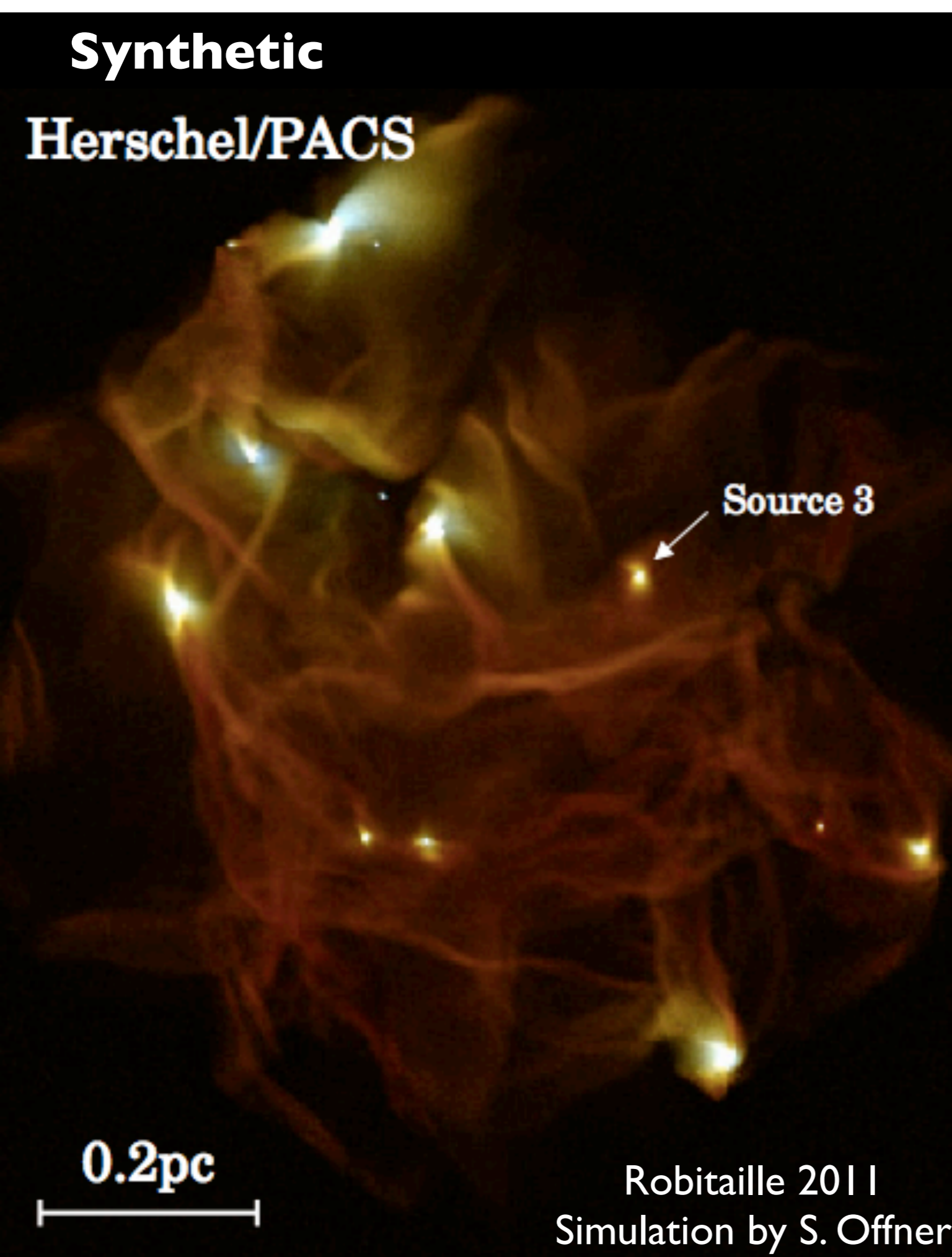


**Synthetic**

**Herschel/PACS**



**0.2pc**

Robitaille 2011  
Simulation by S. Offner

# Dust Continuum Modeling: Monte Carlo Radiative Transfer with Hyperion

Stella Offner  
HiPACC  
Aug 6, 2013

