#### **FLASH Code Tutorial**

#### part V special features

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- "Features" so far:
- gravity solvers
  - multi-pole
  - multi-grid
  - BHTree
- particles
  - sinks
- radiation module
  - MGD
  - ray-trace + ionising radiation

#### • multi-species $\implies$ with individual properties

<b>Property Name</b>	Description	Data type
Α	Number of protons and neutrons in nucleus	real
Z	Atomic number	real
N	Number of neutrons	real
E	Number of electrons	real
BE	Binding Energy	real
GAMMA	Ratio of heat capacities	real
MS_ZMIN	Minimum allowed average ionization	real
MS_EOSTYPE	EOS type to use for MTMMMT EOS	integer
MS_EOSSUBTYPE	EOS subtype to use for MTMMMT EOS	integer
MS_EOSZFREEFILE	Name of file with ionization data	string
MS_EOSENERFILE	Name of file with internal energy data	string
MS_EOSPRESFILE	Name of file with pressure data	string
MS_NUMELEMS	Number of elements comprising this species	integer
MS_ZELEMS	Atomic number of each species element	$\operatorname{array}(\operatorname{integer})$
MS_AELEMS	Mass number of each species element	$\operatorname{array}(\operatorname{real})$
MS_FRACTIONS	Number fraction of each species element	$\operatorname{array}(\operatorname{real})$
MS_OPLOWTEMP	Temperature at which cold opacities are used	real

source/Multispecies/MultispeciesMain
 initialise properties: Simulation\_initSpecies.F90

```
#include "Multispecies.h"
#include "Flash.h"
```

- ! These two variables are defined in the Config file as ! SPECIES SF6 and SPECIES AIR
  - call Multispecies\_setProperty(SF6\_SPEC, A, 146.)
  - call Multispecies\_setProperty(SF6\_SPEC, Z, 70.)
  - call Multispecies\_setProperty(SF6\_SPEC, GAMMA, 1.09)
  - call Multispecies\_setProperty(AIR\_SPEC, A, 28.66)
  - call Multispecies\_setProperty(AIR\_SPEC, Z, 14.)

call Multispecies\_setProperty(AIR\_SPEC, GAMMA, 1.4)
end subroutine Simulation\_initSpecies

 Material properties physics/materialProperties

works with HD & MDH

- Viscosity/ViscosityMain
  - Constant
  - Spitzer thermal viscosity  $\implies v \propto T^{5/2}$
- MagneticResistivity/MagneticResistivityMain  $\Rightarrow$  so far: only Constant  $\eta$

 Material properties physics/materialProperties

works with HD & MDH

- thermal Conductivity/ConductivityMain
  - Constant
  - SpitzerHighZ

⇒ for electron conductivity (e.g. HEDP experiments)

$$K_{\rm ele} = \left(\frac{8}{\pi}\right)^{3/2} \frac{k_B^{7/2}}{e^4 \sqrt{m_{\rm ele}}} \left(\frac{1}{1+3.3/\bar{z}}\right) \frac{T_{\rm ele}^{5/2}}{\bar{z} \ln \Lambda_{ei}}$$

• **Relativistic** hydrodynamics:

 $\rightarrow$  e.g. AGN jets: Lorentz-factor ~ 45

physics/Hydro/HydroMain/split/RHD

(A. Mignione)

- h: enthalpy,  $\Gamma:$  specific heat ratio
- $\gamma = \left(1-oldsymbol{v}^2
  ight)^{-1/2}$

