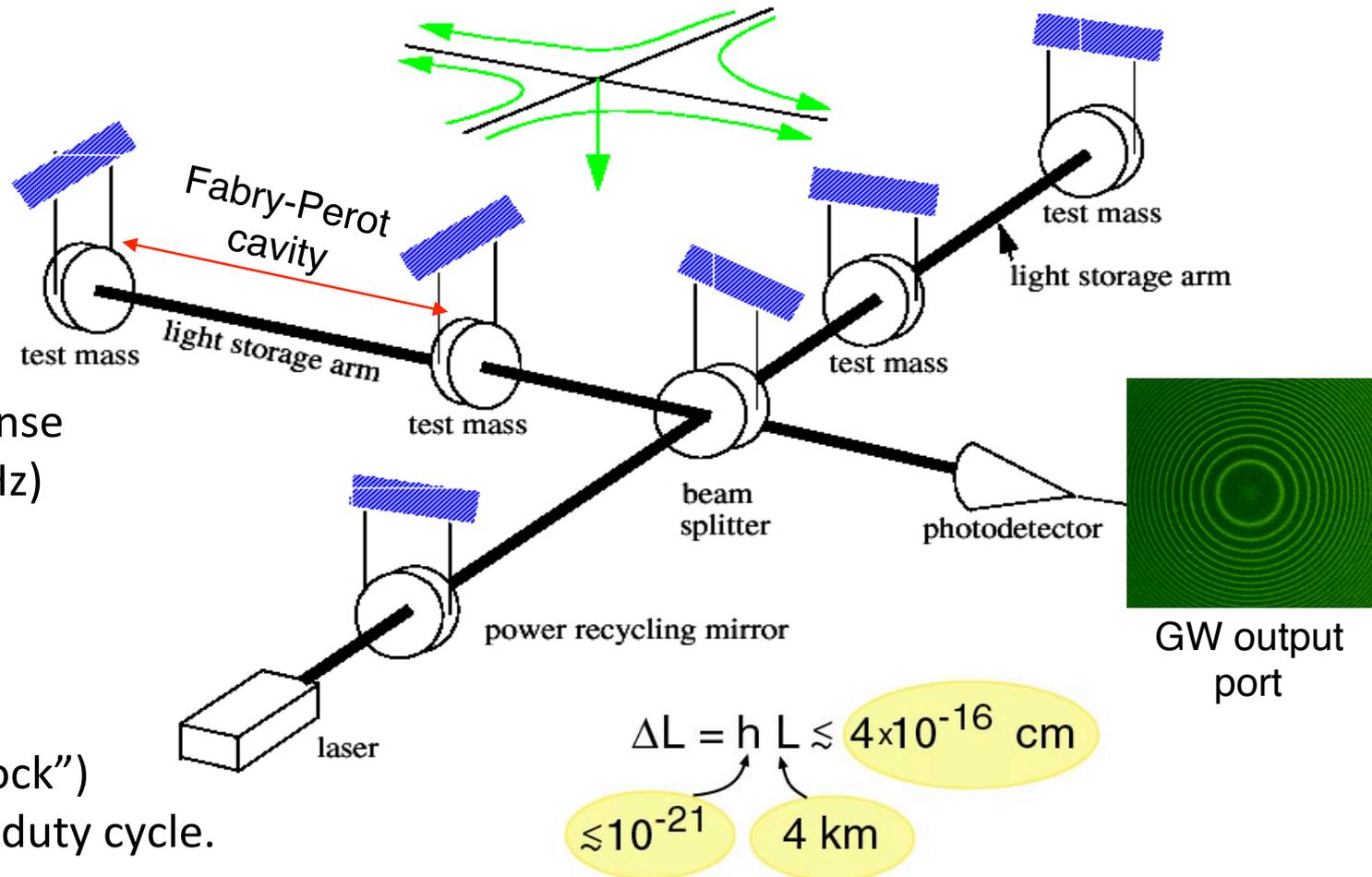
# Gravitational Waves: Indirect Evidence



- GWs lead to “orbital decay”  
-> binary stars get closer to each other.
- Double neutron star systems in the Milky Way.
- PSR 1913+16:  
“Hulse-Taylor Pulsar”  
-> Nobel prize in Physics 1993



# Gravitational Wave Detection



## Advantages:

- Broadband response (~50 Hz to few KHz)
- High sensitivity

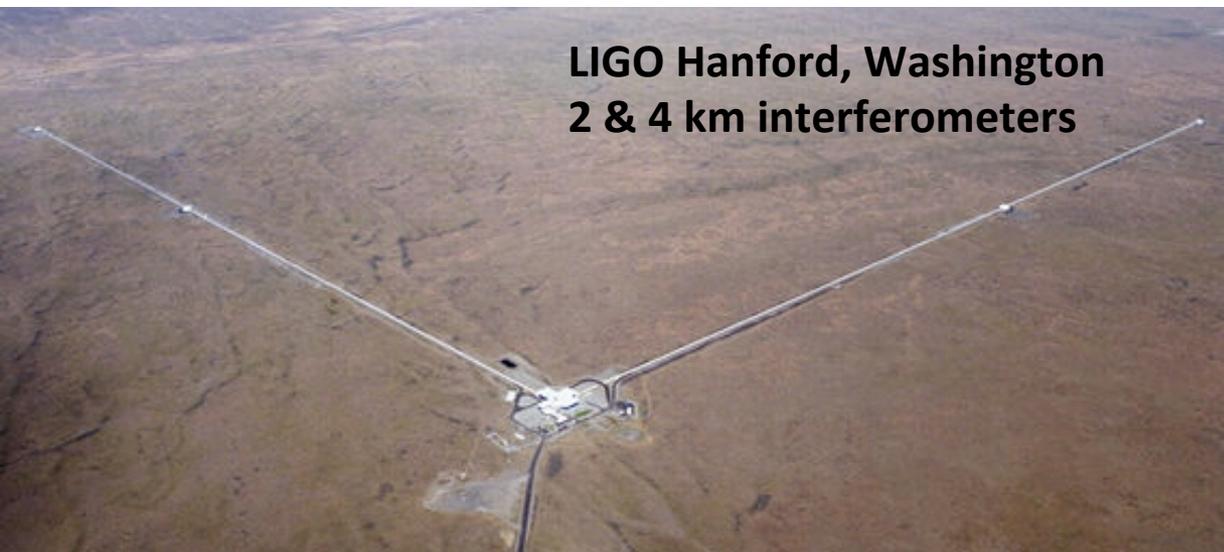
## Disadvantage:

- Very difficult to keep stable ("in lock")  
 -> relatively poor duty cycle.  
 (LIGO ~60%,  
 Virgo ~80%)

Basic Michelson Interferometer design + upgrades  
 (power recycling, Fabry Perot cavities)



# Laser Interferometer Gravitational-Wave Observatory



LIGO Hanford, Washington  
2 & 4 km interferometers



LIGO Livingston, Louisiana  
4 km interferometer

Measure relative  
displacements of  $10^{-22}$

Envisioned in the 1980s by  
Kip Thorne, Rai Weiss, Ron Drever  
Built in the 1990s.

6 "science runs" 2002-2010.



# Laser Interferometer Gravitational-Wave Observatory



LIGO Hanford, Washington  
2 & 4 km interferometers

Caltech 

-> Hydrogen Bohr radius at  
the Earth-Sun distance.

-> 1/1000 proton radius  
over 4 km arm length.

Livingston, Louisiana  
interferometer

Measure relative  
displacements of  $10^{-22}$

Envisioned in the 1980s by  
Kip Thorne, Rai Weiss, Ron Drever  
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A long, white, corrugated metal pipeline stretches across a dry, hilly landscape. The pipeline is supported by a series of metal brackets and runs parallel to a paved road on the left. In the distance, a small, white, rectangular building with a flat roof is visible, labeled as the "mid station". The surrounding terrain is arid and brown, with rolling hills and a clear sky. A small sign with the number "571" is visible on the road in the lower-left corner.

mid station

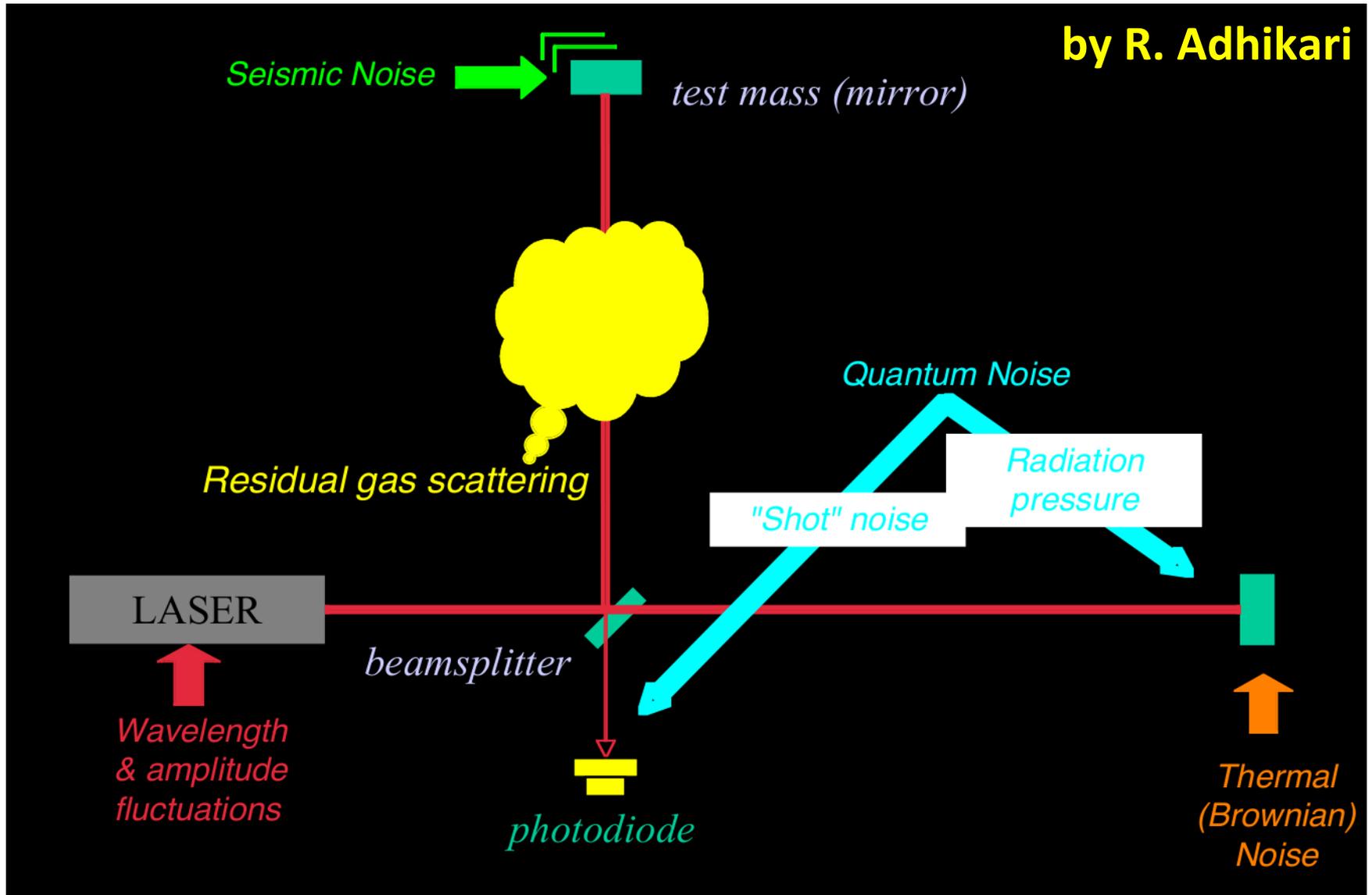
**Initial LIGO: 2000-2010**  
currently being upgraded  
to **Advanced LIGO**



**Advanced LIGO  
will be 10 x more  
sensitive!**

# Noise Sources

by R. Adhikari



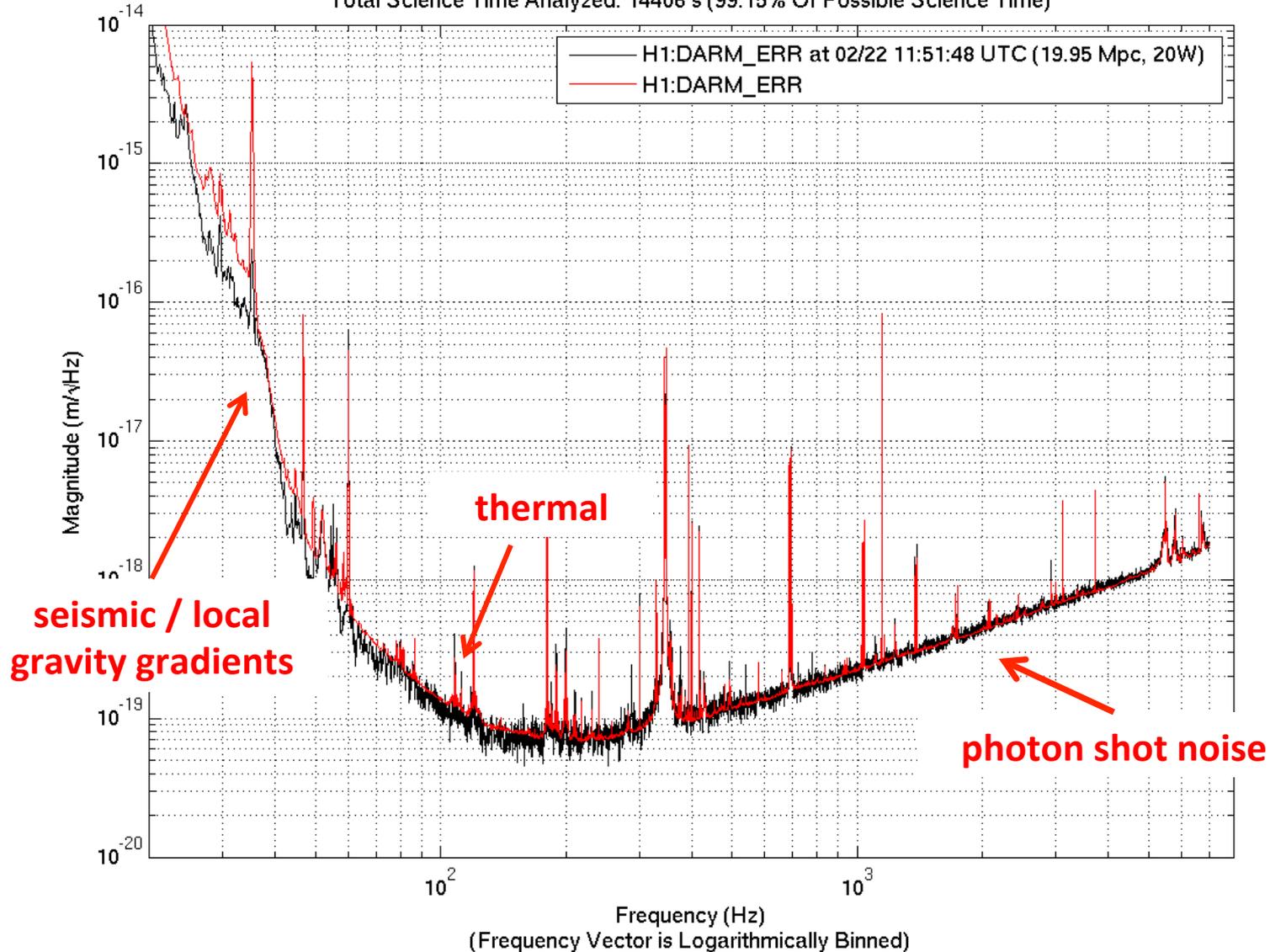
# Noise Budget

H1:DARM\_ERR at 20W (05/13 22:43:33 UTC - 05/14 06:43:33 UTC)

Range Of Calibrated Spectrum: 18.04 Mpc

Total Science Time Analyzed: 14406 s (99.15% Of Possible Science Time)

One-sided noise amplitude spectral density



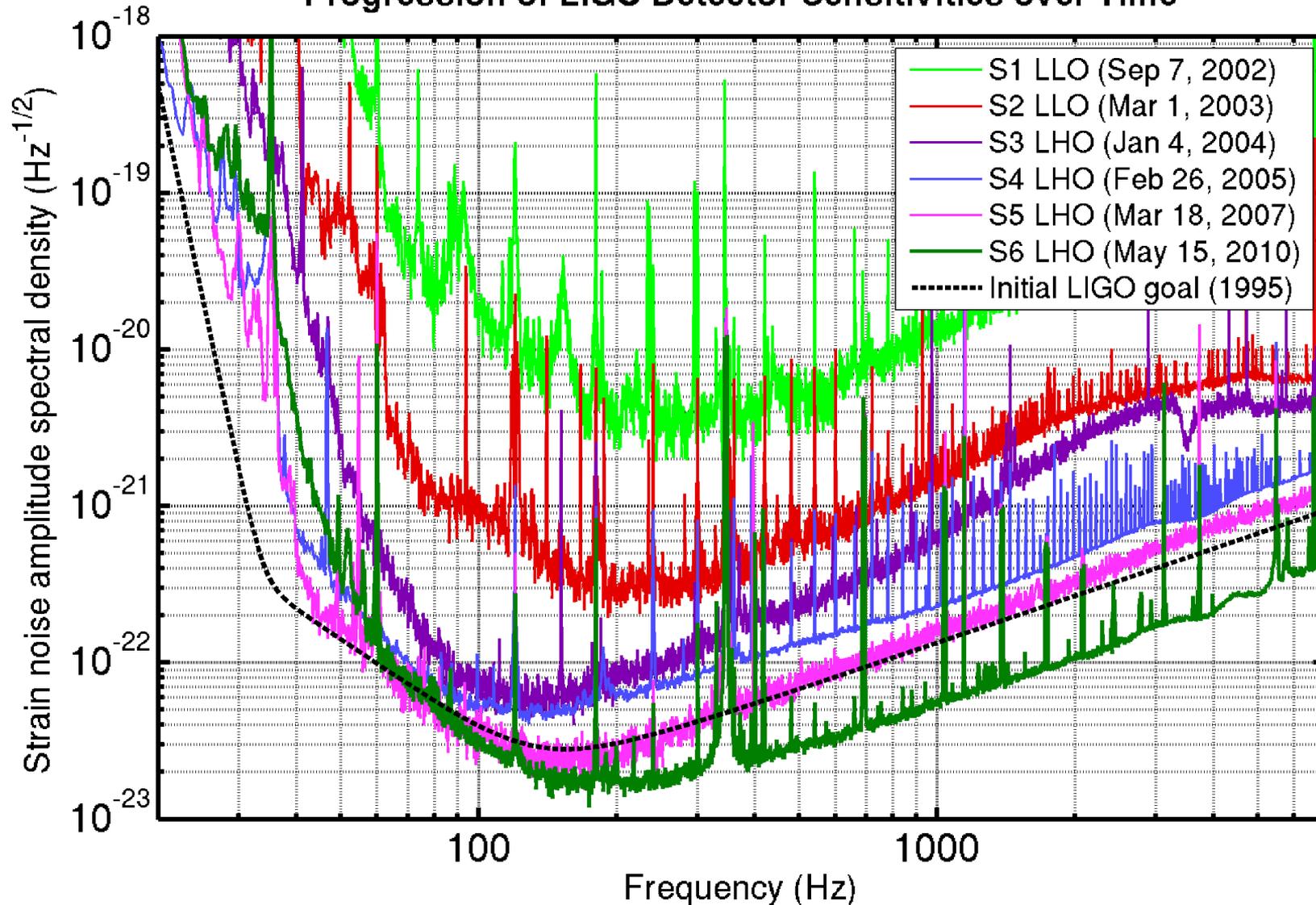
# Anthropogenic Noise...



+ trucks, trains, tree cutting, rush hour on highways...