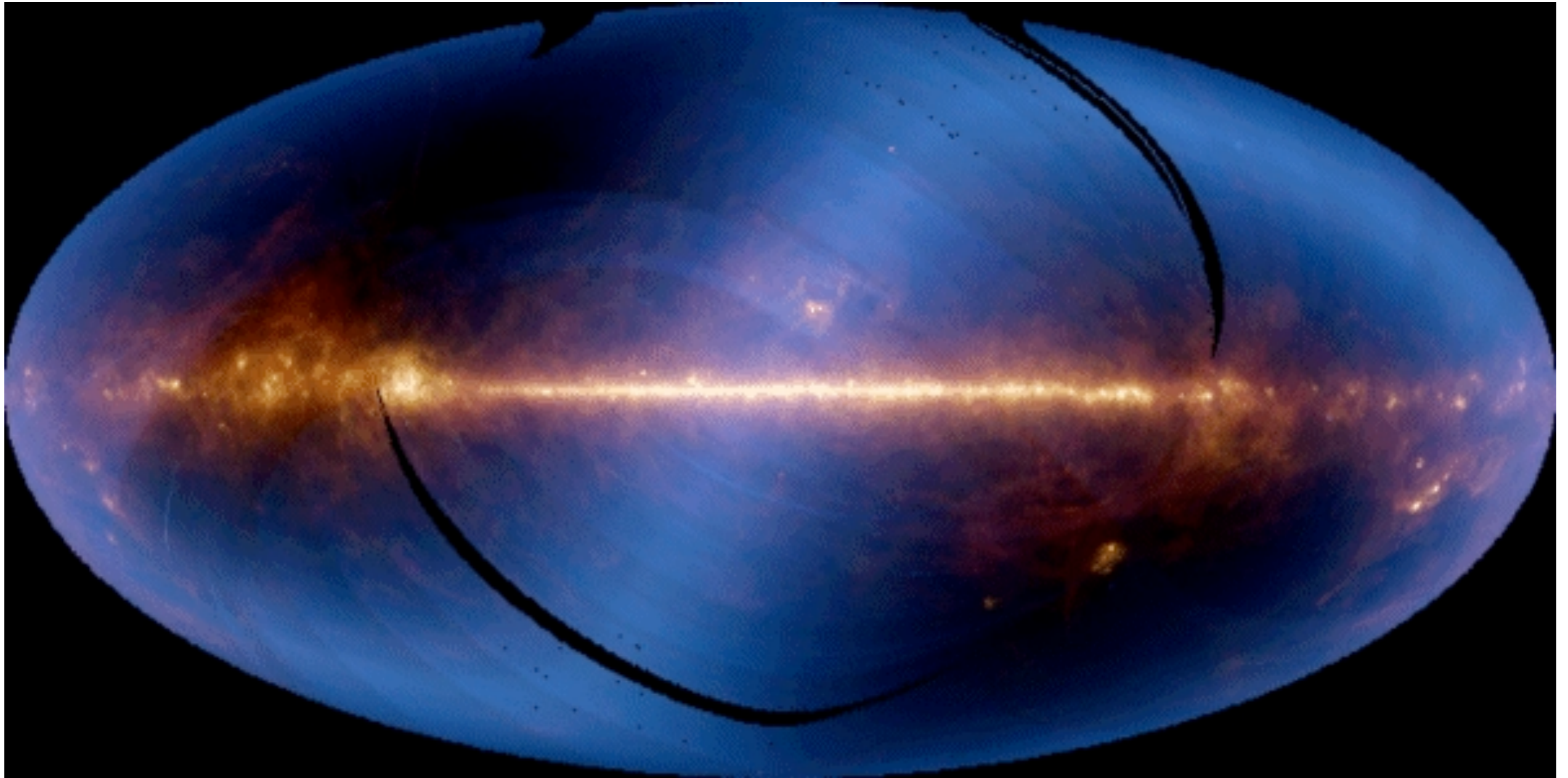
# Outline

- Why model dust?
- The physics of dust: emission, absorption & scattering
- Monte Carlo methods
- Hyperion
- Project

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# Why model dust?