#### $\rightarrow$ use relativistic units: c = 1

 Relativistic hydrodynamics: physics/Hydro/HydroMain/split/RHD

RHD Sod



RHD Riemann2D

 Relativistic hydrodynamics: physics/Hydro/HydroMain/split/RHD



RHD\_Sod

RHD\_Riemann2D

 $\rightarrow$  no RMHD yet

#### • **Cosmology** unit:

physics/Cosmology/CosmologyMain

#### use co-moving variables:

$$\begin{split} \rho &\equiv a^{3}\tilde{\rho} & \longrightarrow & \frac{\partial\rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0 \\ p &\equiv a\tilde{p} & \frac{\partial\rho \mathbf{v}}{\partial t} + \nabla \cdot (\rho \mathbf{v} \mathbf{v}) + \nabla p + 2\frac{\dot{a}}{a}\rho \mathbf{v} + \rho \nabla \phi = 0 \\ T &\equiv & \frac{\tilde{T}}{a^{2}} & \frac{\partial\rho E}{\partial t} + \nabla \cdot [(\rho E + p)\mathbf{v}] + \frac{\dot{a}}{a}[(3\gamma - 1)\rho\epsilon + 2\rho v^{2}] + \rho \mathbf{v} \cdot \nabla \phi = 0 \\ \rho\epsilon &\equiv & a\tilde{\rho}\tilde{\epsilon} & \frac{\partial\rho\epsilon}{\partial t} + \nabla \cdot [(\rho\epsilon + p)\mathbf{v}] - \mathbf{v} \cdot \nabla p + \frac{\dot{a}}{a}(3\gamma - 1)\rho\epsilon = 0 \\ \vdots \text{ scale factor} & \nabla^{2}\phi = \frac{4\pi G}{a^{3}}(\rho - \bar{\rho}) \end{split}$$

~ variables: physical variables

a(t)

$$\Rightarrow$$
 terms  $\propto \frac{\dot{a}}{a}$  are source terms

• Cosmology unit:

Cosmology\_solveFriedmannEqn

- $\Rightarrow$  compute the scale factor a(t)
  - $\rightarrow$  using a 4th order Runge-Kutta with

$$H^{2}(t) \equiv \left(\frac{\dot{a}}{a}\right)^{2} = H_{0}^{2} \left(\frac{\Omega_{m}}{a^{3}} + \frac{\Omega_{r}}{a^{4}} + \Omega_{\Lambda} - \frac{\Omega_{c}}{a^{2}}\right) ; \ \bar{\rho} \quad \equiv \quad \Omega_{m} \rho_{\text{crit}}$$

 $H_0$ : today's Hubble parameter [1/sec]

curvature:  $\Omega_c \equiv \Omega_m + \Omega_r + \Omega_\Lambda - 1$ 

#### • Cosmology unit:

#### runtime parameters

Parameter	Type	Default	Description			
useCosmology	BOOLEAN	.true.	True if cosmology is to be used in this simula-			
			tion			
OmegaMatter	REAL	0.3	Ratio of total mass density to critical density			
			at the present epoch $(\Omega_m)$			
OmegaBaryon	REAL	0.05	Ratio of baryonic (gas) mass density to crit-			
			ical density at the present epoch; must be			
			$\leq$ OmegaMatter $(\Omega_b)$			
CosmologicalConstant	REAL	0.7	Ratio of the mass density equivalent in the cos-			
			mological constant to the critical density at the			
			present epoch $(\Omega_{\Lambda})$			
OmegaRadiation	REAL	$5 \times 10^{-5}$	Ratio of the mass density equivalent in radia-			
			tion to the critical density at the present epoch			
			$(\Omega_r)$			
HubbleConstant	REAL	$2.1065  imes 10^{-18}$	Value of the Hubble constant $H_0$ in sec <sup>-1</sup>			
MaxScaleChange	REAL	HUGE(1.)	Maximum permitted fractional change in the			
			scale factor during each timestep			
65 km/sec/Mpc						

• Cosmology unit:

one test setup: Pancake

⇒ Zeldovich (1970) analytic solution of a collapsing ellipsoid in an expanding background

 $\Rightarrow$  collapses first along the short axis  $\Rightarrow$  pancake structure

- Collisionless plasma: charged particles **PIC** (particle in cell)
  - $\Rightarrow$  continuous MHD description breaks down for large ion gyroradius  $r_{\rm gyr} \approx m_{\rm ion} v / q B$ compared to the system size, e.g. solar magnetosphere

 $\rightarrow$  in FLASH

Particles/ParticlesMain/active/charged/HybridPIC

- $\rightarrow$  charged ion particles within a continuous fluid
  - $\Rightarrow$  computational less expensive than pure multispecies particle simulations