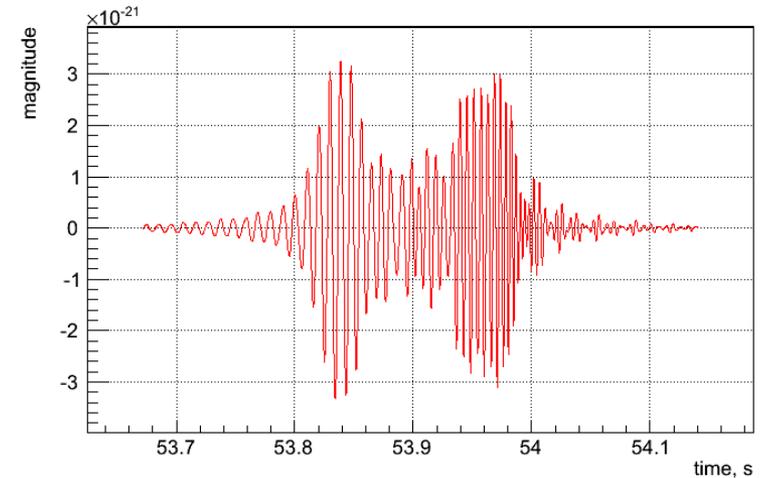
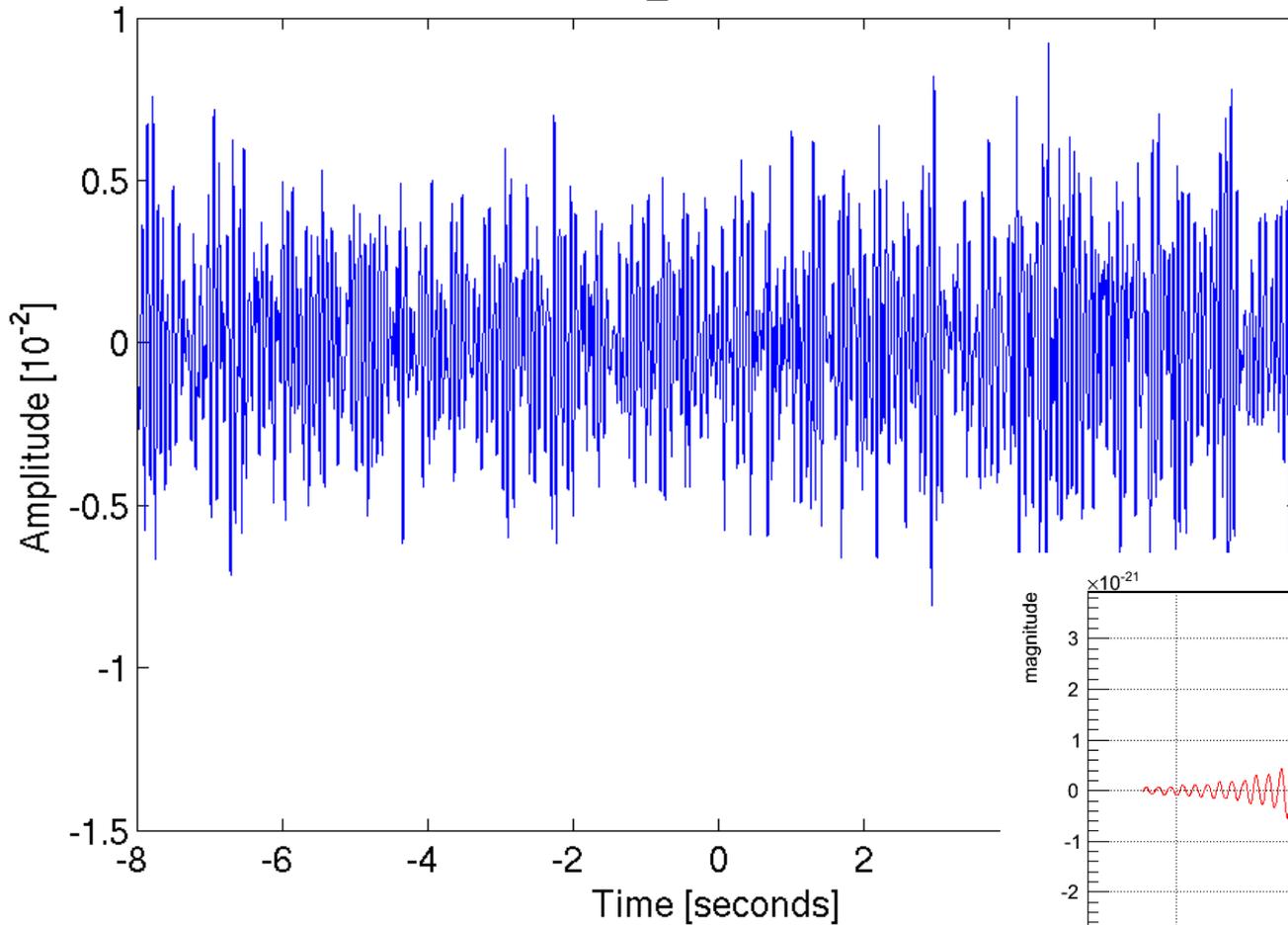
# Initial LIGO Interferometers: Sensitivity

Progression of LIGO Detector Sensitivities over Time



# The Data Analysis Challenge: Digging out the Signal

H1:LSC-DARM\_ERR at 968654557.957



# Gravitational Wave Astronomy

## International Network of LIGOs

First Generation – 2000 -- 2010

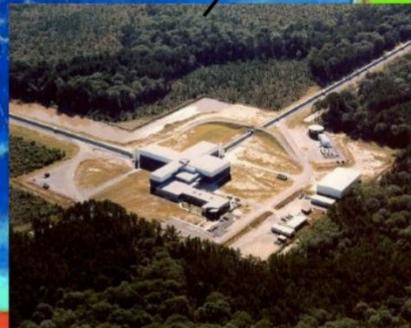
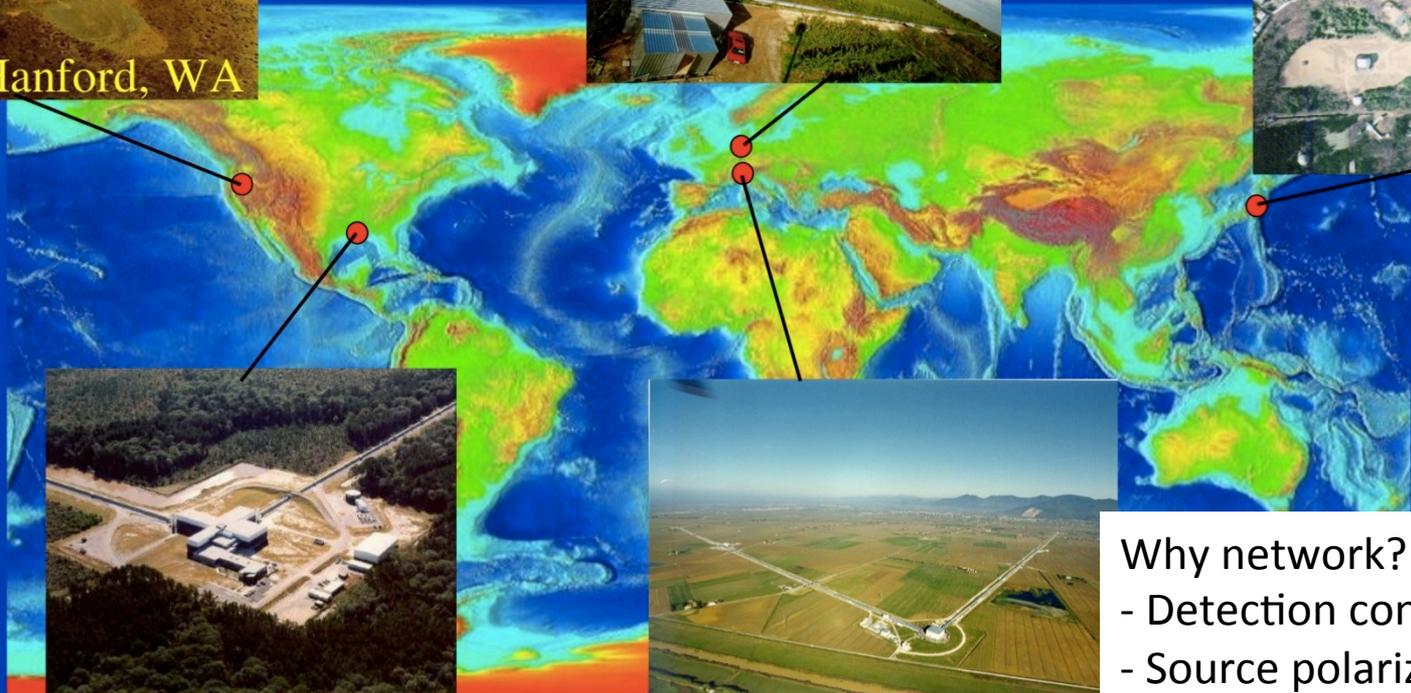


LIGO Hanford, WA

GEO 600  
Germany



TAMA 300  
Japan



LIGO Livingston, LA



VIRGO, Italy

Why network?

- Detection confidence
- Source polarization
- Sky localization
- Sky coverage
- Duty cycle

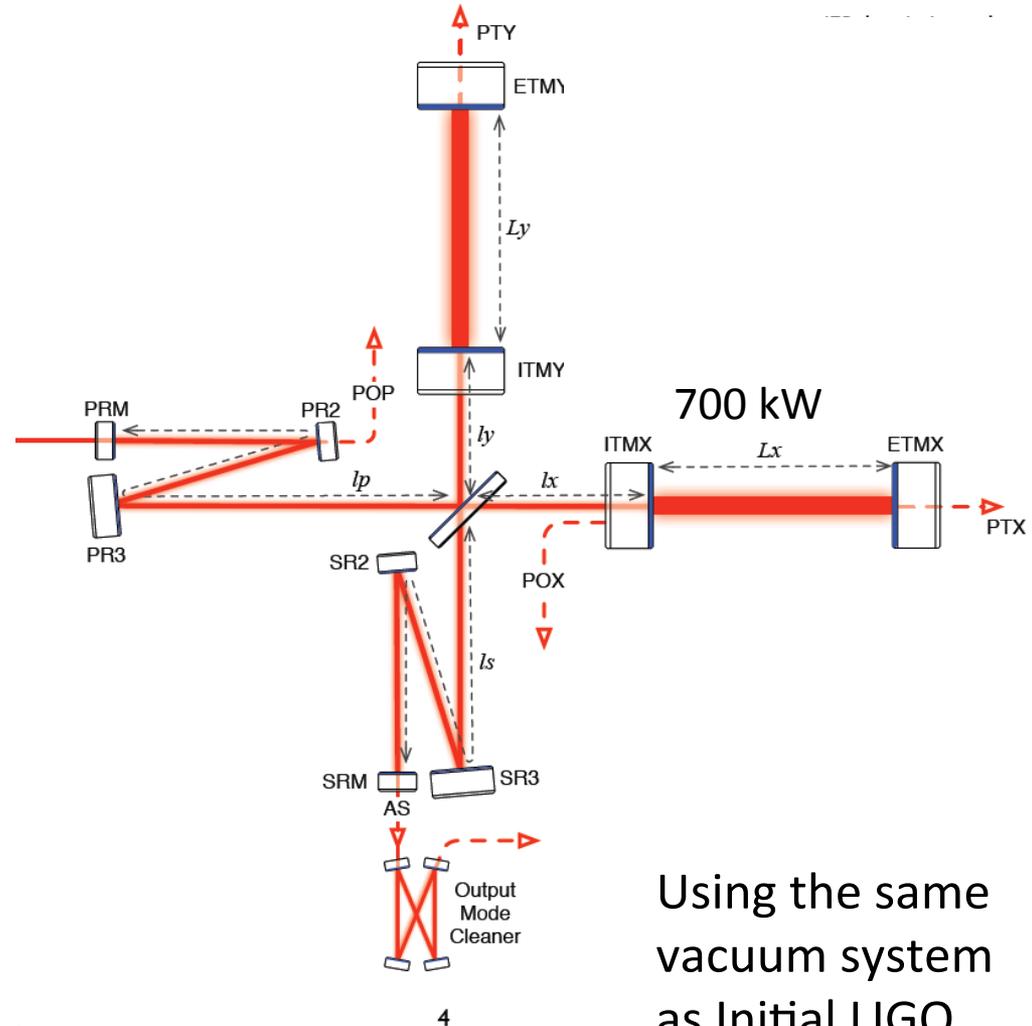


Joint LIGO/GEO + Virgo data in most recent science runs.

# Advanced LIGO

## What is Advanced?

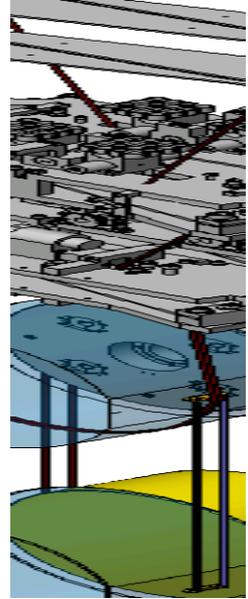
Parameter	Initial LIGO	Advanced LIGO
<b>Input Laser Power</b>	10 W (10 kW arm)	<b>180 W</b> (>700 kW arm)
<b>Mirror Mass</b>	10 kg	<b>40 kg</b>
<b>Interferometer Topology</b>	Power-recycled Fabry-Perot arm cavity Michelson	Dual-recycled Fabry-Perot arm cavity Michelson (stable RC)
<b>Optimal Strain Sensitivity</b>	$3 \times 10^{-23}$ / rHz	Tunable, better than $5 \times 10^{-24}$ / rHz in broadband
<b>Seismic Isolation Performance</b>	$f_{low} \sim 50$ Hz	$f_{low} \sim 12$ Hz
<b>Mirror Suspensions</b>	Single Pendulum	Quadruple pendulum



Using the same vacuum system as Initial LIGO.

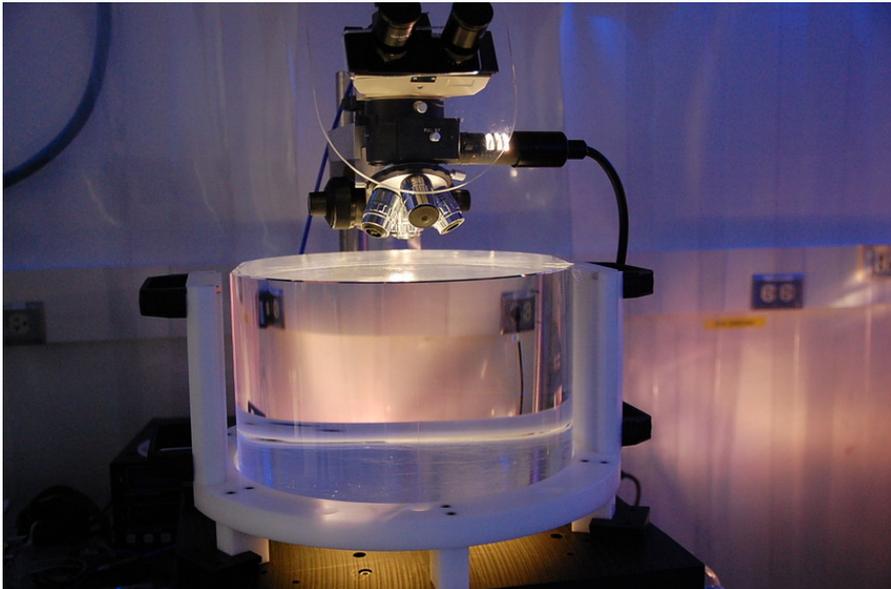
# Advanced LIGO Mirrors

- Made of high-purity fused silica.
- Initial LIGO: 25 cm diameter, 10 cm thick, 10.7 kg.  
**Advanced LIGO: 34 cm diameter, 20 cm thick, 40 kg.**
- Surfaces polished to  $\sim 1$  nm, most with slight curvature.
- Coated to reflect with extremely low scattering loss.

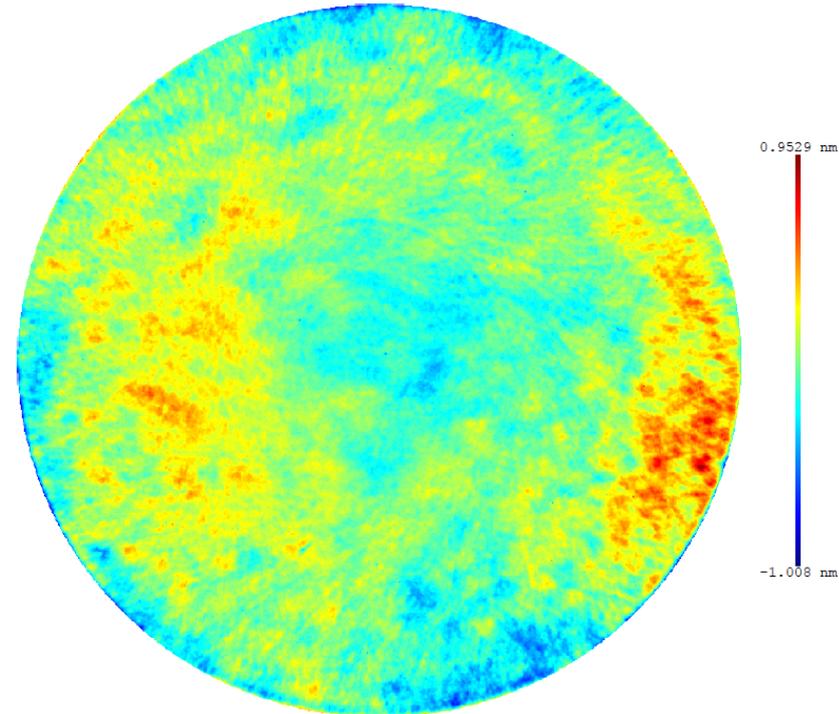


at

ETM 01 R1 D300 Z1-4 Removed



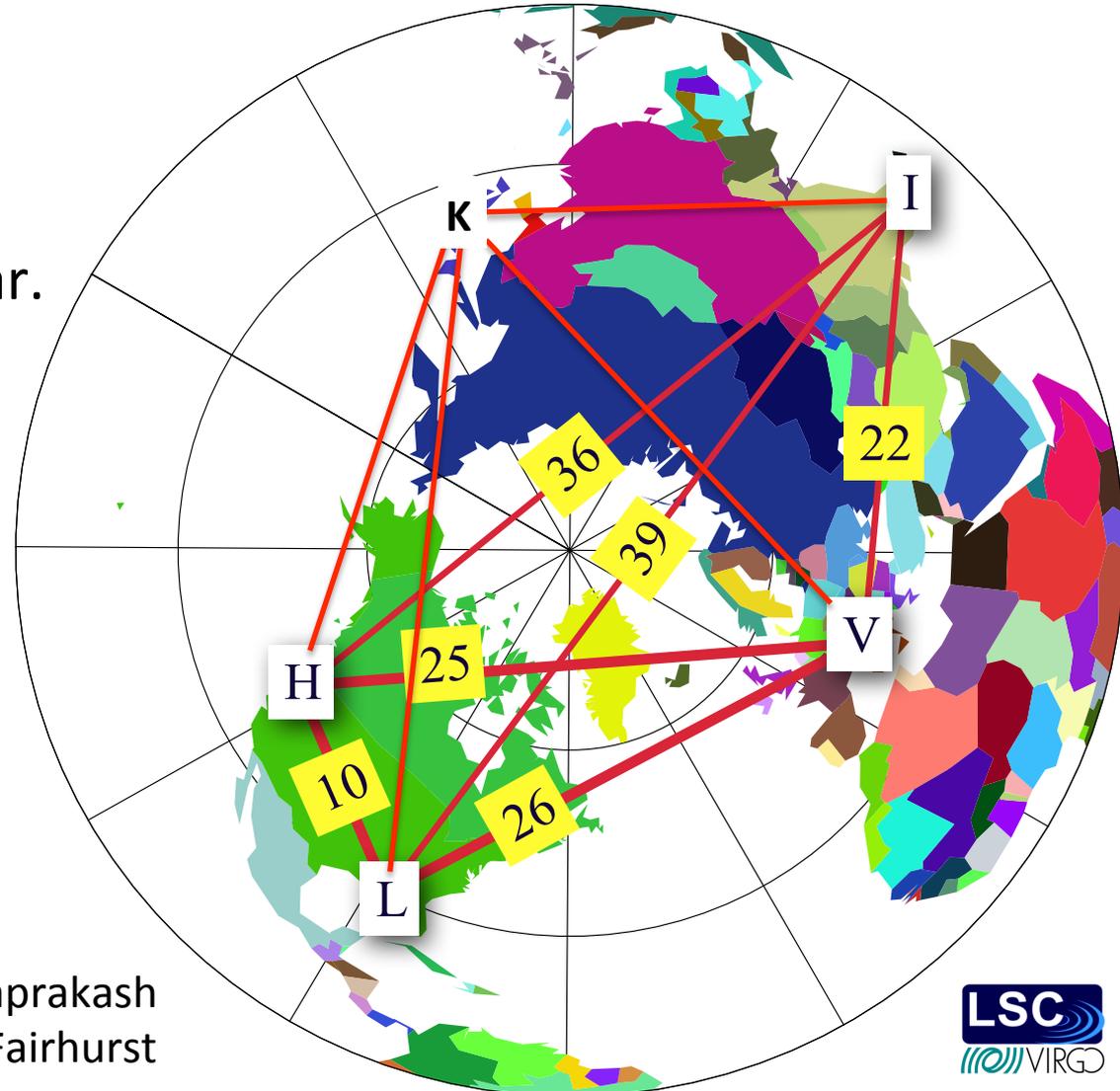
(Source: P. Shawhan, UMD)



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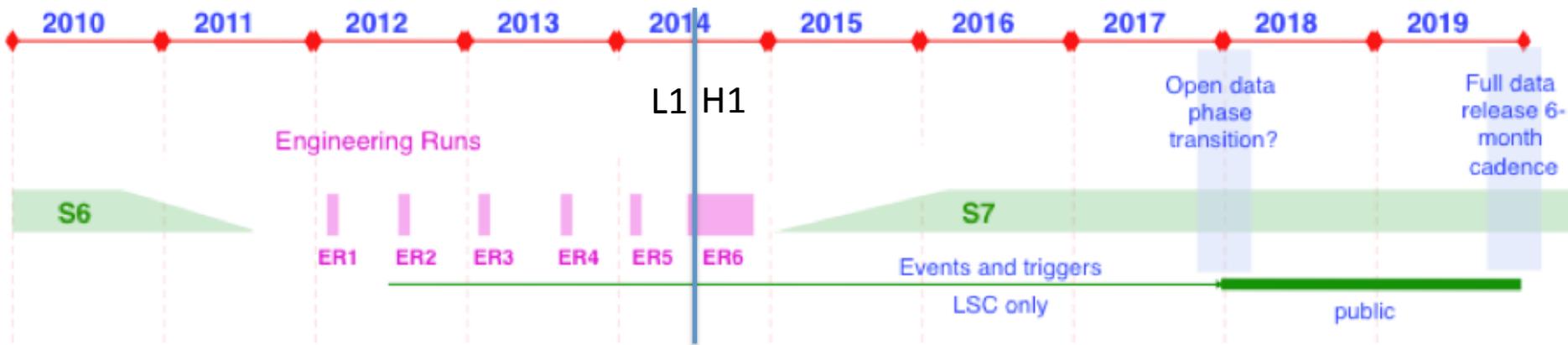
# The Future: Advanced Detectors

- Upgrades to existing IFOs -> **LIGO & Virgo are currently offline.**  
“Astrowatch” by GEO600.
- 10 x sensitivity  
-> 1000 x probed volume.  
Expect  $\mathcal{O}(10)$  events / year.
- New interferometers:  
**LIGO India**  
KAGRA (Japan)