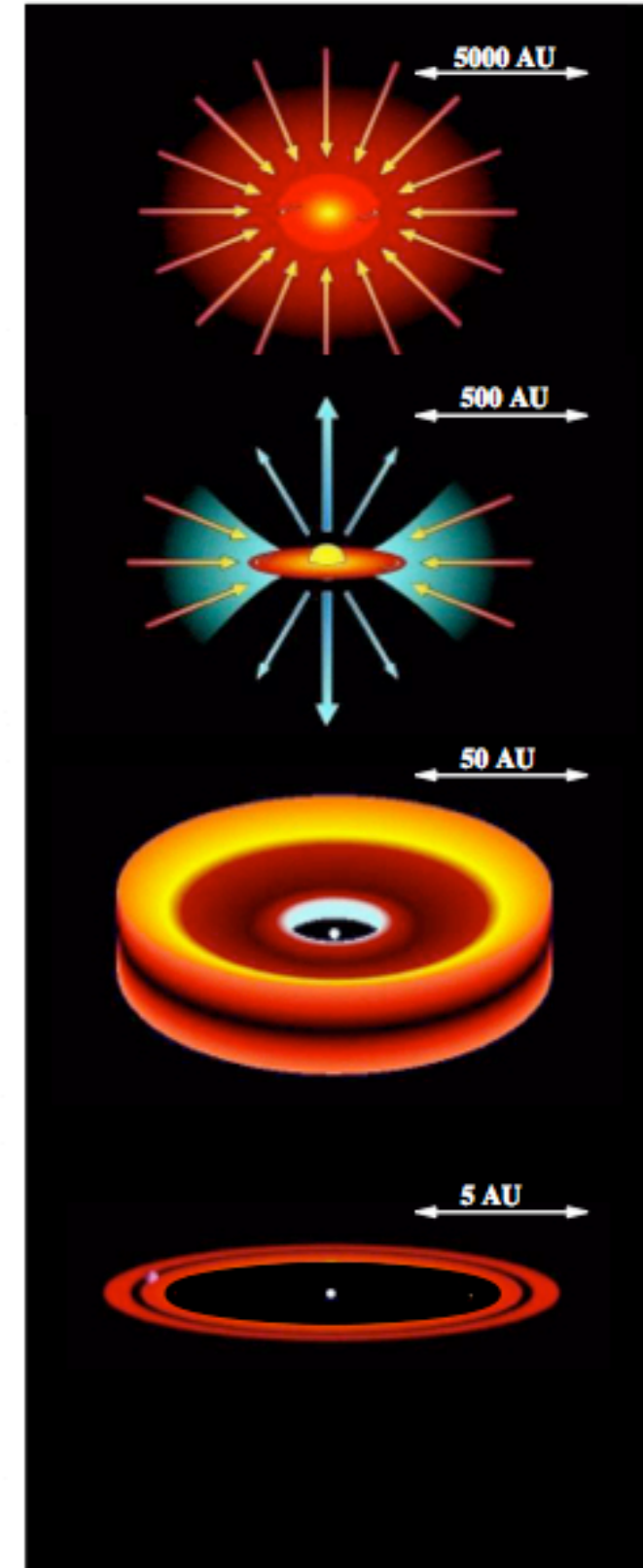
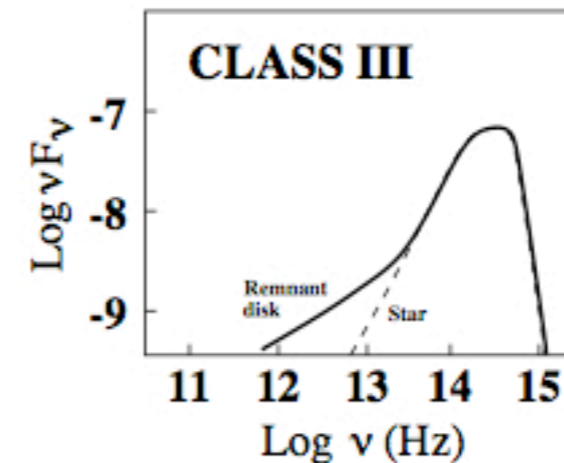
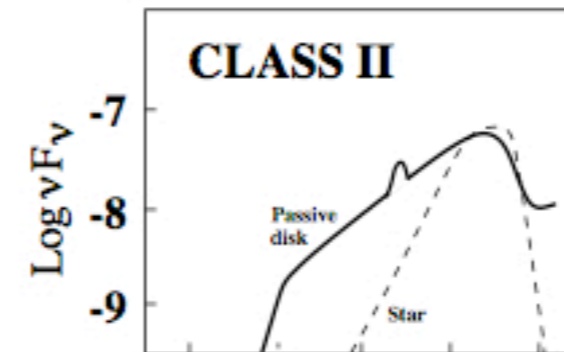
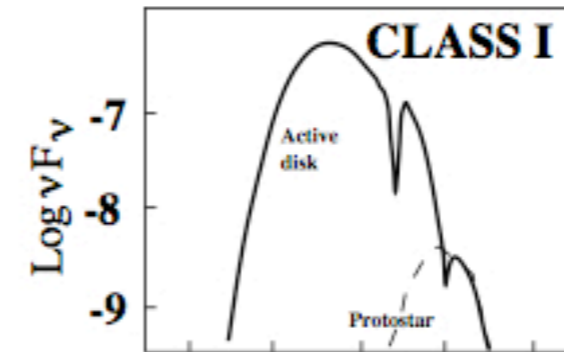
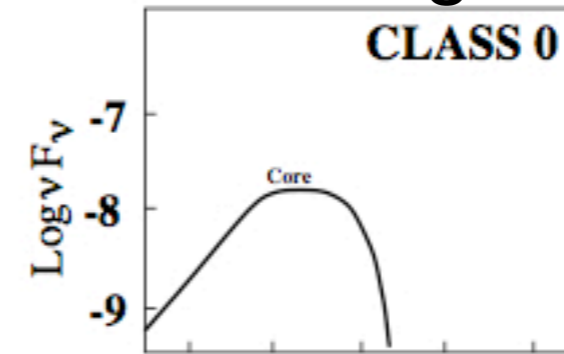
IRAS All Sky Survey