Particles/ParticlesMain/active/charged/HybridPIC

• coupling via Lorentz force:

$$\frac{d\mathbf{r}_{i}}{dt} = \mathbf{v}_{i}, \quad \frac{d\mathbf{v}_{i}}{dt} = \frac{q_{i}}{m_{i}} \left( \mathbf{E} + \mathbf{v}_{i} \times \mathbf{B} \right), \quad i = 1, \dots, N_{I}$$
$$\mathbf{E} = \frac{1}{\rho_{I}} \left( -\mathbf{J}_{I} \times \mathbf{B} + \mu_{0}^{-1} \left( \nabla \times \mathbf{B} \right) \times \mathbf{B} \right) - \nabla p_{e} \quad ; \quad \frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

 $ho_{
m I}$ : ion density,  $J_{
m I}$ : ion current,  $p_{
m e}$ : electron pressure

- Grid\_mapParticlesToMesh
   map particle mass and charge to mesh
- Grid\_mapToMeshParticles
   interpolate mesh fields to particle position

Particles/ParticlesMain/active/charged/HybridPIC

- mapping schemes:
  - linear interpolation (Cloud-in-Cell):
    - ⇒ Particles/ParticlesMapping/CIC
  - Particles/ParticlesMapping/Quadratic
- advancing:
  - Euler, RK, Midpoint, ...
- time scales:
  - due to velocity:  $\Delta t \max_i(|\mathbf{v}_i|) < \Delta x$
  - due to plasma waves:

$$\Delta t < \frac{\Omega_i^{-1}}{\pi} \left(\frac{\Delta x}{\delta_i}\right)^2 \sim \frac{n}{B} \left(\Delta x\right)^2, \qquad \delta_i = \frac{1}{|q_i|} \sqrt{\frac{m_i}{\mu_0 n}}$$

• Collisionless plasma: charged particles PIC

#### $\Rightarrow$ particle properties:

Variable	Type	Default	Description
pt_picPname_1	STRING	"H+"	Specie 1 name
$pt_picPmass_1$	REAL	1.0	Specie 1 mass, $m_i$ [amu]
$pt_picPcharge_1$	REAL	1.0	Specie 1 charge, $q_i$ [e]
$pt_picPdensity_1$	REAL	1.0	Initial $n_I$ specie 1 $[m^{-3}]$
$pt_picPtemp_1$	REAL	1.5e5	Initial $T_I$ specie 1 [K]
pt_picPvelx_1	REAL	0.0	Initial $\mathbf{u}_I$ specie 1 [m/s]
pt_picPvely_1	REAL	0.0	
$pt_picPvelz_1$	REAL	0.0	
$pt_picPweight_1$	REAL	1.0	Real particles per macro-
			particle of specie 1

#### $\Rightarrow$ example: Plasma

### FLASH code: developments

- FLASH: ongoing developments
  - chemistry: coupling with KROME (S. Bovino & D. Seifried)
  - radiation transfer
    - ⇒ extend point source ray-trace using parallel rays for photon scattering (L. Buntemeyer)
  - implementation of TreeCol (Paul Clark & Simon Glover)
     ⇒ get column density for external radiation

# Disc Formation in Turbulent Cloud Cores

Robi Banerjee University of Hamburg

Co-Worker: **Daniel Seifried** (Hamburg), Ralph Pudritz (McMaster), Ralf Klessen (ITA)

ISSAC 2013, Robi Banerjee

## Star Formation: Early-type discs

Observations of Class 0 protostellar discs: Tobin et al. 2012



ISSAC 2013, Robi Banerjee

#### Magnetic Fields



## Magnetic Fields

#### magnetic criticality

mass-to-flux ratio:

$$\mu \equiv \left(\frac{M}{\Phi}\right) = \text{self-gravity / magnetic support}$$

critical value:

 $\mu_{\rm crit} = 0.13/\sqrt{G}$ 

spherical collapsing structure Mouschovias & Spitzer 1976

 $\mu_{\rm crit} = \frac{1}{2\pi\sqrt{G}} \approx 0.16/\sqrt{G}$ 

uniform disc Nakano & Nakamura 1978

# Star Formation: Early-type discs

Collapse of magnetised, rotating cloud cores
stronger magnetic fields: μ < 5 in agreement with observations</li>



(e.g. Crutcher et al. 2010)



Hennebelle & Teyssier 2008, ...