Sathyaprakash  
Fairhurst

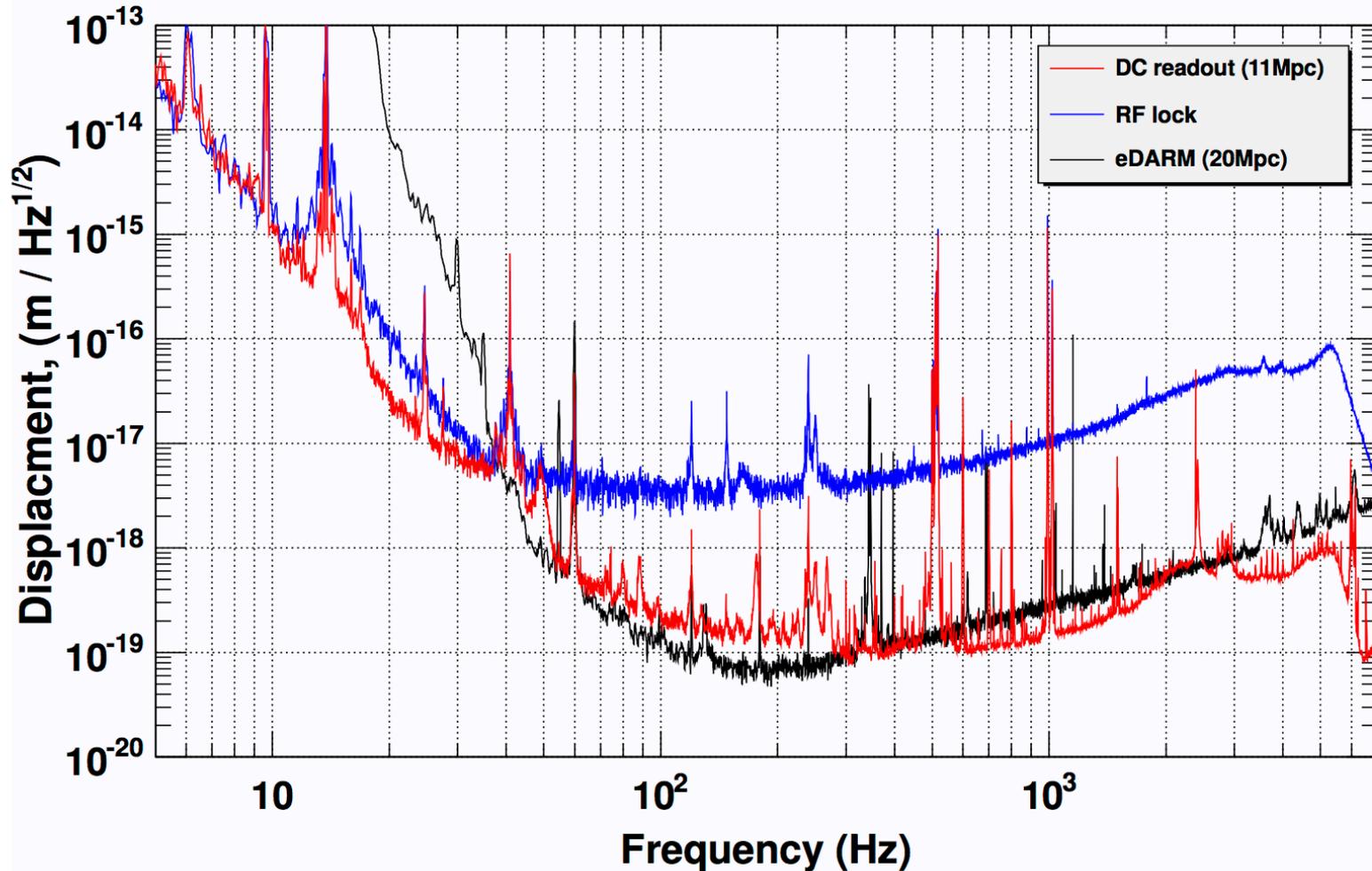
# Advanced LIGO: Status & Timeline



- **Advanced LIGO:**
  - Livingston (L1) detector completed, locked for > 2h.
  - Hanford (H1) in final stages of installation.
  - On track for first science data in mid/late 2015.
  - Design sensitivity expected 2017-2020.  
NS-NS range ~200-300 Mpc; CCSNe: galaxy, LMC/SMC
  - First science run 2-detector (poor sky localization).
- Advanced Virgo & KAGRA: 2015/16+
- LIGO India: 2021-22+

# Current L1 Sensitivity

DARM NOISE, PSL POWER = 4.7W

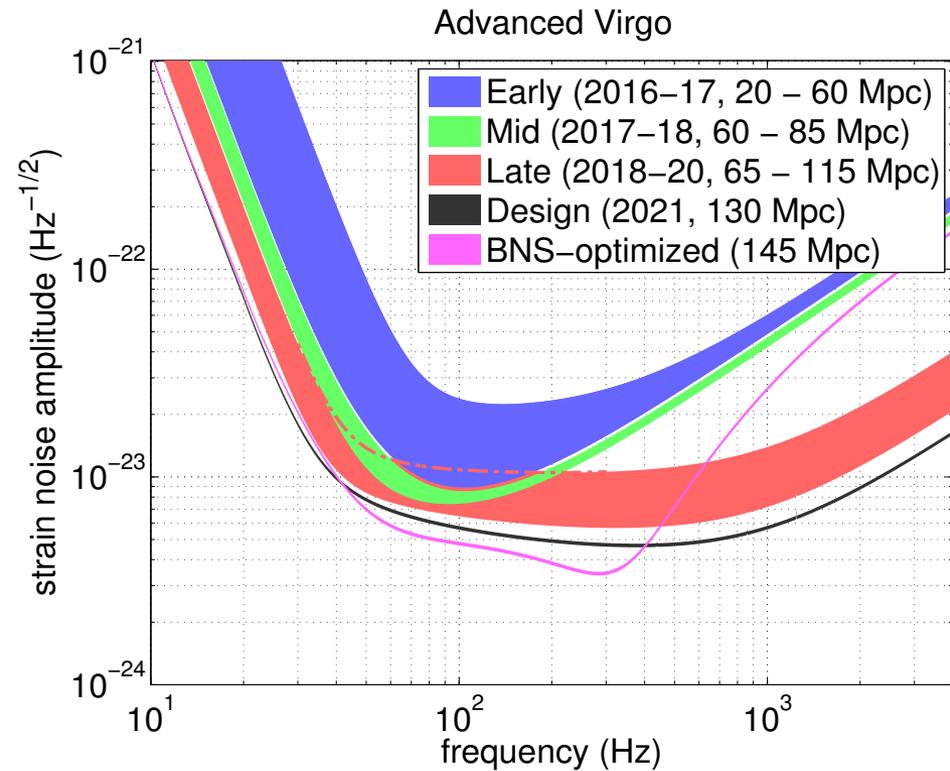
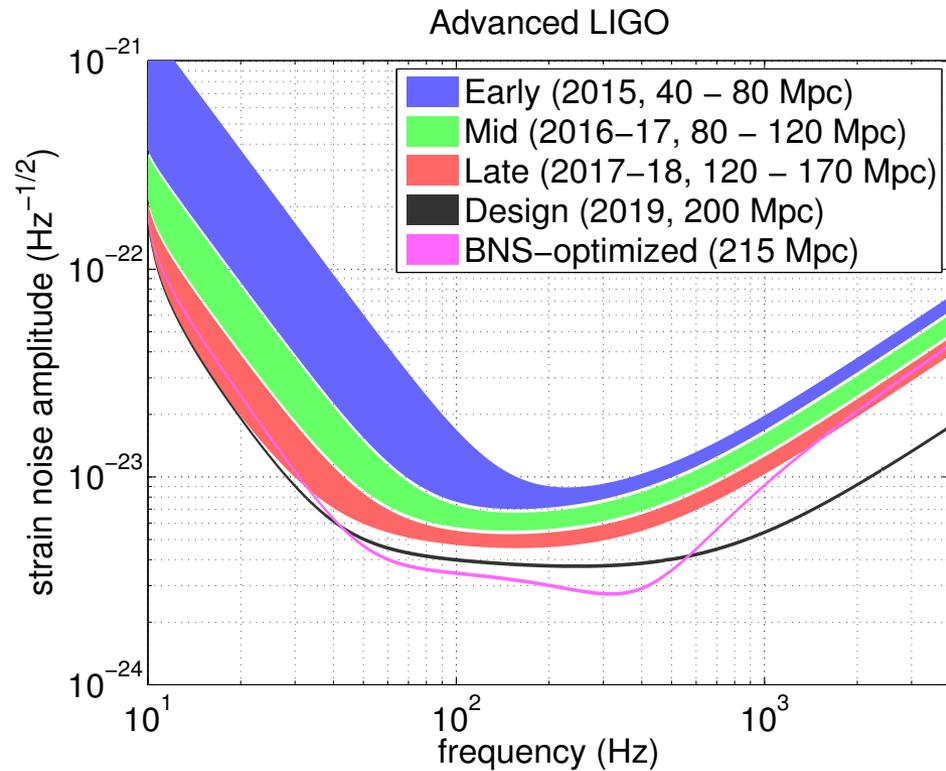


\*T0=15/07/2014 04:30:47

~1 month after first lock as good as  
initial LIGO after ~2.5 years.

# Expected Sensitivity Evolution

arXiv:1304.0670



# What will Advanced LIGO see?

(and how often will it see it?)

- Nearby core-collapse supernova rate: (1– 3) / 100 yrs.  
(No galactic core-collapse supernova until aLIGO ready!)
- Binary merger rate? Rough Estimate:
  - Merger rate in the Milky Way: few per  $10^6$  yrs.
  - Advanced LIGO NSNS range: 200 Mpc
  - Milky Way-equivalent galaxy density: 1 / 100 Mpc<sup>3</sup>
  - Detection rate:  $O(1)$ /yr

# What will 2019 Advanced LIGO see?

(and how often will it see it?)

- Summarized in Abadie et al., CQG 27, 173001 (2010) :

**Table 5.** Detection rates for compact binary coalescence sources.

IFO	Source <sup>a</sup>	$\dot{N}_{\text{low}} \text{ yr}^{-1}$	$\dot{N}_{\text{re}} \text{ yr}^{-1}$	$\dot{N}_{\text{high}} \text{ yr}^{-1}$	$\dot{N}_{\text{max}} \text{ yr}^{-1}$
Initial	NS–NS	$2 \times 10^{-4}$	0.02	0.2	0.6
	NS–BH	$7 \times 10^{-5}$	0.004	0.1	
	BH–BH	$2 \times 10^{-4}$	0.007	0.5	
	IMRI into IMBH			$<0.001^{\text{b}}$	$0.01^{\text{c}}$
	IMBH-IMBH			$10^{-4^{\text{d}}}$	$10^{-3^{\text{e}}}$
Advanced	NS–NS	0.4	40	400	1000
	NS–BH	0.2	10	300	
	BH–BH	0.4	20	1000	
	IMRI into IMBH			$10^{\text{b}}$	$300^{\text{c}}$
	IMBH-IMBH			$0.1^{\text{d}}$	$1^{\text{e}}$

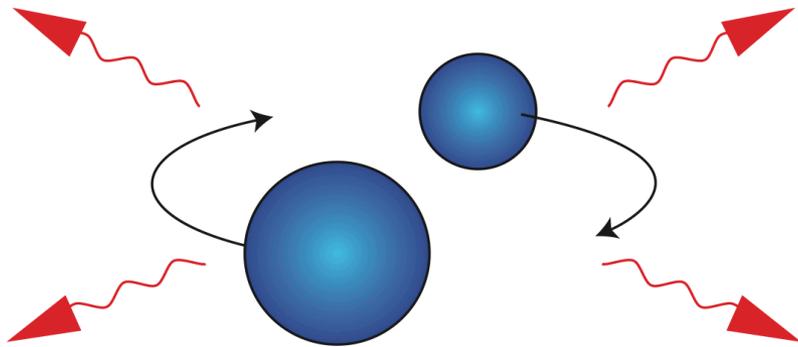
**Warning:**  
**Population synthesis!**

“Realistic” (=best-guess) event rates per year with advanced detectors later this decade

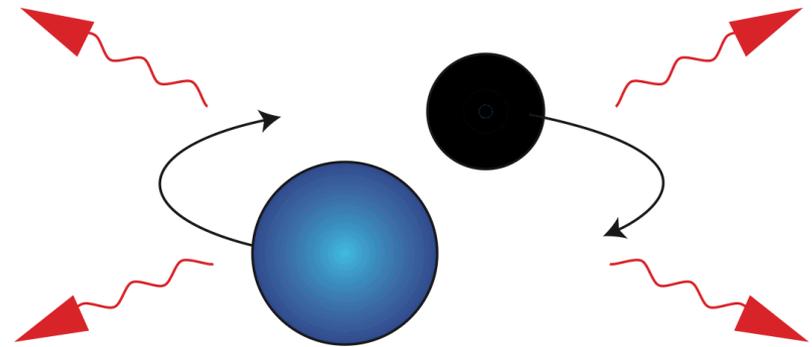


# Neutron Star Mergers

- Neutron Star + Neutron Star (NSNS)
- Black Hole + Neutron Star (BHNS)

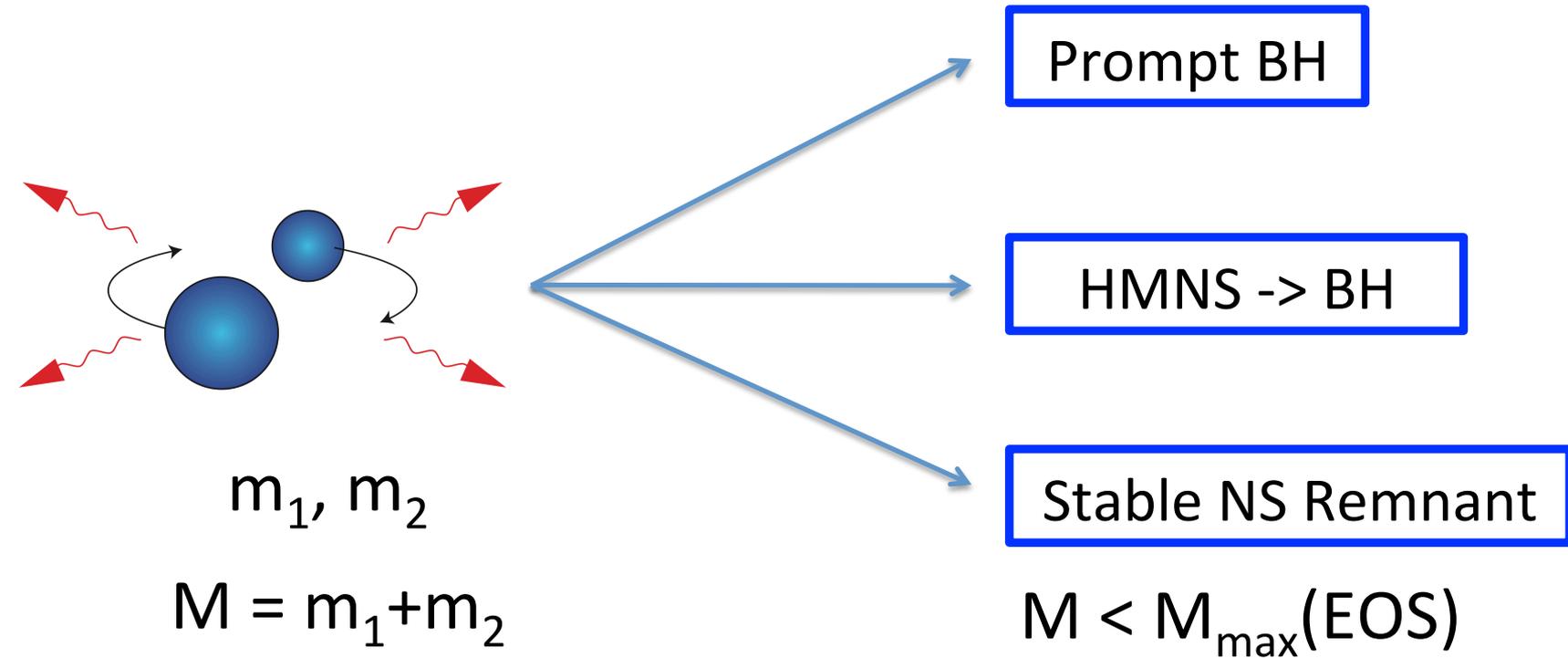


$M_1 \sim M_2 \sim 1.4 M_{\text{Sun}}$   
-> galactic NSNS binaries!



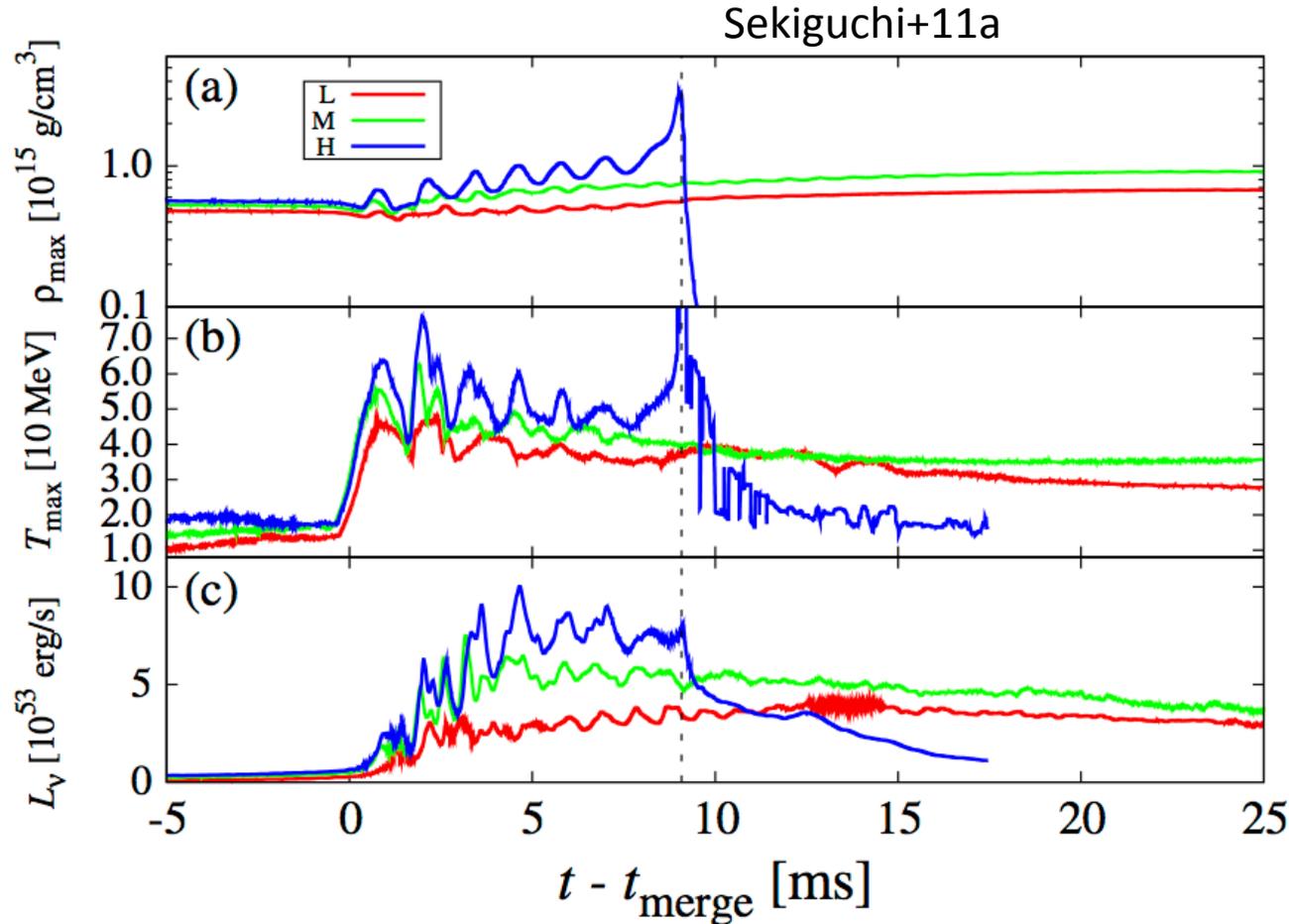
$M_{\text{BH}} \sim 7-10 \times M_{\text{NS}}$  (Belczynski+'10)  
(but no BHNS systems known)

# NSNS Merger Scenarios



Outcome most sensitive to **total mass of binary** and **nuclear EOS**.