# Why model dust?

- Radiation of forming stars is reprocessed by interstellar dust grains
- Reprocessing = extinction (=scattering+absorption), polarization
- Dust to gas ratio:

$$\langle \rho_{dust} / \rho_{gas} \rangle \approx 0.01$$

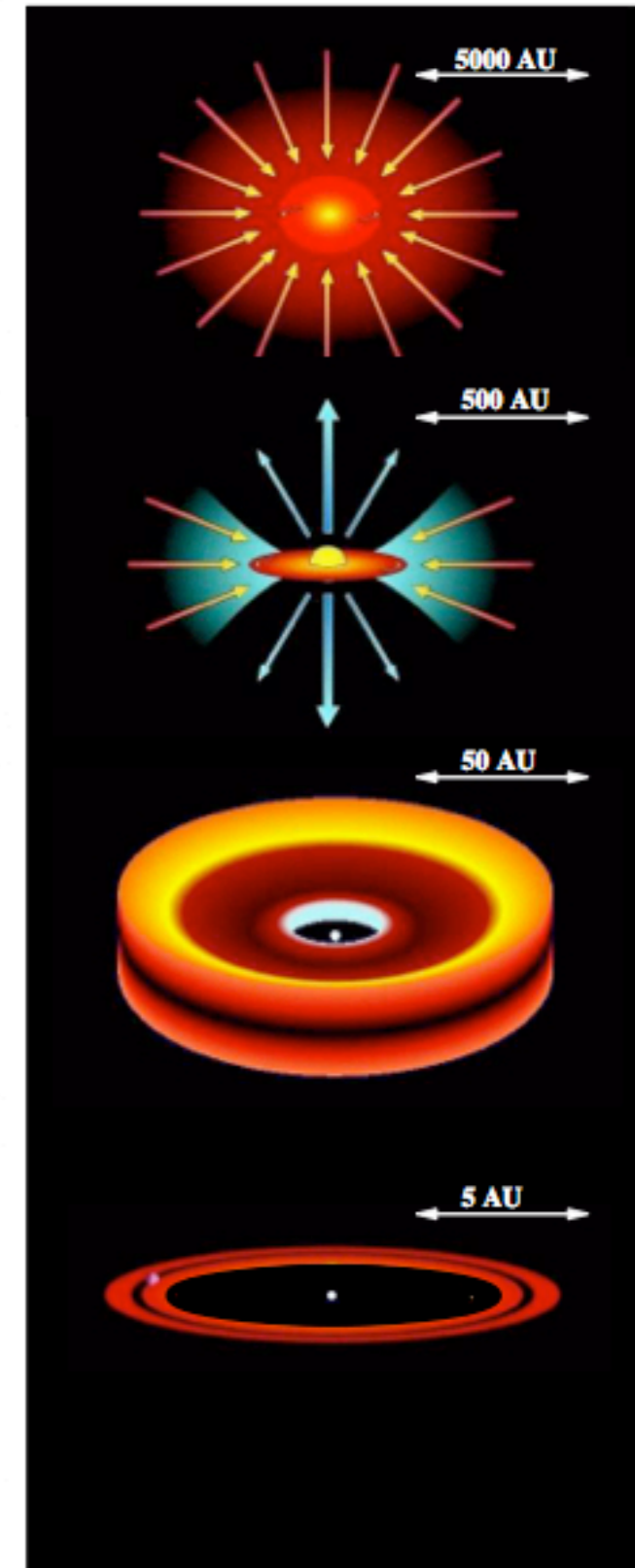
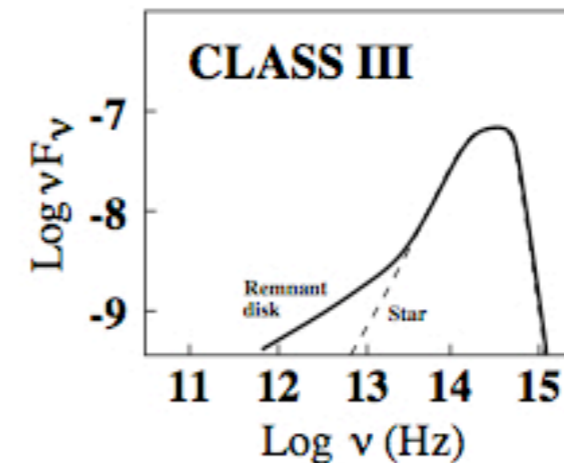
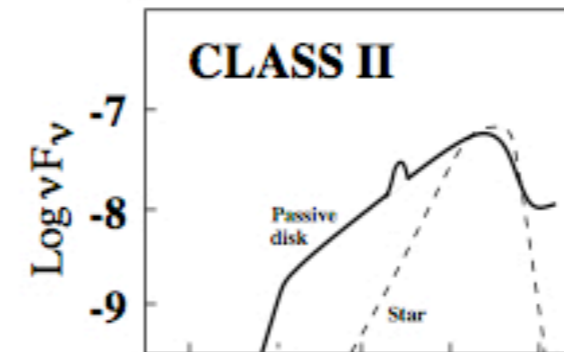
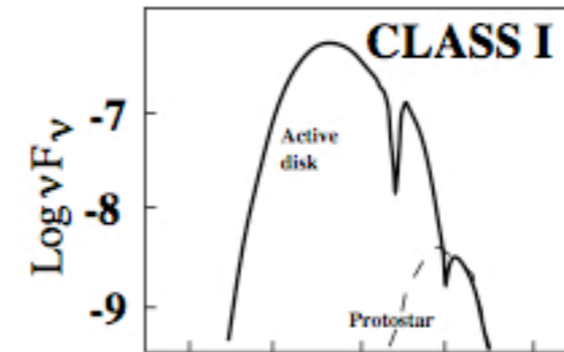
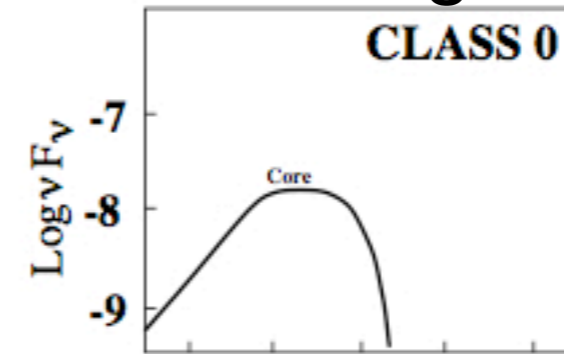
T increasing →