 $\Rightarrow$  **too** efficient magnetic braking  $\Rightarrow$  **no** disc formation

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## Angular Momentum Problem II

#### **Solutions?**

- flux loss by:
  - Ohmic resistivity (Dapp & Basu 2011,

Krasnopolsky et al. 2010)

- ambipolar Diffusion (Duffin & Pudritz 2008, Li et al. 2011)
- turbulent reconnection (Lazarian & Vishniac 1999, Santos-Lima et al. 2012)
- Hall effect (Krasnopolsky et al. 2011)
- Outflows from small discs

# Angular Momentum Problem II

→ Non-ideal MHD and reconnection active only at small scales/high density
→ not effective enough to reduce magnetic braking



⇒ Li, Krasnopolsky & Shang 2011: "The problem of catastrophic magnetic braking that prevents disk formation in dense cores magnetized to realistic levels remains unresolved"

# Parameter study of collapsing cores

Seifried, et al. 2013

Run	$m_{\rm core}$ (M <sub>O</sub> )	r <sub>core</sub> (pc)	μ	Rotation	$\Omega (10^{-13} \text{ s}^{-1})$	$eta_{ ext{turb}}$	Turbulence seed	р	M <sub>rms</sub>	t <sub>sim</sub> (kyr)
2.6-NoRot-M2	2.6	0.0485	2.6	No	0	0.087	А	5/3	0.74	15
2.6-Rot-M2	2.6	0.0485	2.6	Yes	2.20	0.087	Α	5/3	0.74	15
2.6-NoRot-M100	100	0.125	2.6	No	0	0.084	Α	5/3	2.5	15
2.6-Rot-M100	100	0.125	2.6	Yes	3.16	0.084	Α	5/3	2.5	15
2.6-Rot-M100-B	100	0.125	2.6	Yes	3.16	0.084	В	5/3	2.5	15
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2.6-NoRot-M300	300	0.125	2.6	No	0	0.12	Α	5/3	5.0	10
2.6-Rot-M1000	1000	0.375	2.6	Yes	1.90	0.081	Α	5/3	5.4	10

- low + high mass cores
- strong magnetic field
- with/without global rotation
- sub-/supersonic turbulence
- resolution: 1.2 AU



## Initial angular momentum of cores

 observational evidence for rotating cores (R ~ 0.1 pc) e.g. Goodman et al., 1993:

$$\begin{split} \Omega &\sim 10^{-14} - 10^{-13} \text{ s}^{-1} \\ &\Rightarrow j \sim 10^{21} \text{ cm}^2 \text{ s}^{-1} \\ &\Rightarrow \beta \sim 0.03 \propto (t_{\rm ff} \Omega)^2 \end{split}$$

but: large scatter

• compare to galactic shear flow:  $\Omega \sim 10^{-16} - 10^{-15} \text{ s}^{-1}$  $\Rightarrow$  generated by turbulence (Barranco & Goodman, 1998)?

## Initial angular momentum of cores?

• Dib et al. 2010:

synthetic observations from simulations overestimate true values by a factor of **8–10** 



 $\implies$  also consistent with no global rotation on scales > 0.1 pc

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 $\Rightarrow$  discs "reappear"







#### velocity structure







 $\Rightarrow$  only little flux loss

#### Magnetic field structure



rotation vs. magnetic field orientation → inclined rotation helps to form discs? (Hennbelle & Ciardi 2009, Joos et al. 2012)



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 $\alpha / 1^{\circ}$ 

⇒ but no large scale magnetic field component

## Summary: Collapse of Turbulent Cores

- Magnetic braking catastrophe only for unrealistic ICs
- is easy to form discs in a turbulent environment
  - ⇒ see also:
     Santos-Lima et al. 2012
     Myers et al. 2013 (Chris' talk on Wednesday)

 $\Rightarrow$  flux loss by turbulent reconnection ? (Lazarian & Vishniac 1999)

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