# NSNS Postmerger Evolution



H. Shen EOS

L:  $2 \times 1.35 M_{\odot}$ ;

M:  $2 \times 1.5 M_{\odot}$ ;

H:  $2 \times 1.6 M_{\odot}$

Total baryonic masses:  
(2.90, 3.28, 3.54)  $M_{\odot}$

TOV:  $2.56 M_{\odot}$ ;

uniform rot.:  $3.05 M_{\odot}$ ;

diff. rot.: no formal limit

-> see also

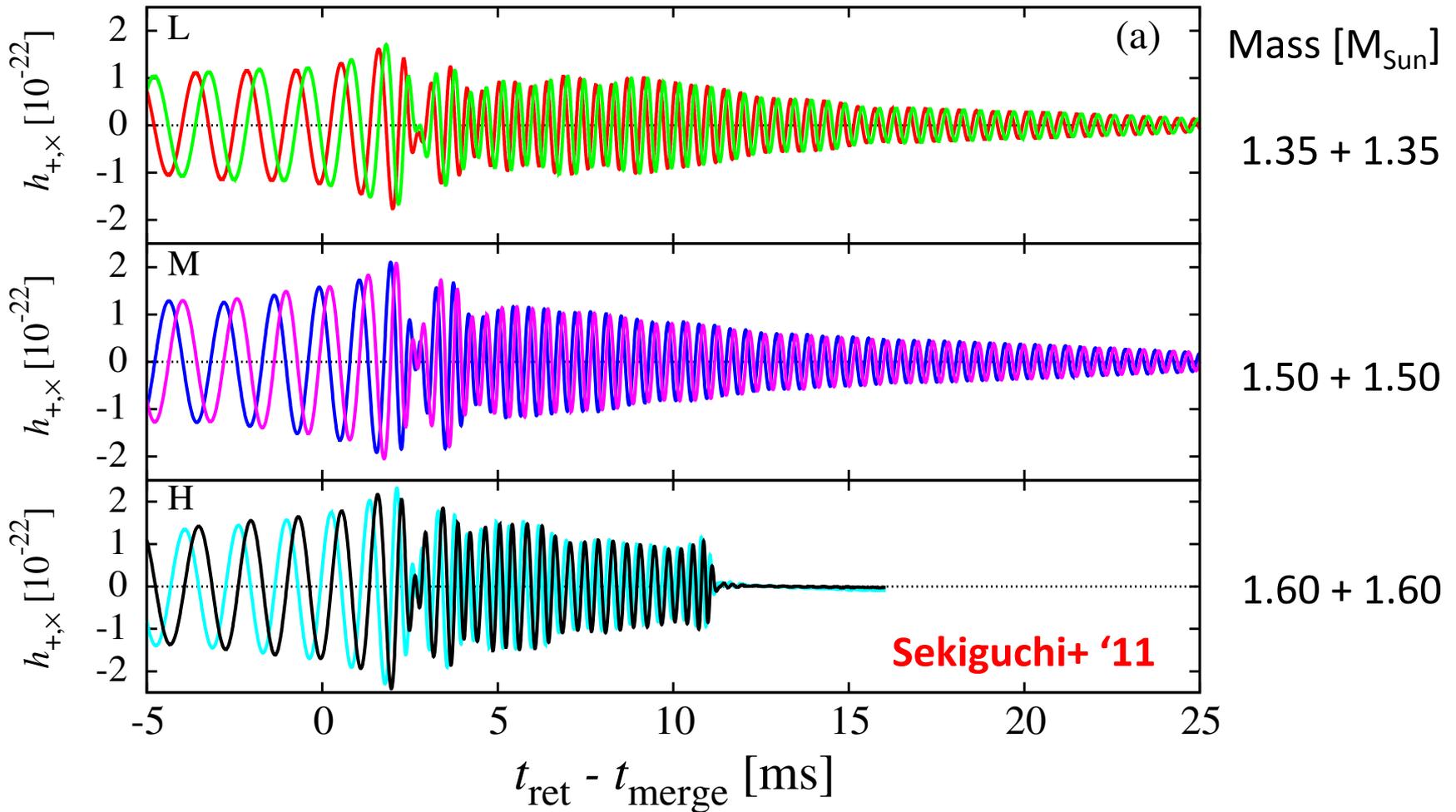
Bauswein+10,12,13

**HMNS**: support by differential rotation, only small thermal contribution.

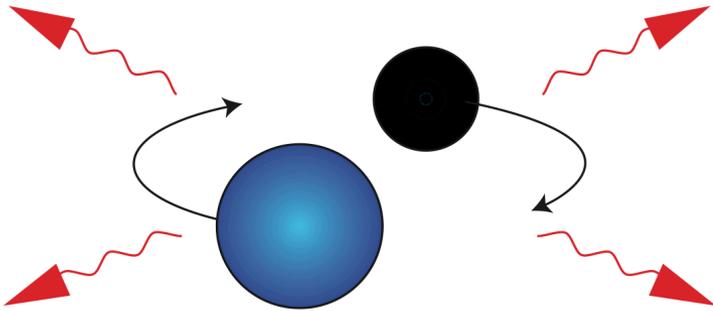
**Secular evolution**: governed by energy loss to GWs, neutrinos, and angular momentum redistribution by 3D torques / magnetorotational instability.

# NSNS Postmerger Evolution

Sekiguchi+11a



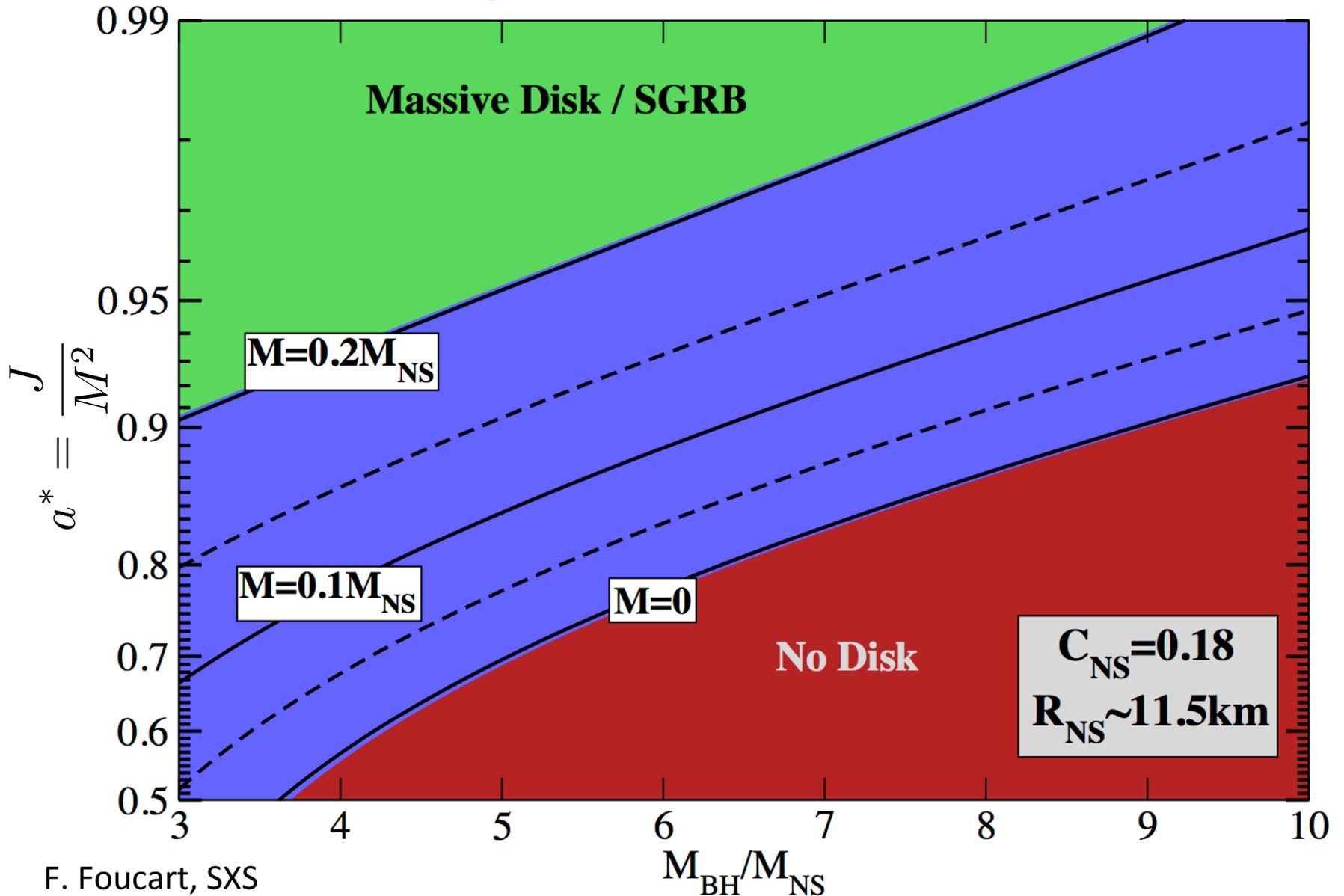
# BHNS Merger Scenarios



$$a^* = \frac{J}{M^2}$$

- Tidal disruption or complete “swallow”.
- The greater BH spin  $a^*$ , the stronger disruption.
- The larger  $M_{\text{BH}}$ , the more spin required for disruption.
- Typical BH/NS mass-ratio uncertain.  
Best guess: 7/1 – 10/10.

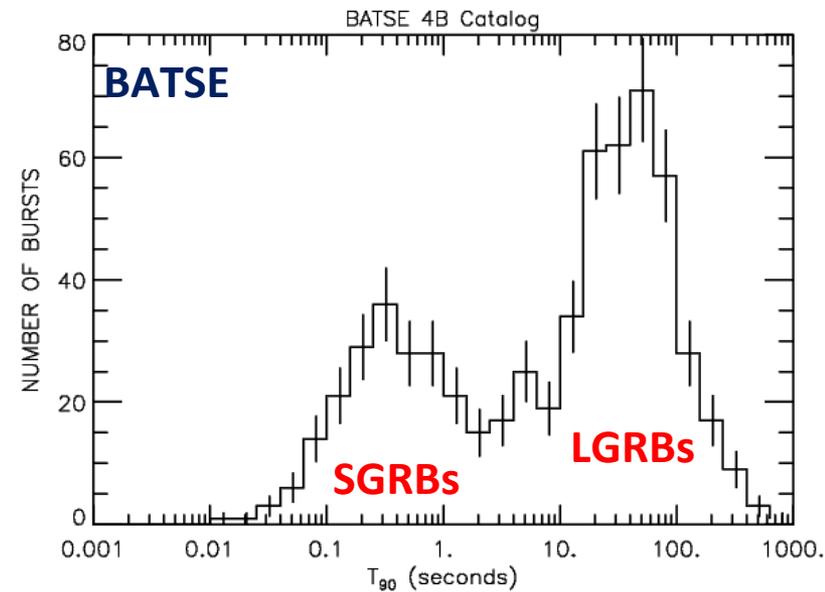
# BHNS Merger Scenarios: Remnant



# Gamma-Ray Bursts

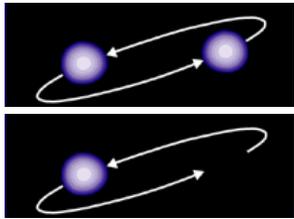
[Reviews: e.g. Woosley & Bloom '06, Piran '05, Meszaros '05]

- Two general groups of GRBs:  
Long and Short
- Favored model:  
Beamed Ultrarelativistic outflow emitting  $\gamma$ -rays.

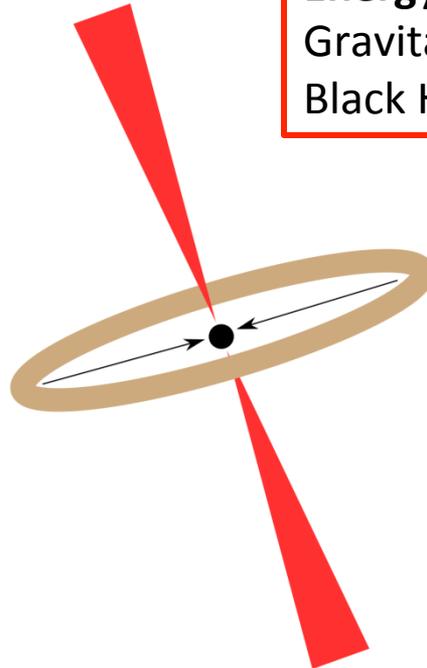


## Simplistic Engine Picture:

NS-NS / NS-BH merger



Massive H/He-poor Star



Energy sources:

Gravitational energy (accretion)  
Black Hole/NS spin energy.

Disk Mass:  
 $\sim 0.1-0.2 M_{\text{Sun}}$



**SGRB**

Disk Mass:  
 $\sim 1 M_{\text{Sun}}$



**LGRB**

Mediating Processes:

Neutrino Pair Annihilation  
Magnetohydrodynamics

# Nuclear Astrophysics with Binary Mergers

**Nuclear Equation of State (EOS)**

**Crust Physics & Superfluidity (SF)**

**Neutrinos/Neutrino Interactions**

**Nuclear Reactions & Opacities**

Inspiral

Late Inspiral

Merger

Postmerger

Late Time  
( $t > \sim 1s$ )



**GRB?**

Inspiral

Late Inspiral

Merger/Disruption

Postmerger

**Crust/SF**

**EOS**

**EOS**

**EOS**

**EOS**

**Neutrinos**

**Neutrinos**

**Neutrinos**

**Neutrinos**

**Nuclear**

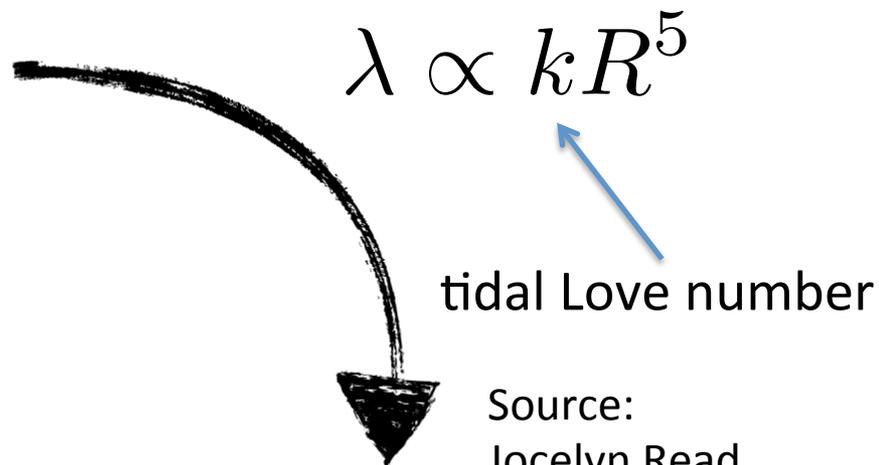
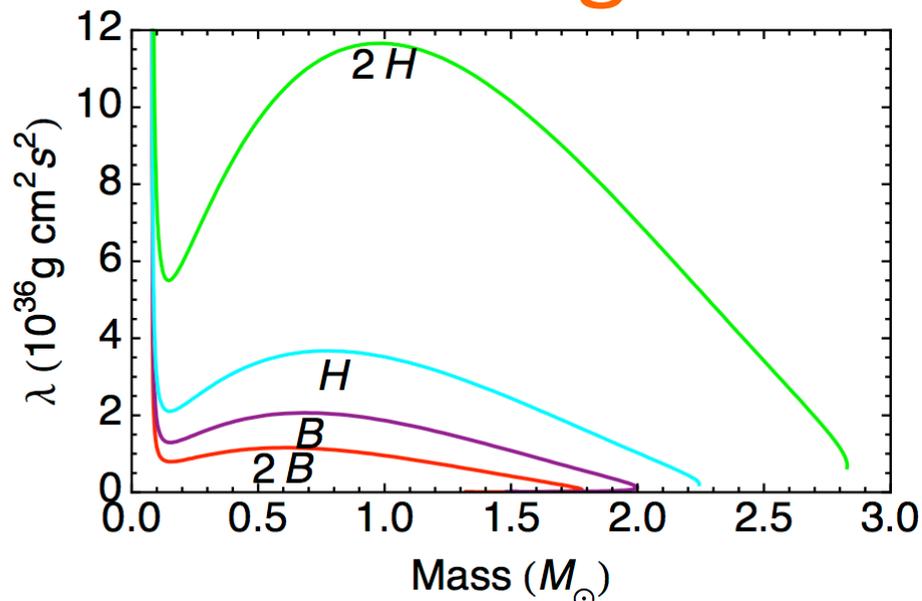
**Nuclear**

**Nuclear**

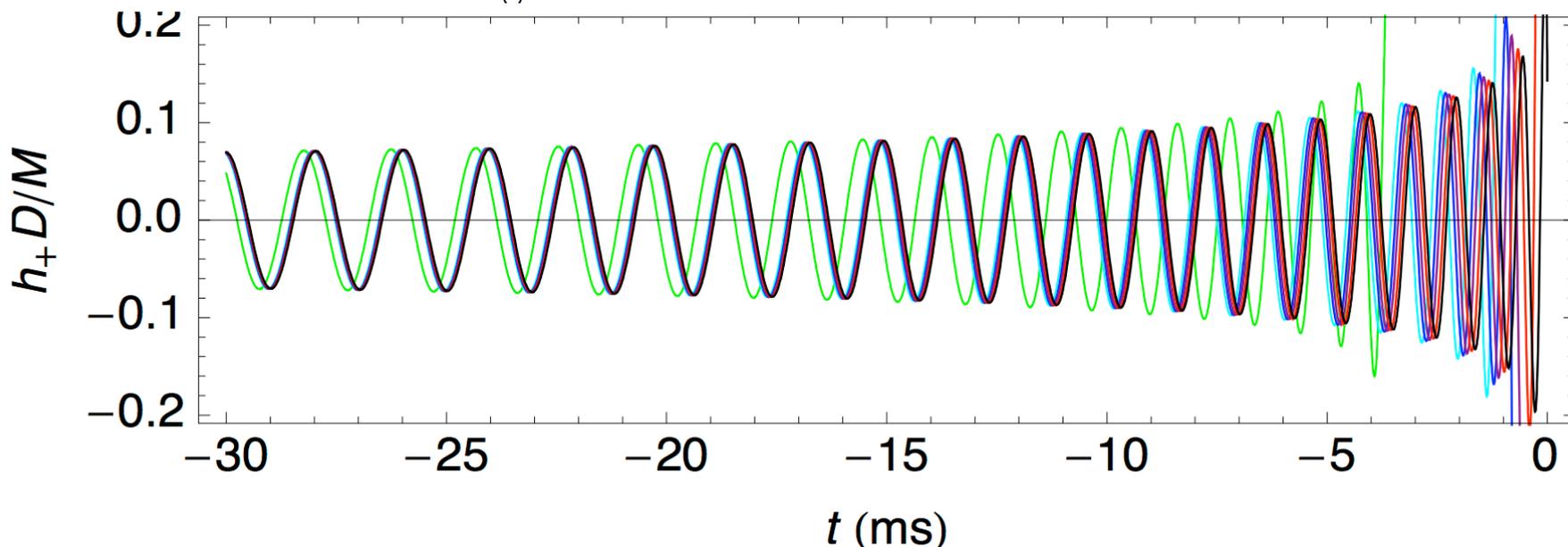
# NSNS Mergers and the Nuclear EOS

- LIGO will measure  $M_{\text{chirp}}$ , mass ratio.
- Late inspiral: Tidal deformation of the NSs  
-> EOS-dependent effect on phase evolution of the waveform
- Merger / postmerger:
  - Survival of the HMNS
  - Oscillation frequencies of the postmerger HMNS.

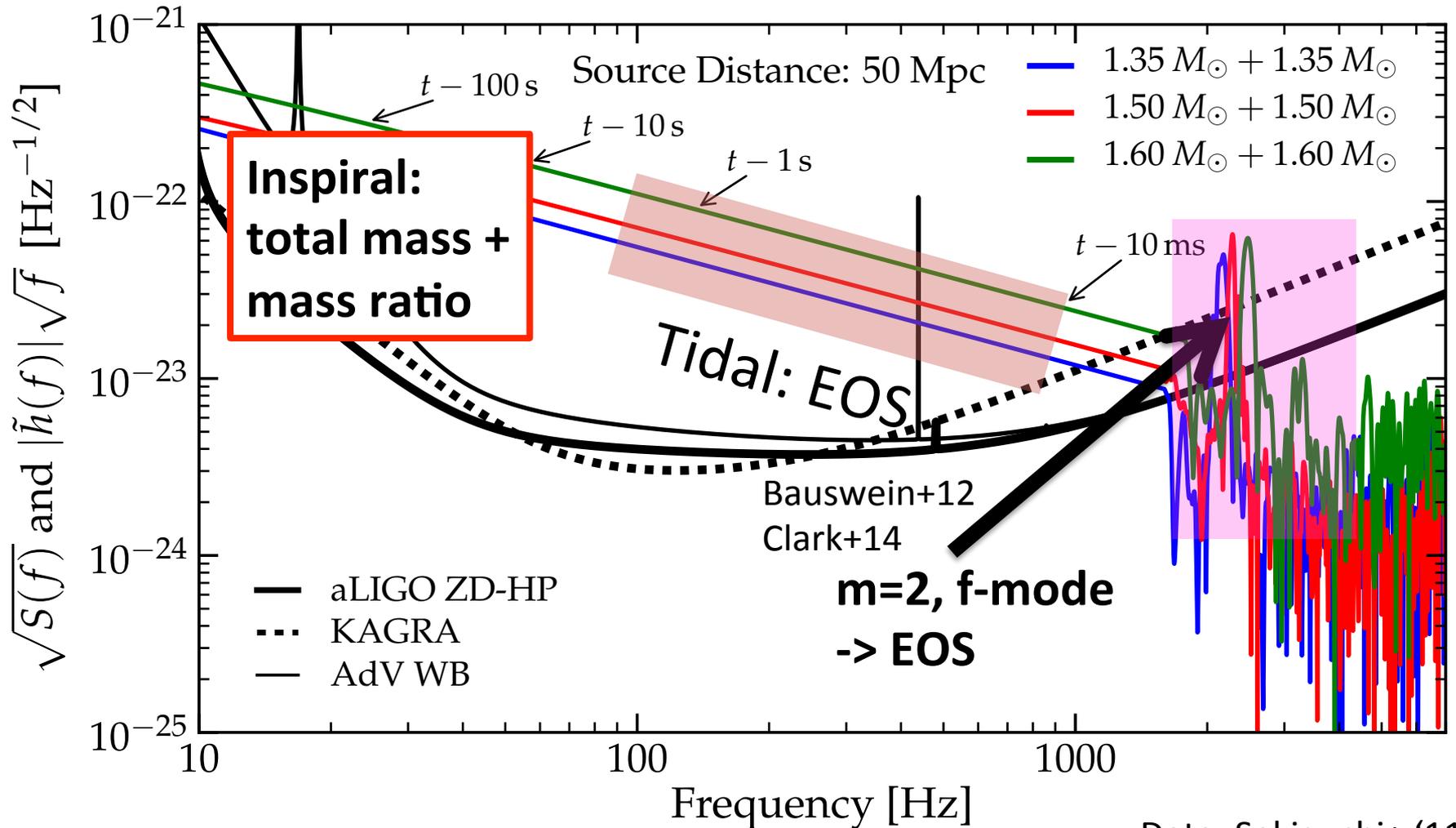
# NSNS Mergers and the Nuclear EOS



Source:  
Jocelyn Read  
CSU Fullerton



# NSNS Mergers and the Nuclear EOS



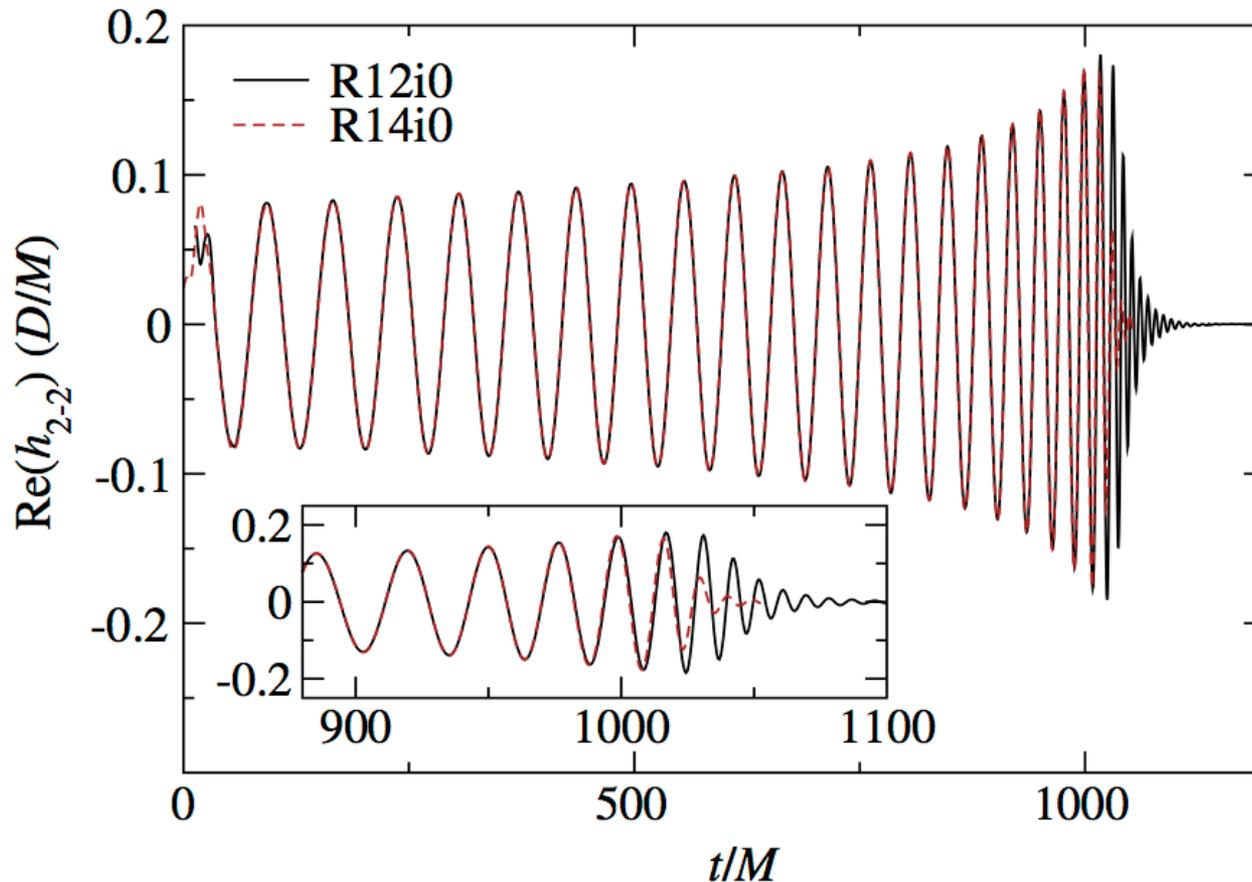
Data: Sekiguchi+ '11  
Figure: Sarah Gossan

Late inspiral + merger:  $E_{\text{GW}} \sim 0.1 M_{\odot} c^2$

Best guess:  $\sim 0.5$  event/year @50 Mpc at design sensitivity

# BHNS Mergers and the Nuclear EOS

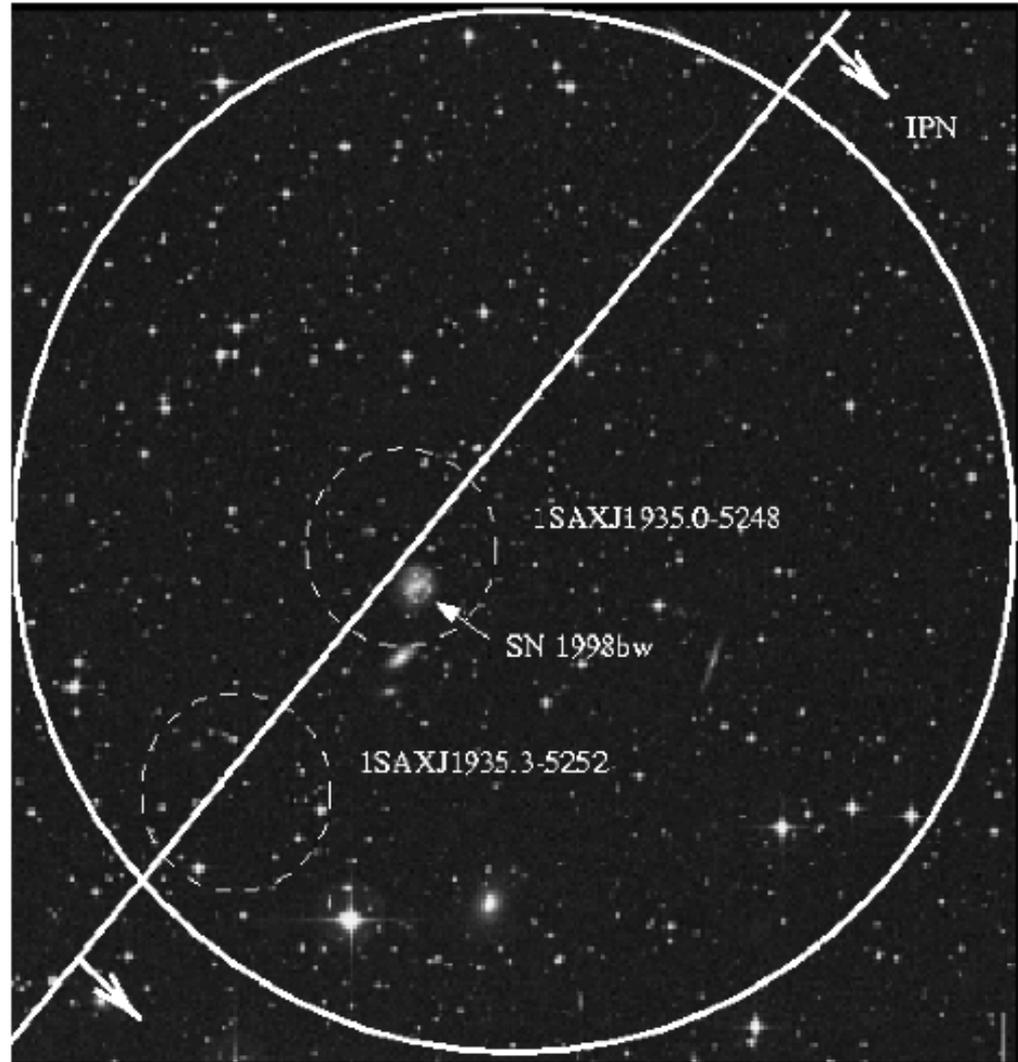
- LIGO will measure  $M_{\text{chirp}}$ , mass ratio.
- Tidal deformations during late inspiral very small.
- If NS disrupted, cut-off frequency of GW signal sensitive to NS radius.

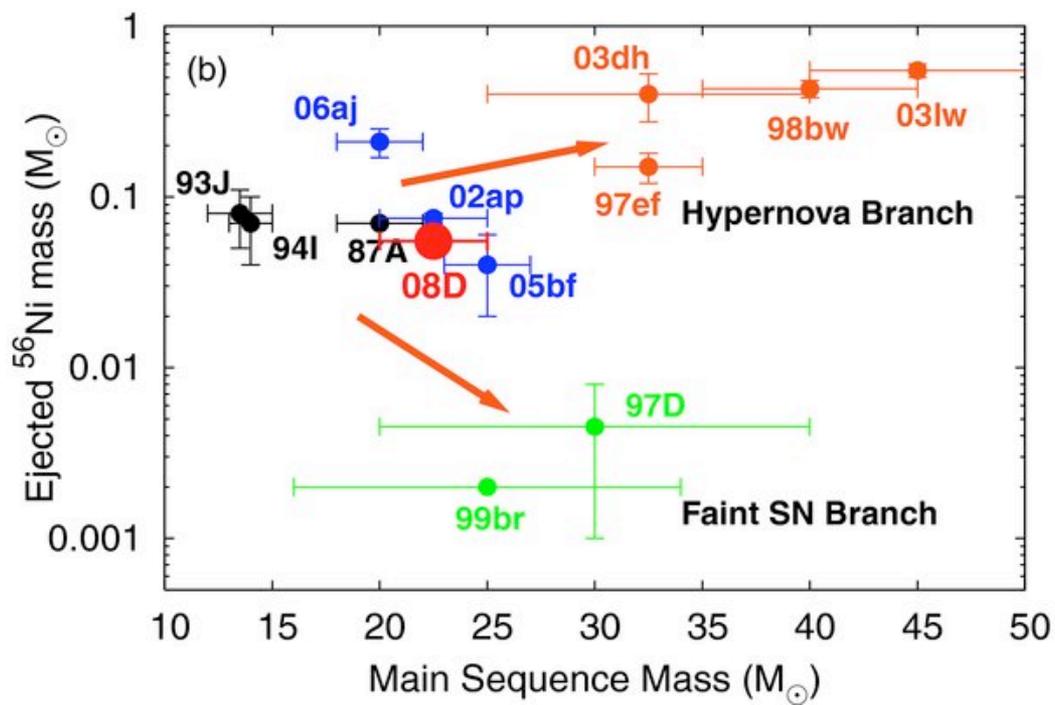
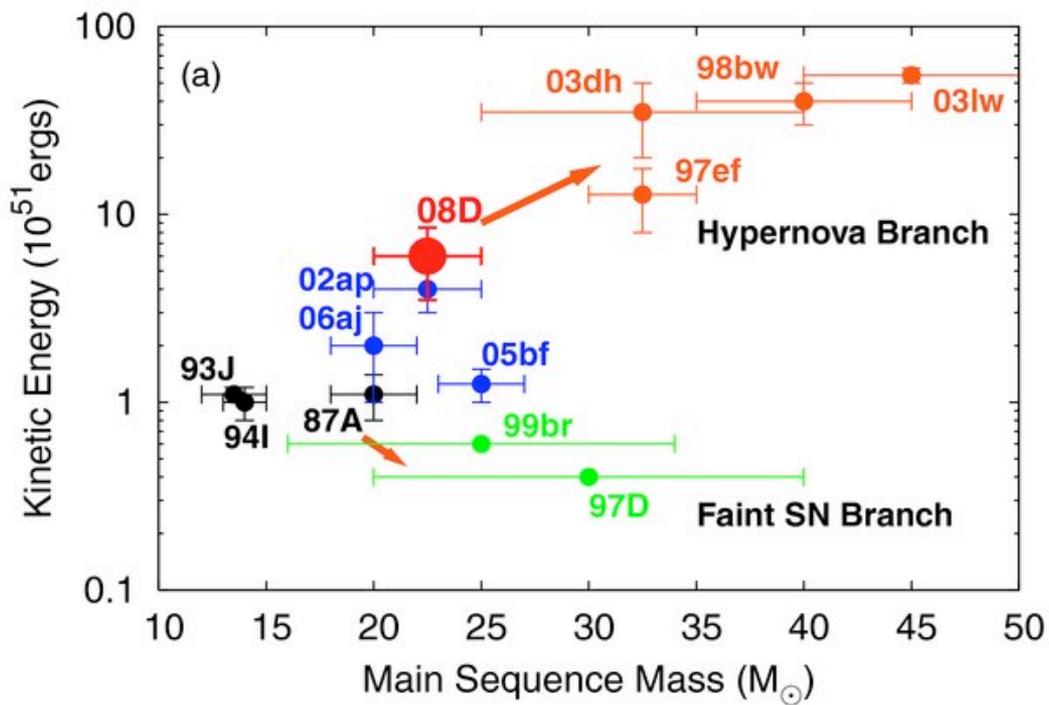


# Extreme Core-Collapse Supernovae and the Long-GRB – CCSN Relationship

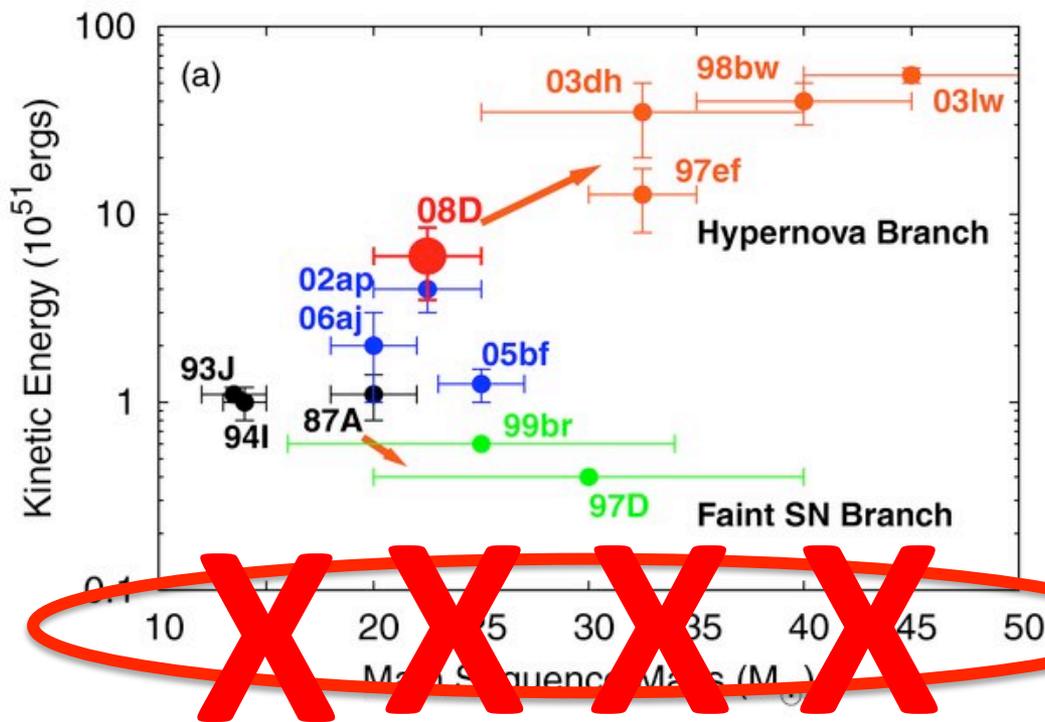
# Extreme Core-Collapse Supernovae

- Type Ic-bl (“broad lined”) core-collapse supernovae
- Relativistic outflows, hyperenergetic:  
 $\sim 10^{52}$  erg = 10 B
- $\sim 1\%$  of all CCSNe
- $\sim 10\%$  of Type Ic-bl CCSNe associated with a long GRB.
- All CCSNe associated with GRBs are Type Ic-bl.  
11 GRB-CCSNe known.



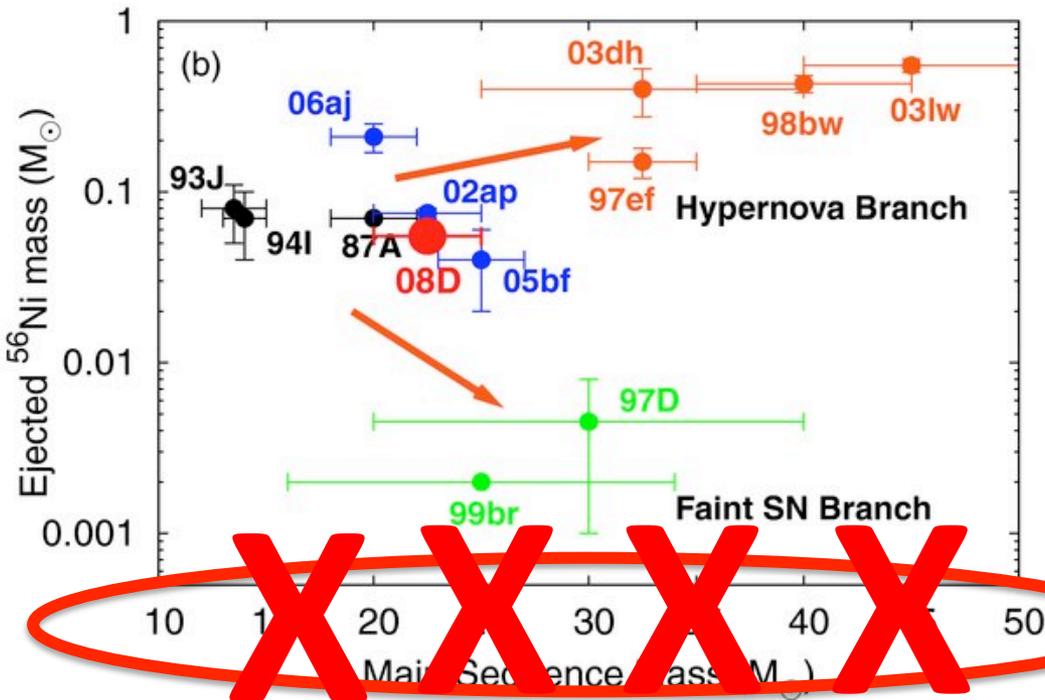


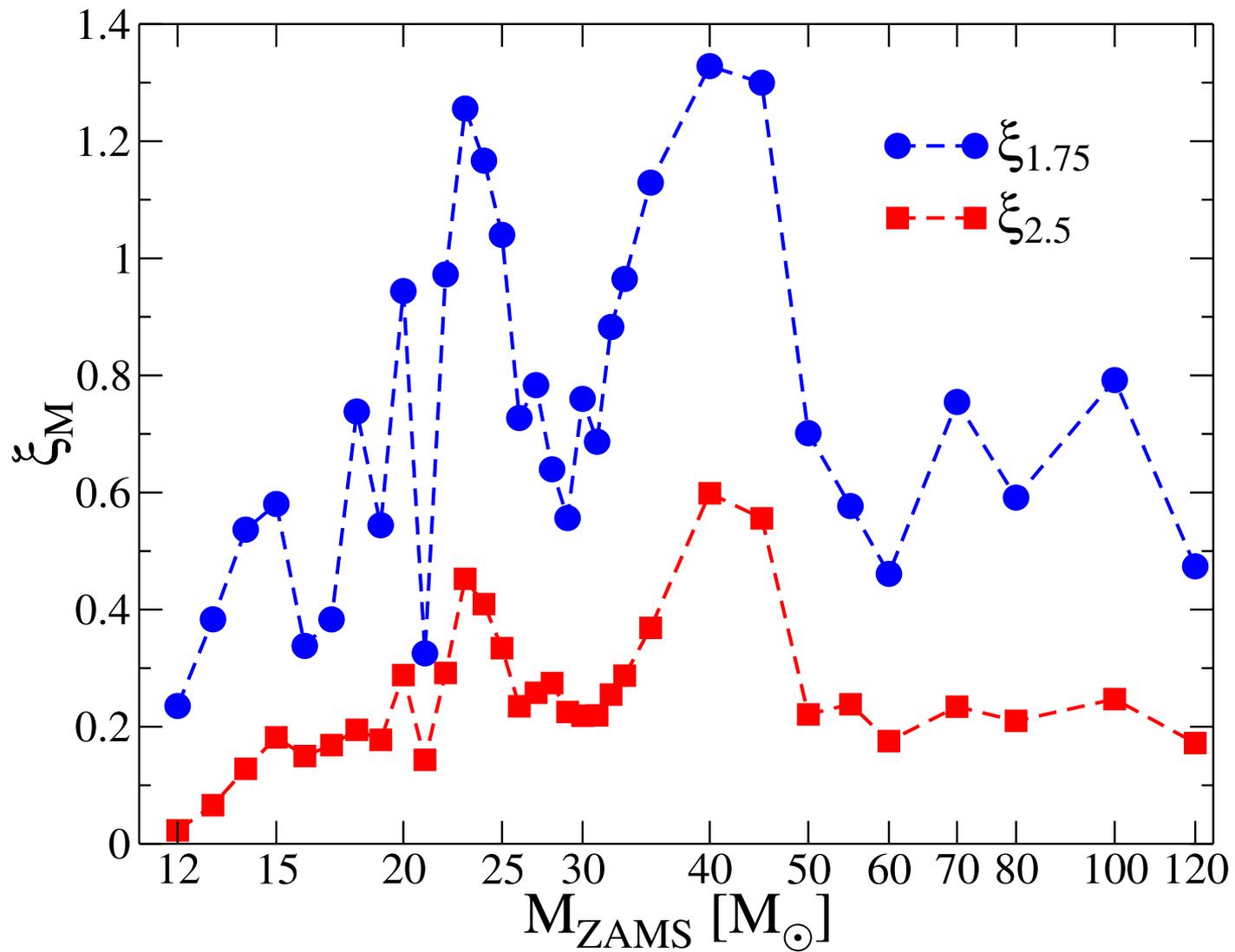
largely  
made up!



Ignores  
fact that ~all  
massive stars  
in binaries

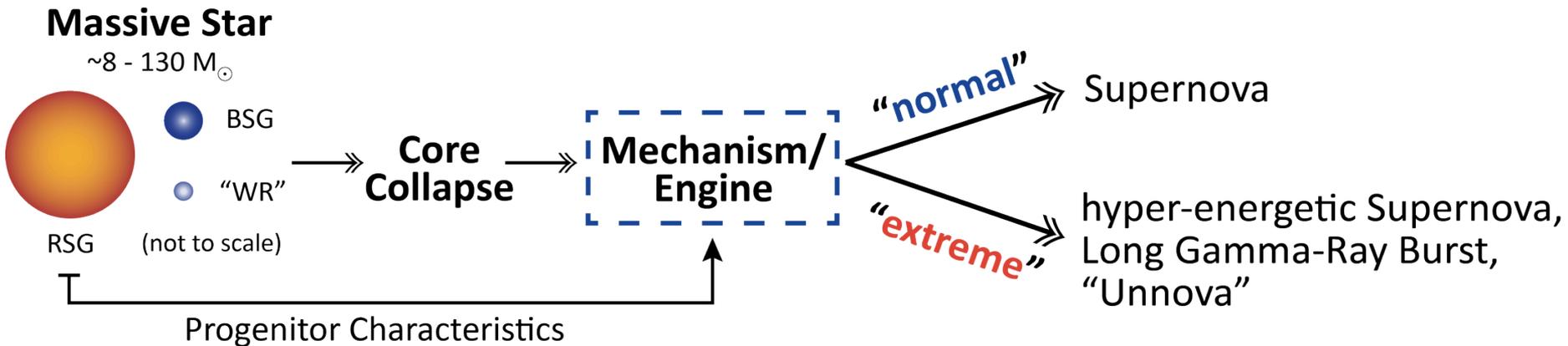
largely  
made up!





$$\xi_{2.5} = \frac{2.5 M_{\odot}}{R(M_{\text{bary}} = 2.5 M_{\odot})} \Big|_{t=t_{\text{bounce}}}$$

# Extreme Core-Collapse Supernovae

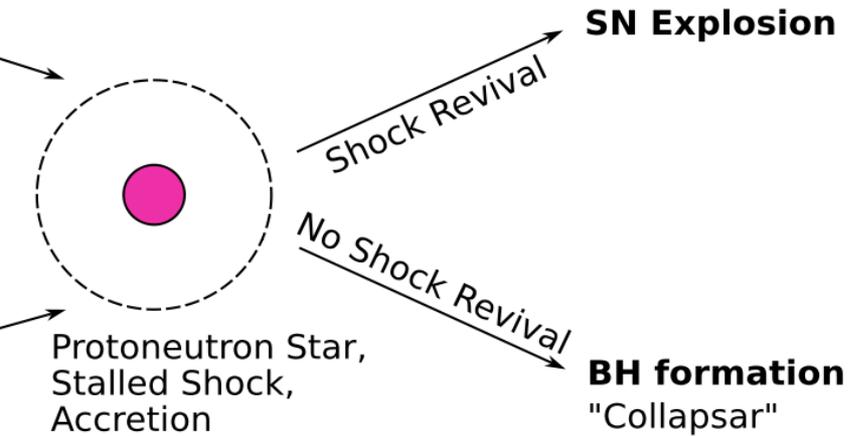


- What powers a hypernova / a long GRB?  
Neutrino-driven CCSN mechanism is inefficient ( $\eta \sim 10\%$ );  
difficult to obtain 1 B!

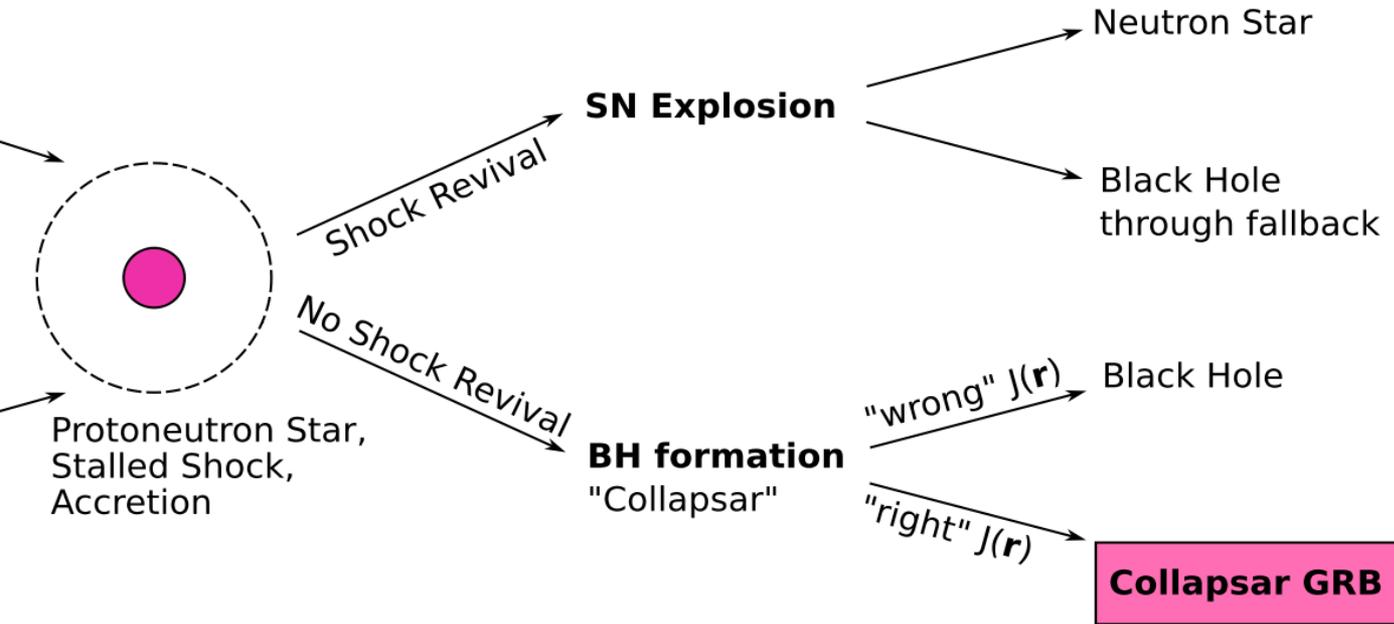
## Possibility:

Rapid rotation + strong magnetic fields  
-> energetic collimated outflows

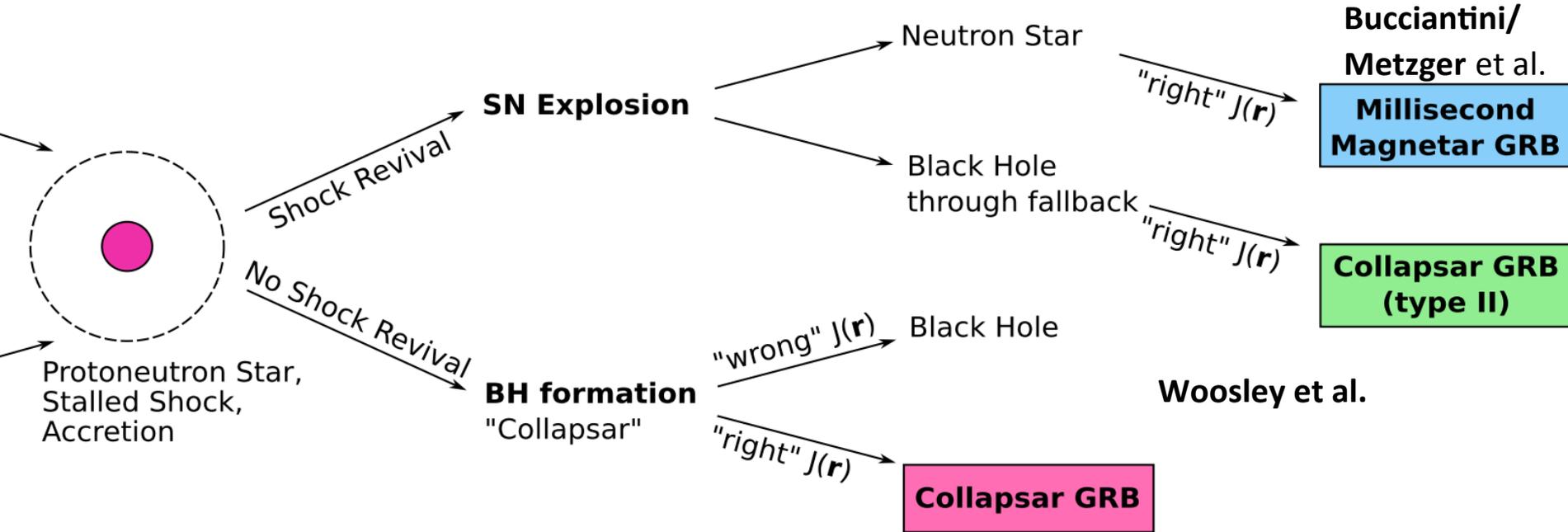
# The CCSN – Long Gamma-Ray Burst Connection



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# The CCSN – Long Gamma-Ray Burst Connection



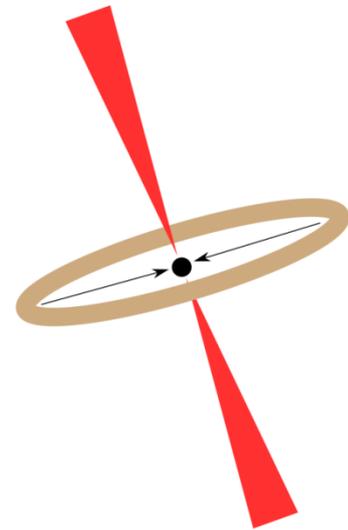
## (1) Millisecond Proto-Magnetar Model

-> GRB driven by spindown; requires  $O(\text{ms})$  initial period. Subsequent to a successful CCSN explosion.

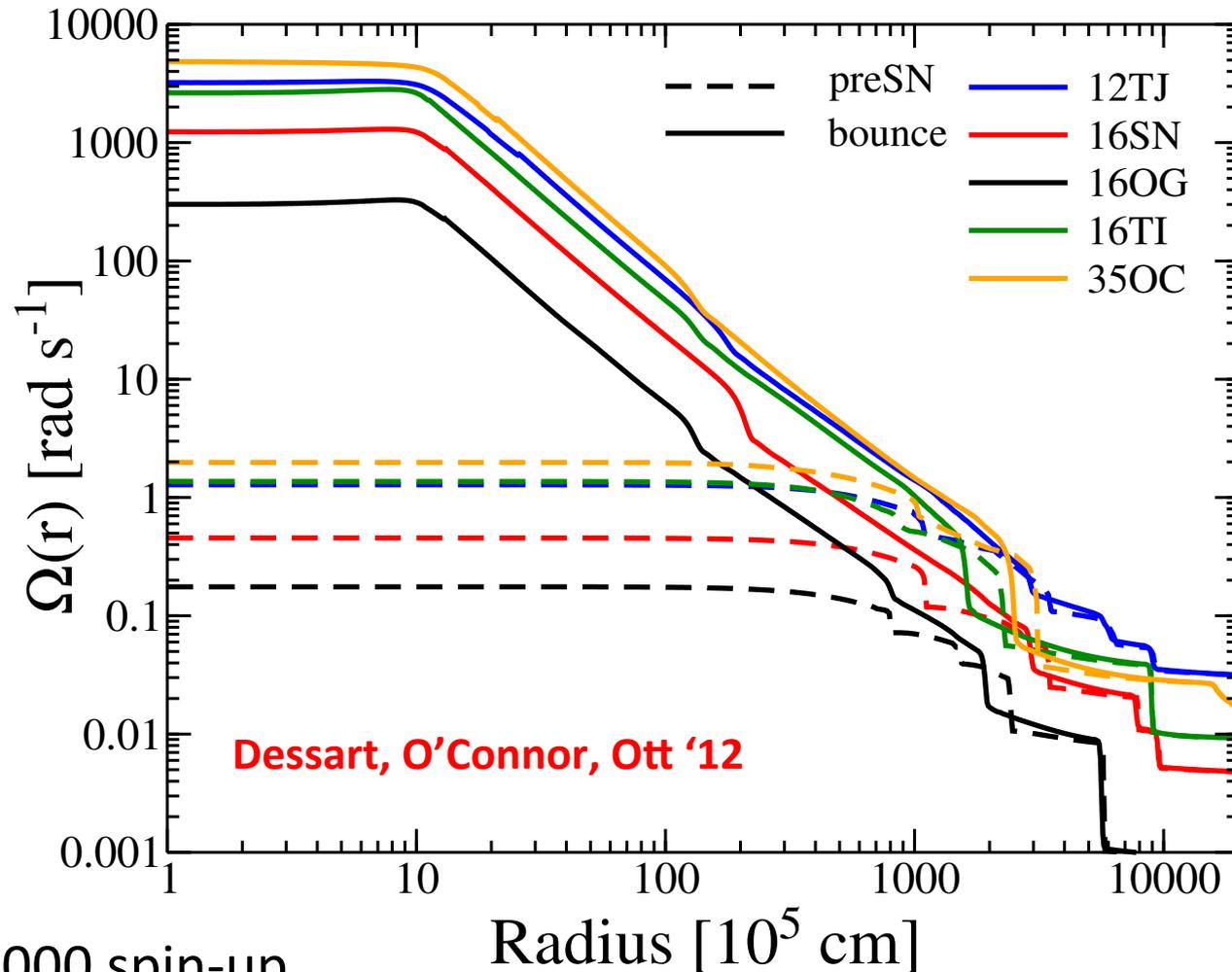
## (2) Collapsar Model

-> Requires accretion disk near ISCO;

$$j = \Omega r^2 = 10^{16} - 10^{17} \text{ cm}^2/\text{s}.$$



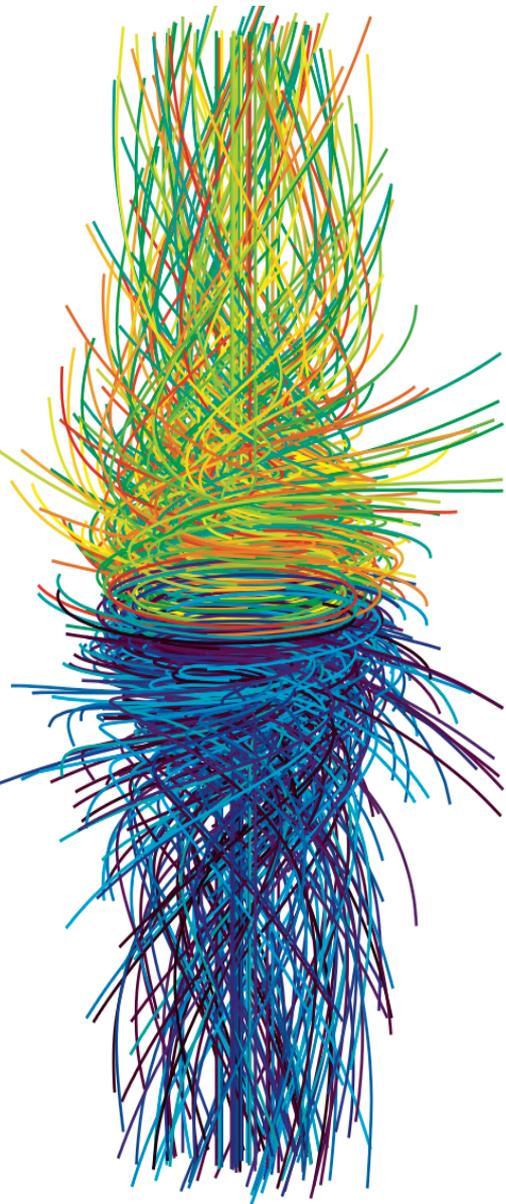
# “Magnetorotational Explosions”



- Core: x 1000 spin-up
- Differential rotation -> reservoir of free energy.
- Spin energy tapped by **magnetorotational instability** (MRI)?

# Magnetorotational Mechanism

[LeBlanc & Wilson '70, Bisnovatyi-Kogan '70,  
Burrows+ '07, Takiwaki & Kotake '11, Winteler+ 12]



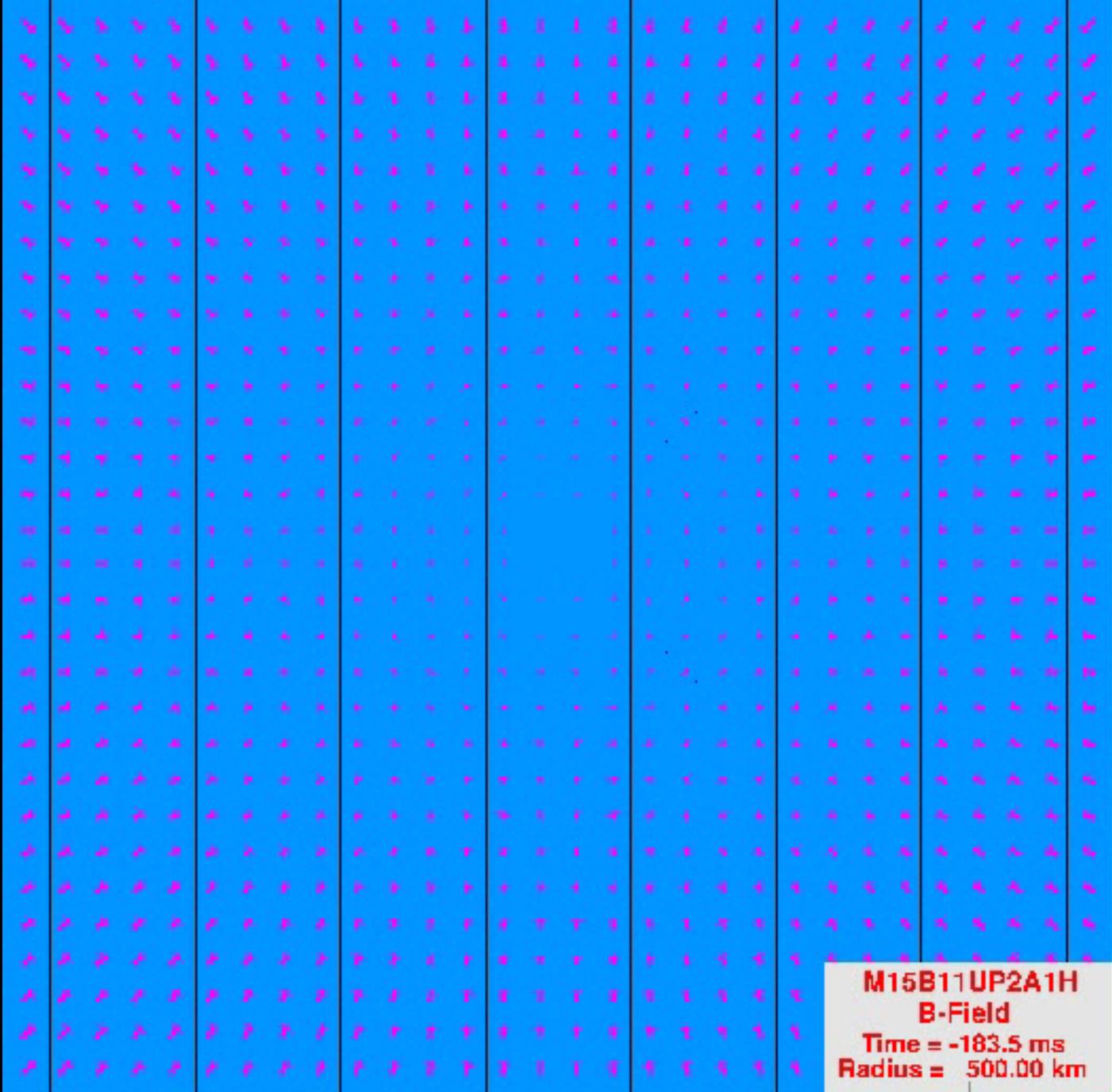
Burrows+'07

**Rapid Rotation + B-field amplification**  
(need magnetorotational instability [MRI];  
difficult to resolve in stellar cores)

**2D: Energetic bipolar explosions.**

Results in ms-period proto-magnetar.  
GRB connection?

**Caveat: Need high core spin; only in  
very few progenitor stars?**



**M15B11UP2A1H**  
**B-Field**  
 Time = -183.5 ms  
 Radius = 500.00 km

Burrows+'07  
 ( $10^{11}$  G  
 seed field)

# 3D Dynamics of Magnetorotational Explosions

New, full 3D GRMHD simulations. **Mösta+ 2014**, ApJL.  
Initial configuration as in Takiwaki+11,  $10^{12}$  G seed field.

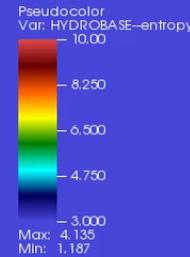
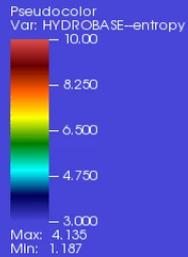


← 2000 km →

← 2000 km →

$t = -3.00$  ms

$t = -3.00$  ms



Octant Symmetry (no odd modes)

Full 3D

# What is happening here?

Mösta+14, ApJL

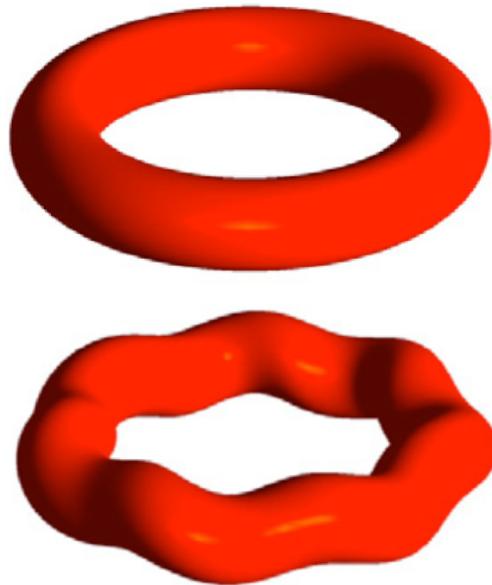
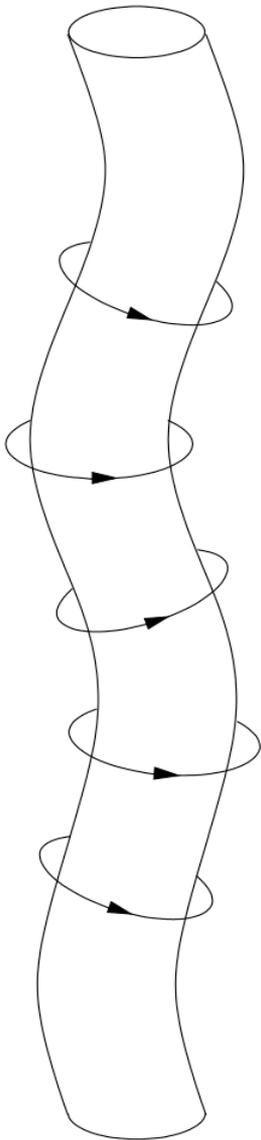


Philipp Mösta

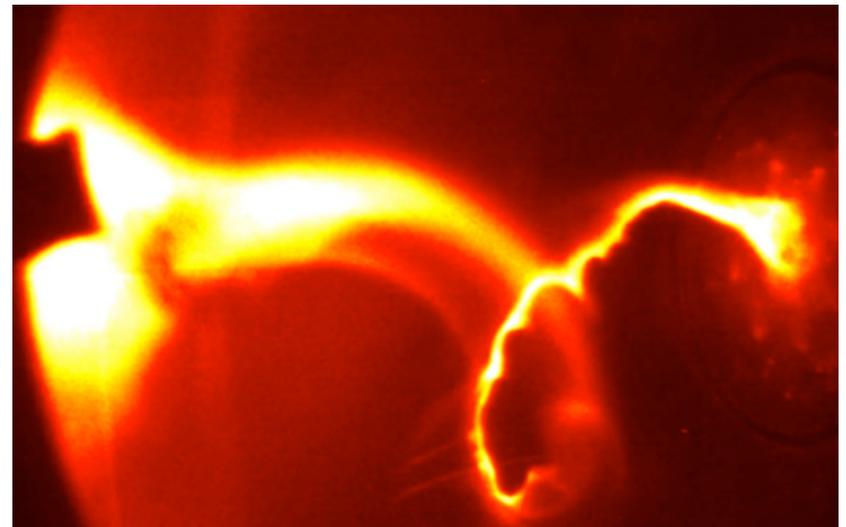


Sherwood Richers

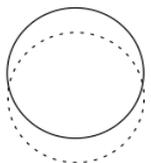
- B-field near proto-NS:  $B_{\text{tor}} \gg B_z$
- Unstable to MHD screw-pinch kink instability.
- Similar to situation in Tokamak fusion reactors!



Sarff+13



Credit: Moser & Bellan, Caltech



Braithwaite+ '06



$$\beta = \frac{P_{\text{gas}}}{P_{\text{mag}}}$$

$$\dagger = -4.95 \text{ ms}$$

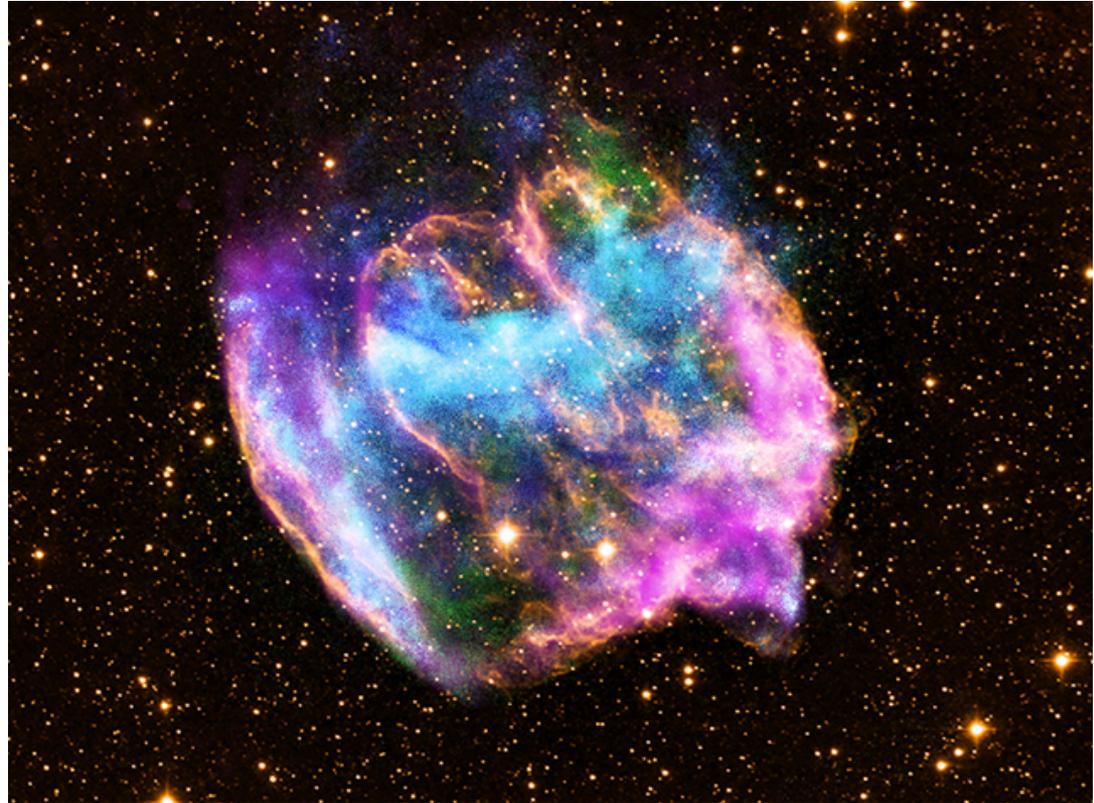
**Mösta+ 2014**

**ApJL**



# Consequence?

- If explosion fails to develop:  
BH formation
- ms Proto-magnetar scenario  
for GRBs might not work.
- Type Ic-blbs might be  
coming from collapsars.



SNR W49B; harboring a black hole? (Lopez+13)

Image credit: Composite X/IR/Radio image NASA/CXC/MIT/Lopez et al./  
Palomar/SF/NRAO/VLA

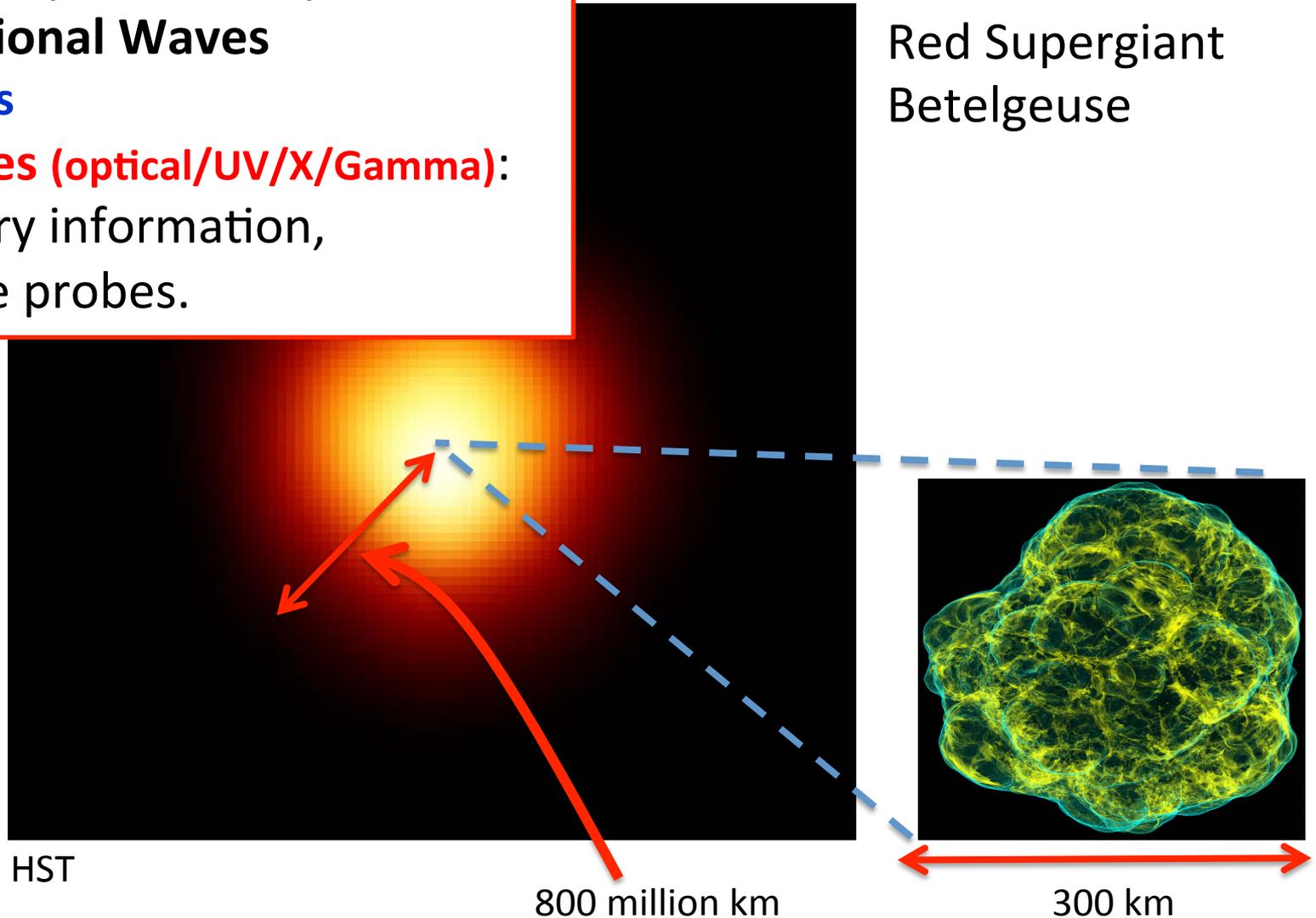
# Gravitational Waves from Core-Collapse Supernovae

# Observing the Heart of a Supernova

Probes of Supernova Physics:

- **Gravitational Waves**
- **Neutrinos**
- **EM waves (optical/UV/X/Gamma):**  
secondary information,  
late-time probes.

Red Supergiant  
Betelgeuse



# Gravitational-Waves from Core-Collapse Supernovae

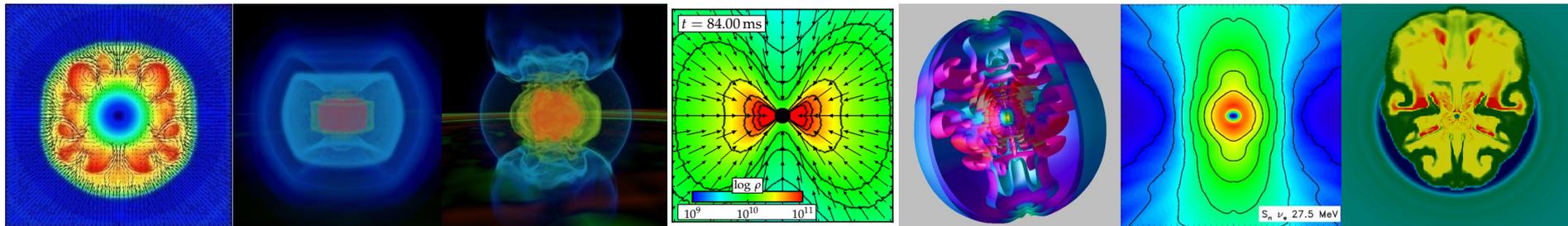
Recent reviews: Ott 09, Kotake 11, Fryer & New 11

Need:

$$h_{jk}^{TT}(t, \vec{x}) = \left[ \frac{2}{c^4} \frac{G}{|\vec{x}|} \ddot{I}_{jk}(t - \frac{|\vec{x}|}{c}) \right]^{TT} \longrightarrow \text{accelerated aspherical (quadrupole) mass-energy motions}$$

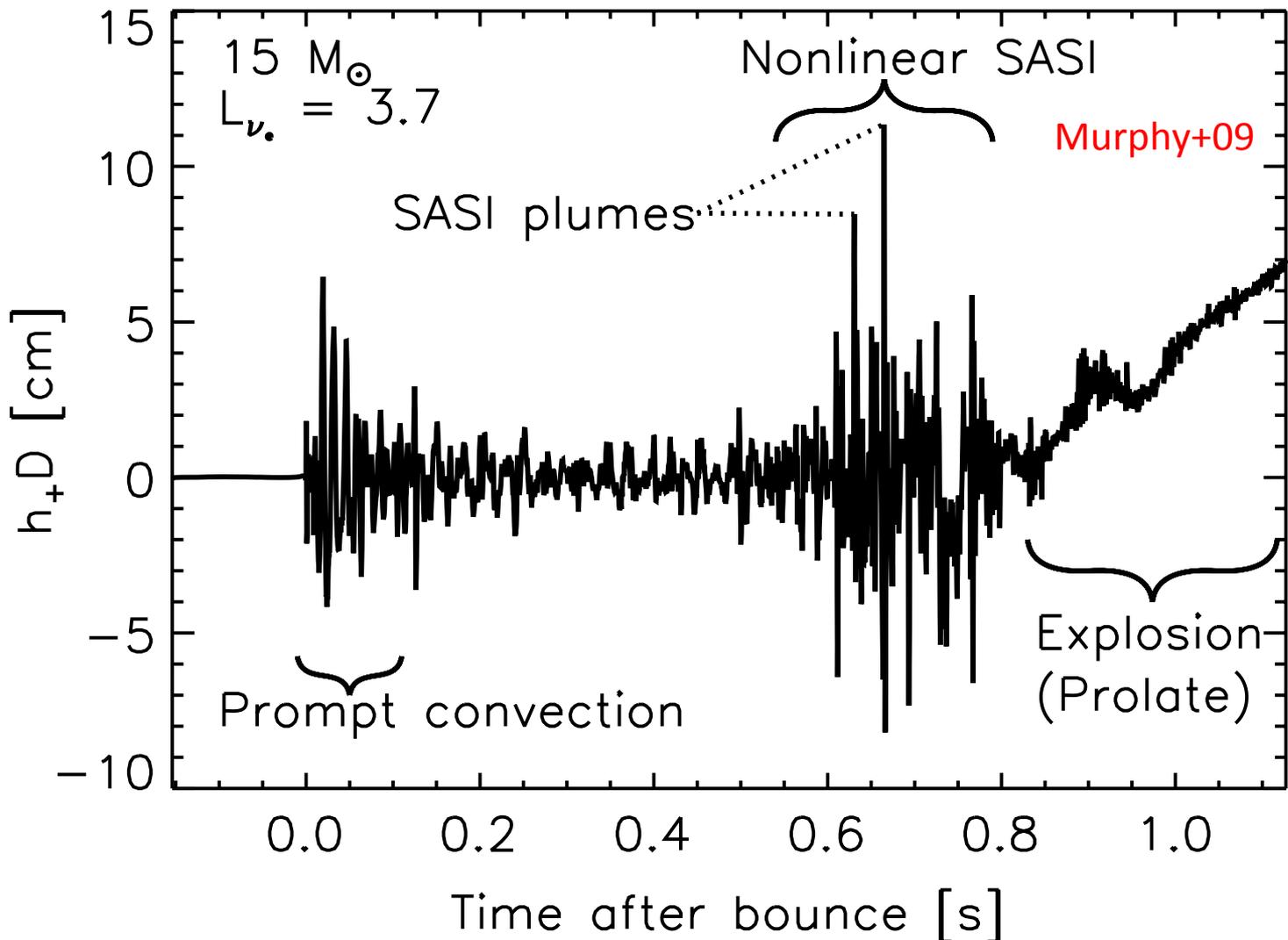
## Candidate Emission Processes:

- ❖ Turbulent convection
- ❖ Rotating collapse & bounce
- ❖ 3D MHD/HD instabilities
- ❖ Aspherical mass-energy outflows



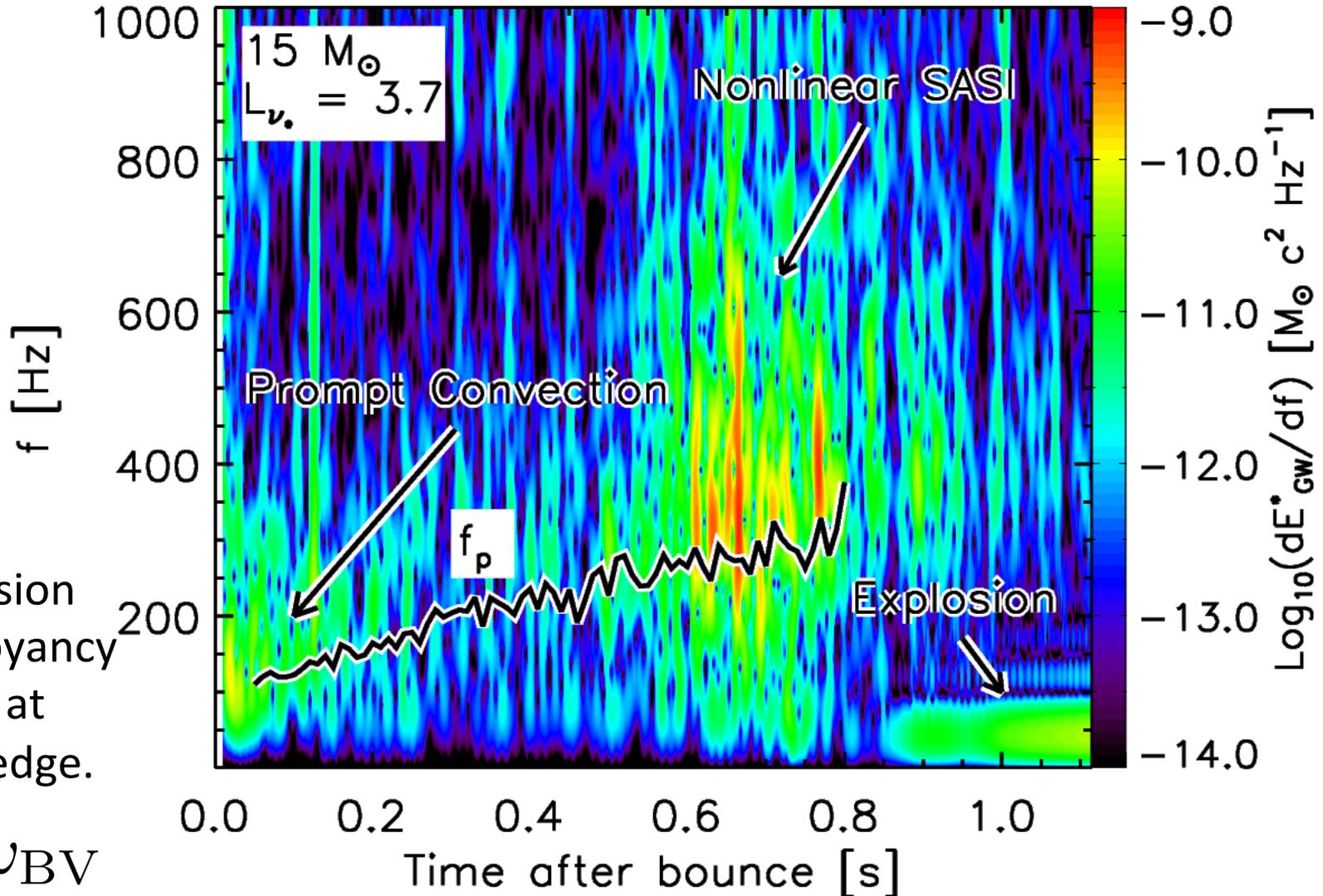
# GWs from Convection & Standing Accretion Shock Instability

Recent work: Murphy+09, Kotake+09, 11, Yakunin+10, E. Müller+12, B.Müller+13



# Time-Frequency Analysis of GWs

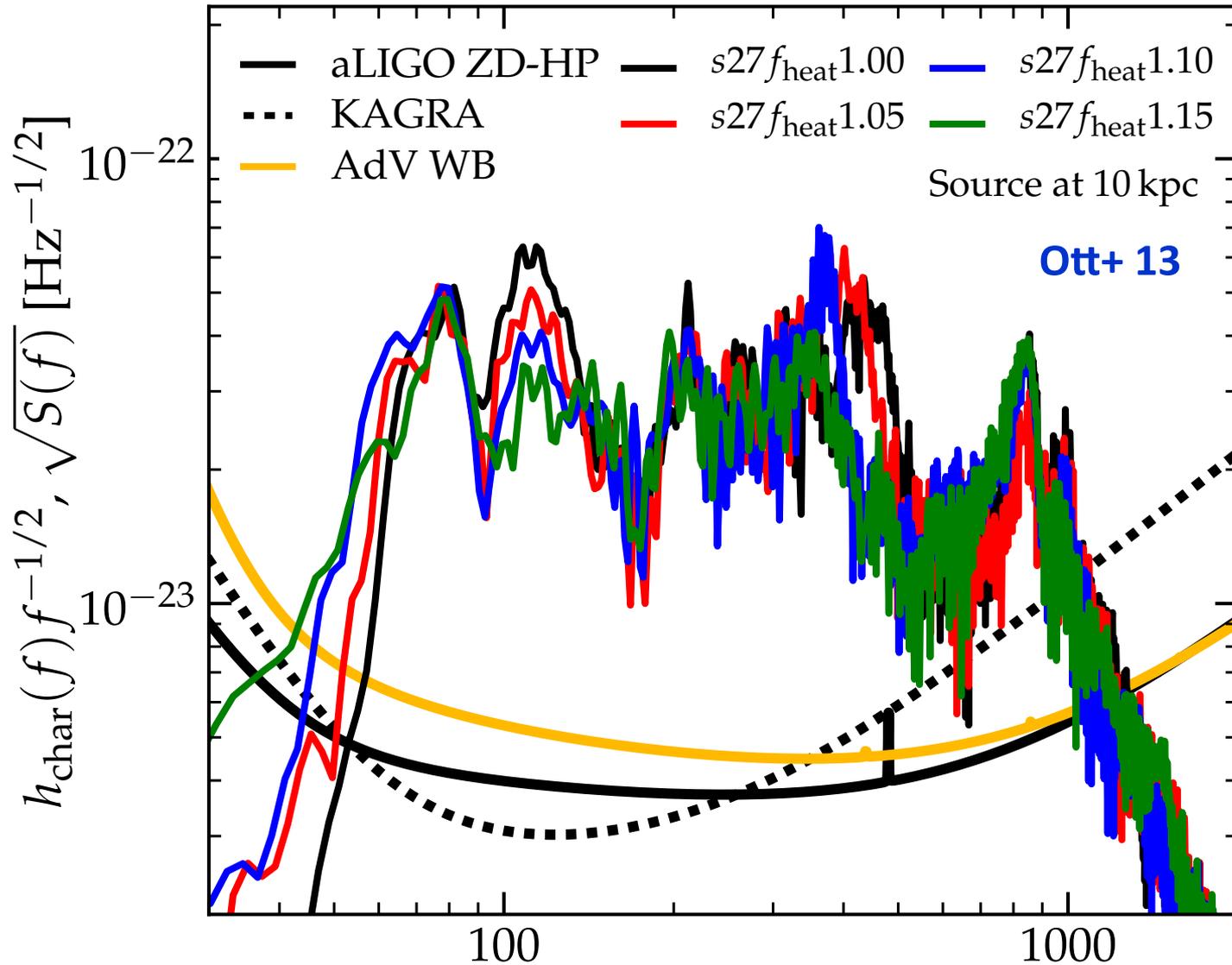
Murphy, Ott, Burrows 09, see also B. Müller+13



Peak emission traces buoyancy frequency at proto-NS edge.

$$f_p \sim \frac{\omega_{\text{BV}}}{2\pi} \quad (\text{buoyancy frequency})$$

# Detectability?

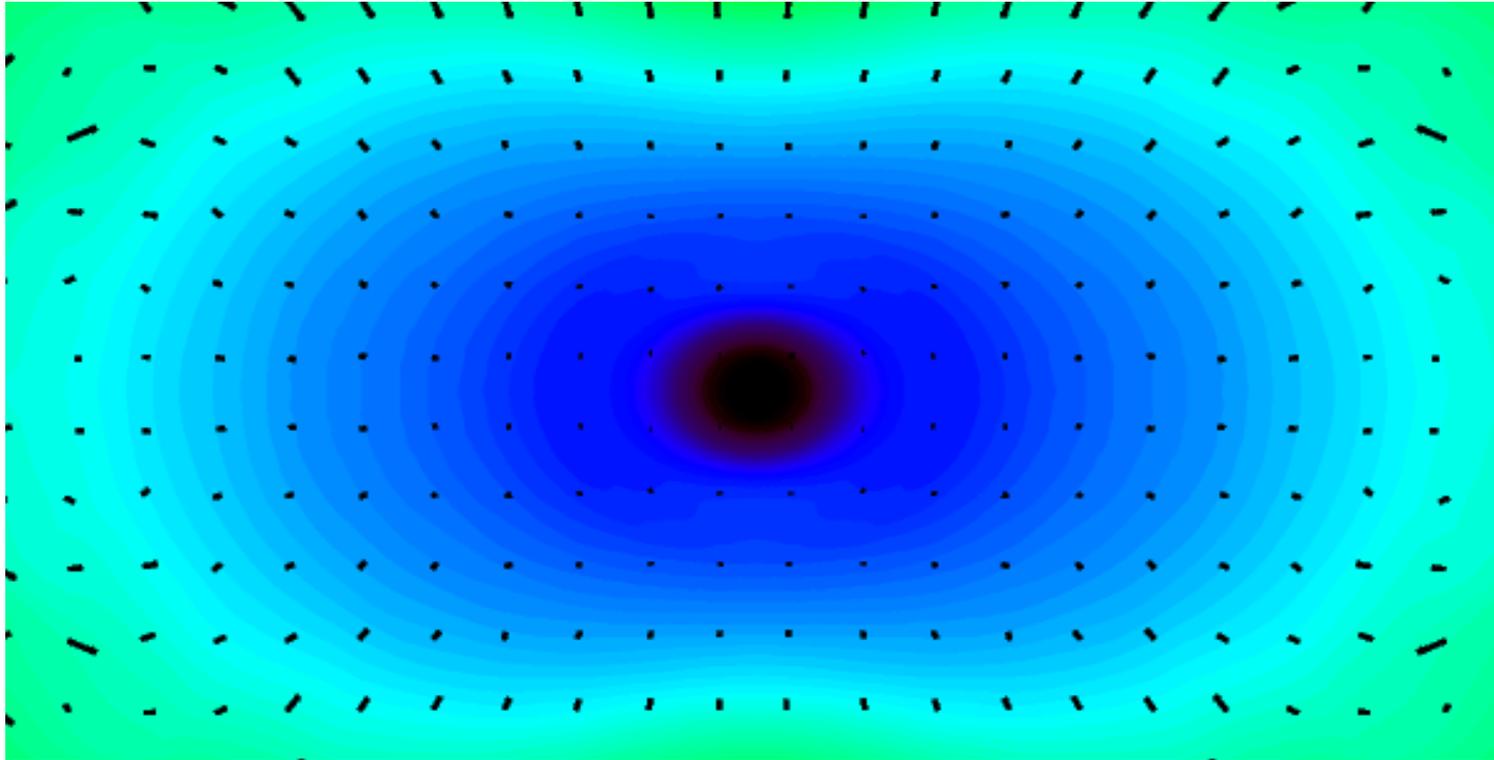


$$h_{\text{char}}(f) = \sqrt{\frac{2}{\pi^2} \frac{G}{c^3} \frac{1}{D^2} \frac{dE_{\text{GW}}(f)}{df}}$$

Frequency [Hz]

# GWs from Rotating Collapse & Bounce

Recent work: Dimmelmeier+08, Scheidegger+10, Ott+12, Abdikamalov+13



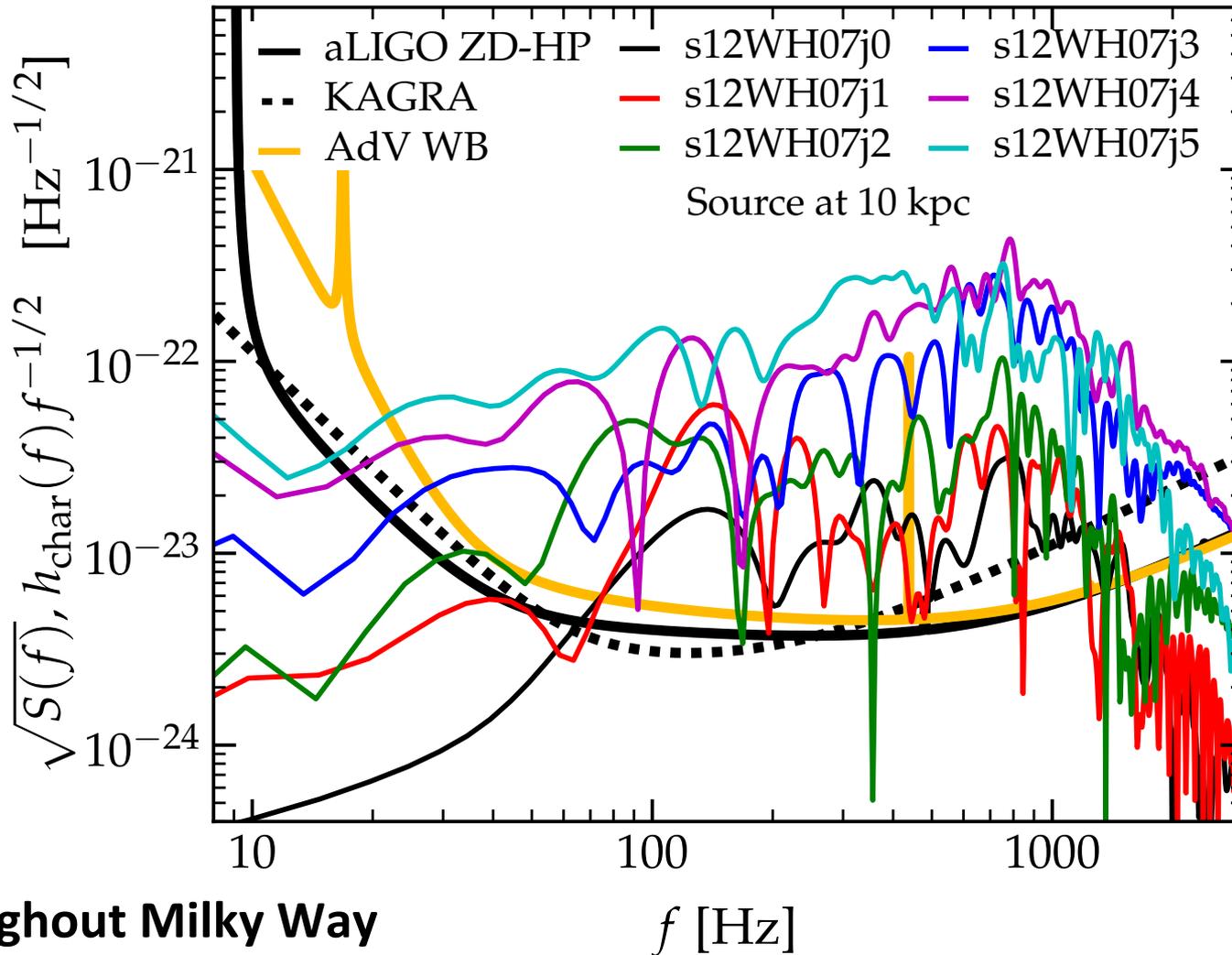
- **Axisymmetric: ONLY  $h_+$**
- Simplest GW emission process: **Rotation** + mass of the inner core + **gravity** + **stiffening of nuclear EOS**
- Strong signals for rapid rotation (-> millisecond proto-NS).

# Can we observe these waves?

Ott+ 12, PRD

**Gravitational Waves**

$$E_{GW} \lesssim 10^{-8} M_{\odot} c^2$$

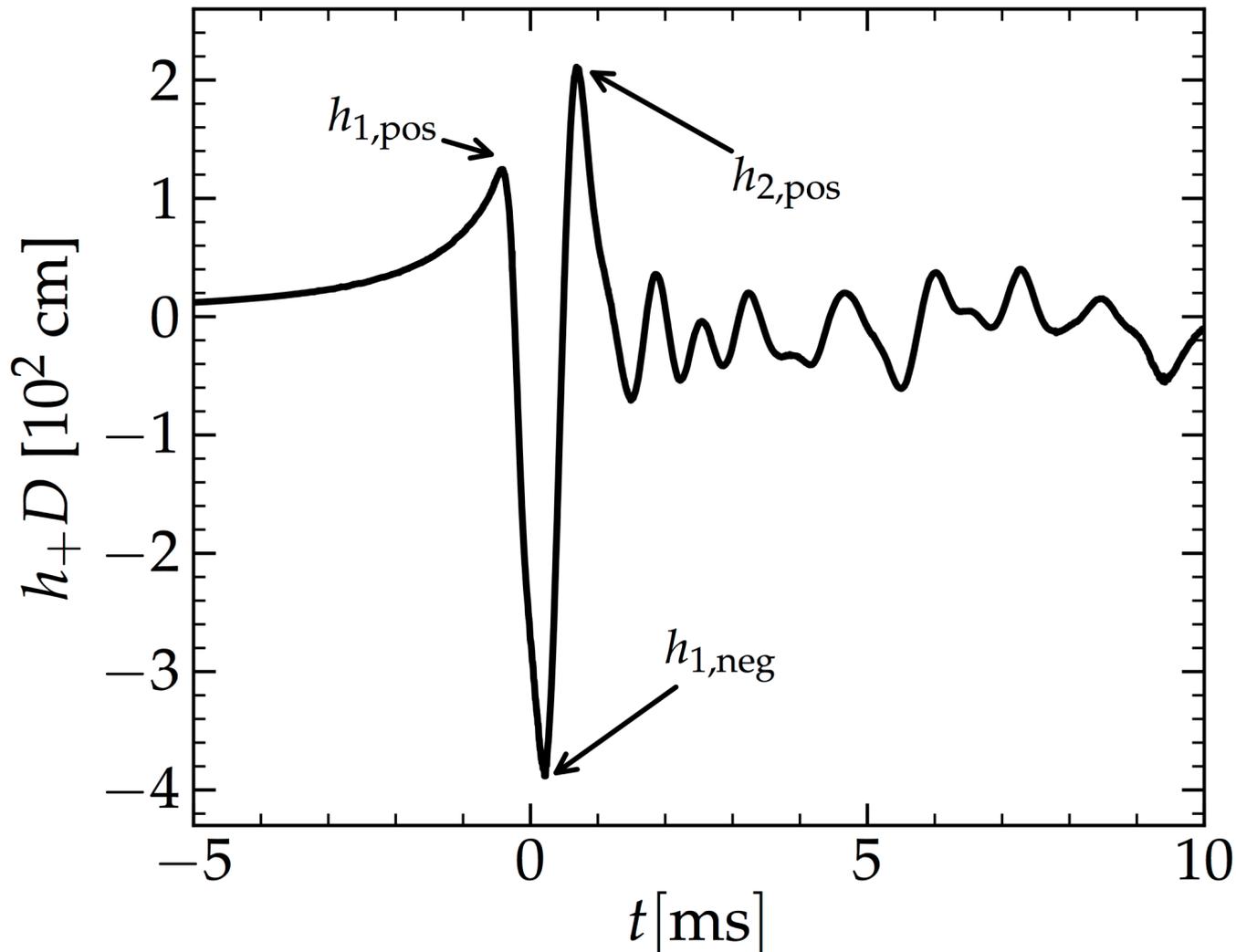


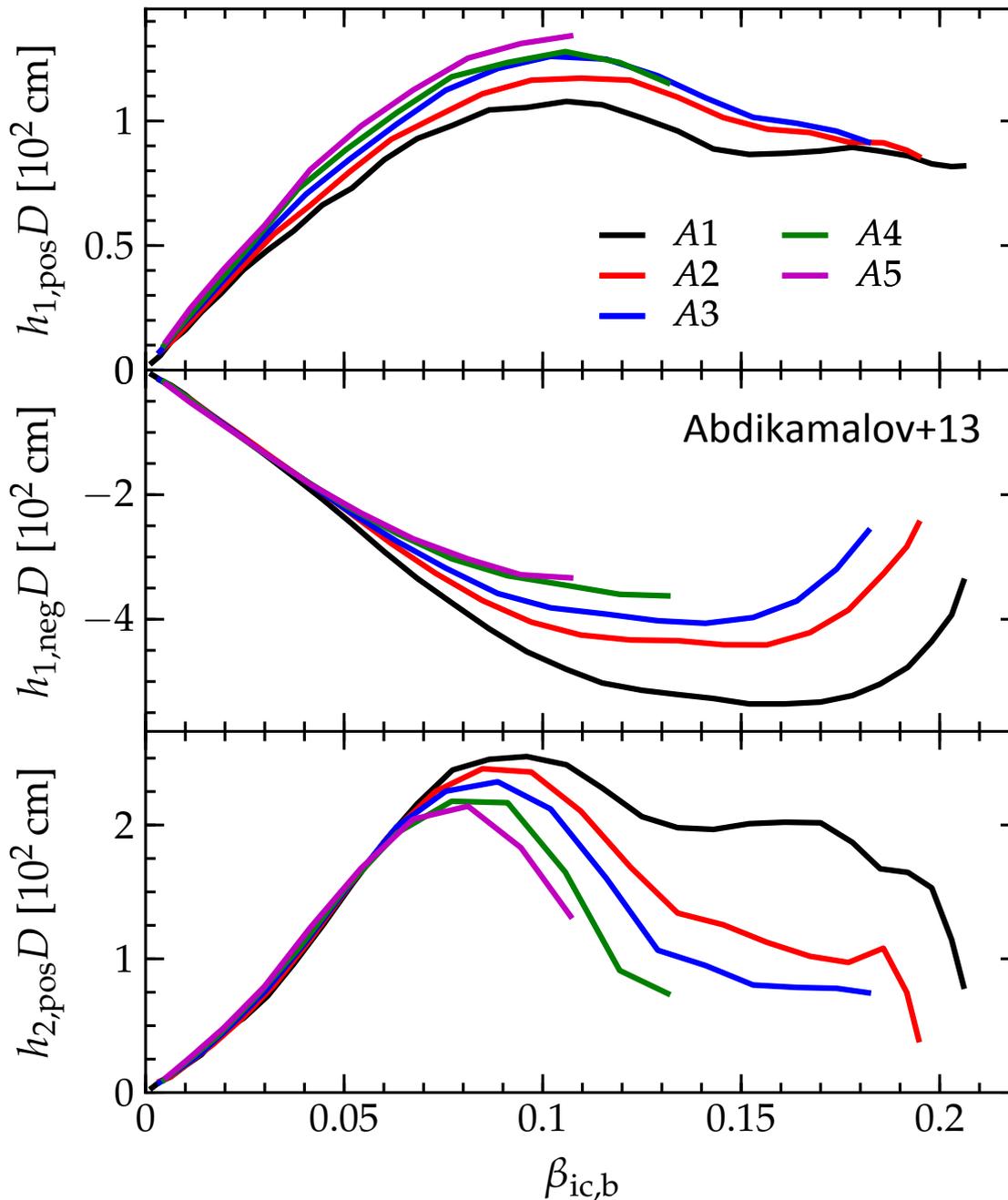
-> Throughout Milky Way  
with aLIGO

# GWs from Rotating Collapse & Bounce

Abdikamalov, Gossan, DeMaio, Ott, arXiv:1311.3678

Simple signal features:





Measure for  
“total rotation” of  
the inner core:

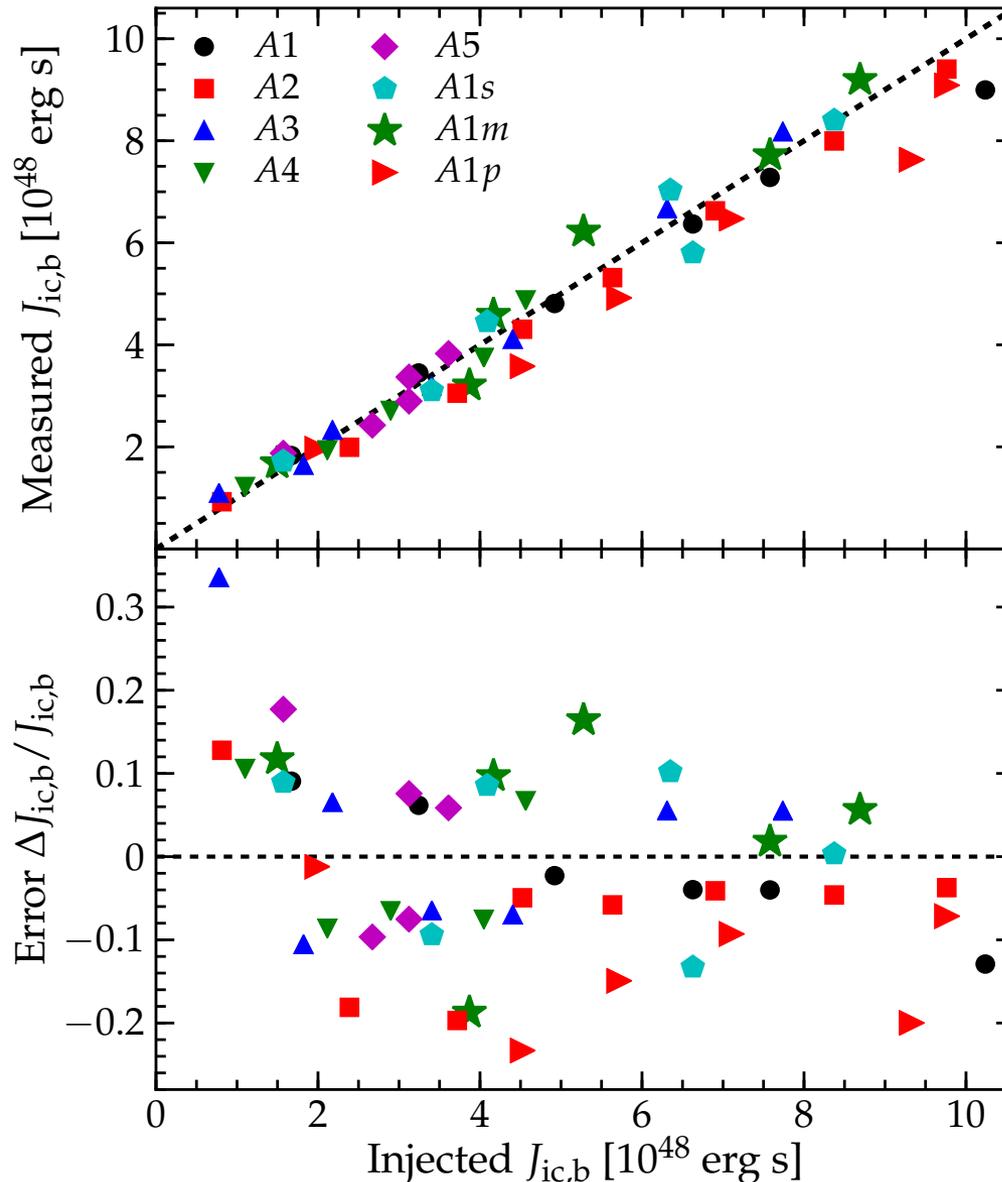
$$\beta = \frac{T}{|W|}$$

Closely related to inner core  
angular momentum

A1(most) – A5(least)  
differential rotation.

# Measuring Inner Core Angular Momentum

Abdikamalov, Gossan, DeMaio, Ott, arXiv:1311.3678



“Matched-filtering” analysis.

Unknown signal injected into simulated detector noise.

Can measure inner core angular momentum with  $< 30\%$  error!



**Join the  
American Physical Society  
Topical Group in Gravitation (GGR)!!!**

<http://www.aps.org/units/ggr/>

Now is a great time to join to help us gain  
APS division status by 2015,  
the centennial of General Relativity!