# Why model dust?

- Perform modeling of radiation-dust interaction to reconstruct:
  - dust properties
  - dust/gas distribution
  - source properties
  - temperature distribution (esp. useful if dust+gas are thermally coupled,  $n > 10^4 \text{ cm}^{-3}$ )

T increasing →

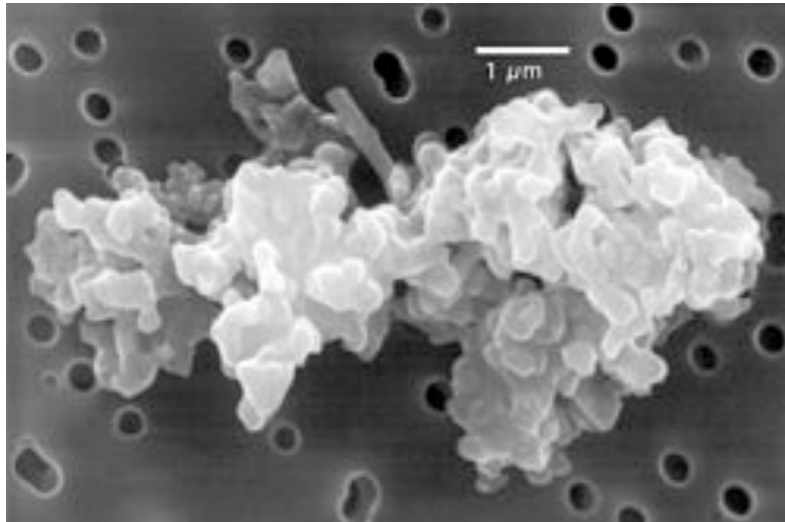


# Outline

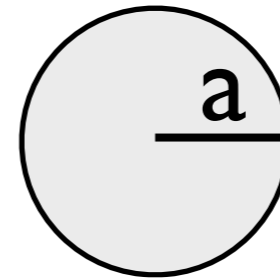
- Why model dust?
- The physics of dust: emission, absorption & scattering
- Monte Carlo methods
- Hyperion
- Project

# Dust Basics

Dust grain



“Dust grain”



(%)

100

. Enceladus (99%)

. Eris(96%)

90

80

70

60

50

40

30

20

10

0

SNOW  
fresh

SNOW  
old

SAND  
dry

ICE

SAND  
wet

SOIL  
dark  
wet

WATER

CUMULUS  
STRATUS

STRATUS

DESERT

SAVANNA

FOREST

ALTOSTRATUS  
CIRRUS

MEADOWS

CROPS

Extinction Cross Section:

$$\sigma(\lambda) = \pi a^2 Q_{ext}(\lambda)$$

Amount of scattering:

$$\text{albedo} = \frac{\sigma_{sca}}{\sigma_{ext}} = \frac{Q_{sca}}{Q_{ext}} \leq 1$$

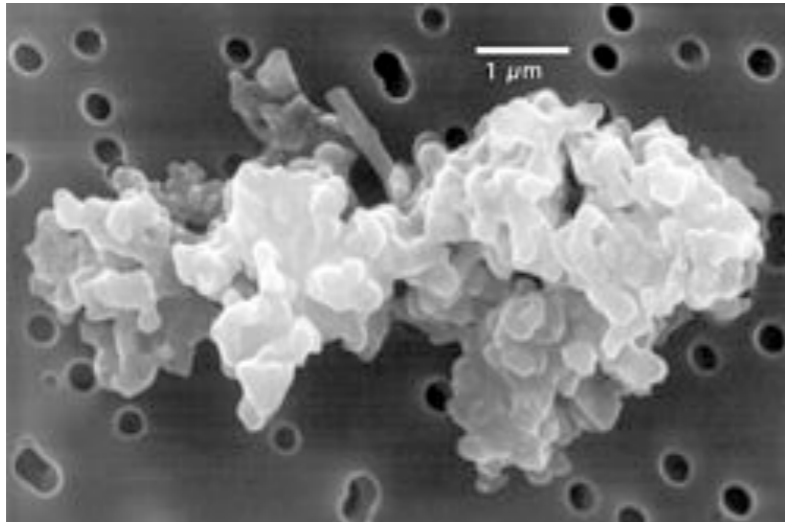
Absorption Opacity:

$$K_{abs} = \pi a^2 Q_{abs} / m_{dust}$$

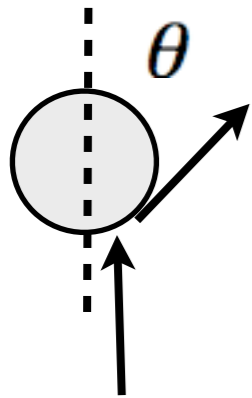
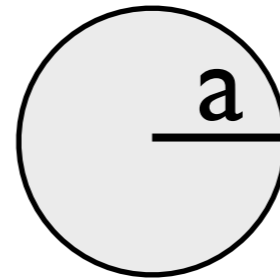


# Dust Basics

Dust grain



“Dust grain”



Scattering Phase Function:

$$g = \langle \cos \theta \rangle = \frac{\int_0^\pi I(\theta) \cos \theta d\Omega}{\int_0^\pi I(\theta) d\Omega}$$

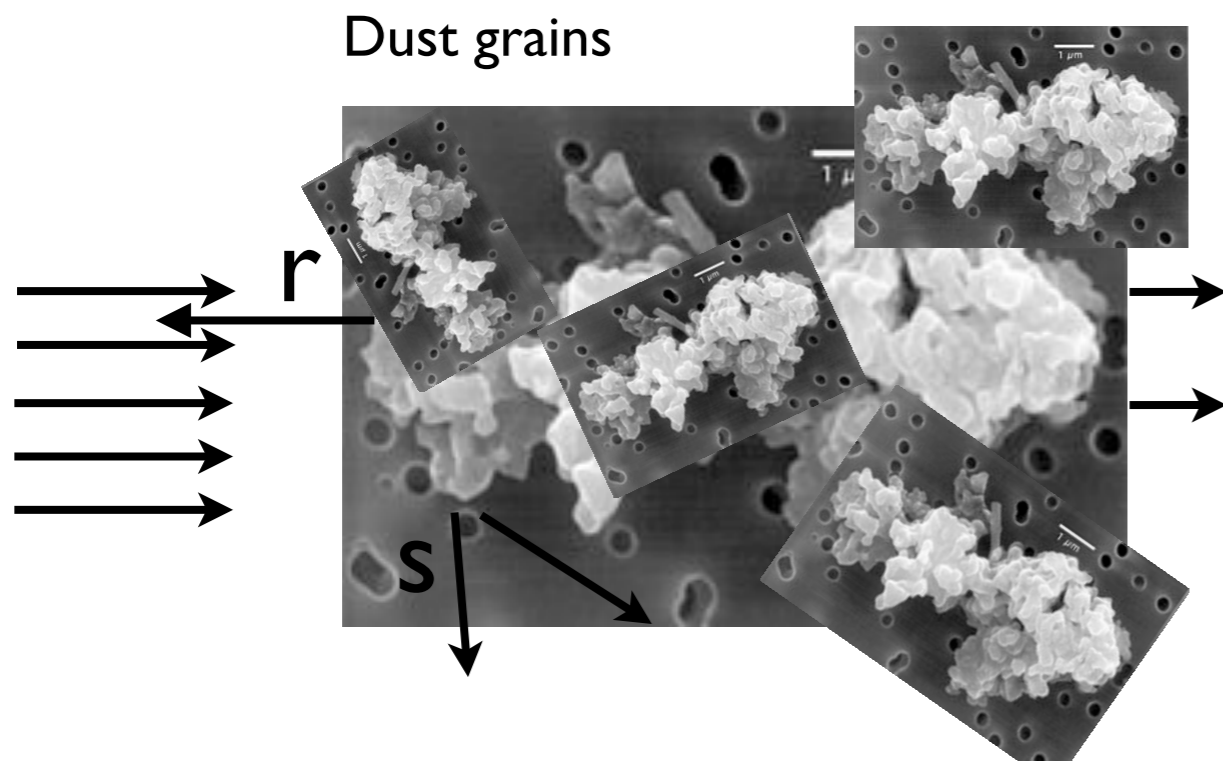
- $g = 1$  Forward (diffraction)
- $g = 0$  Isotropic
- $g = -1$  Backscattered (reflection)

# Dust Basics

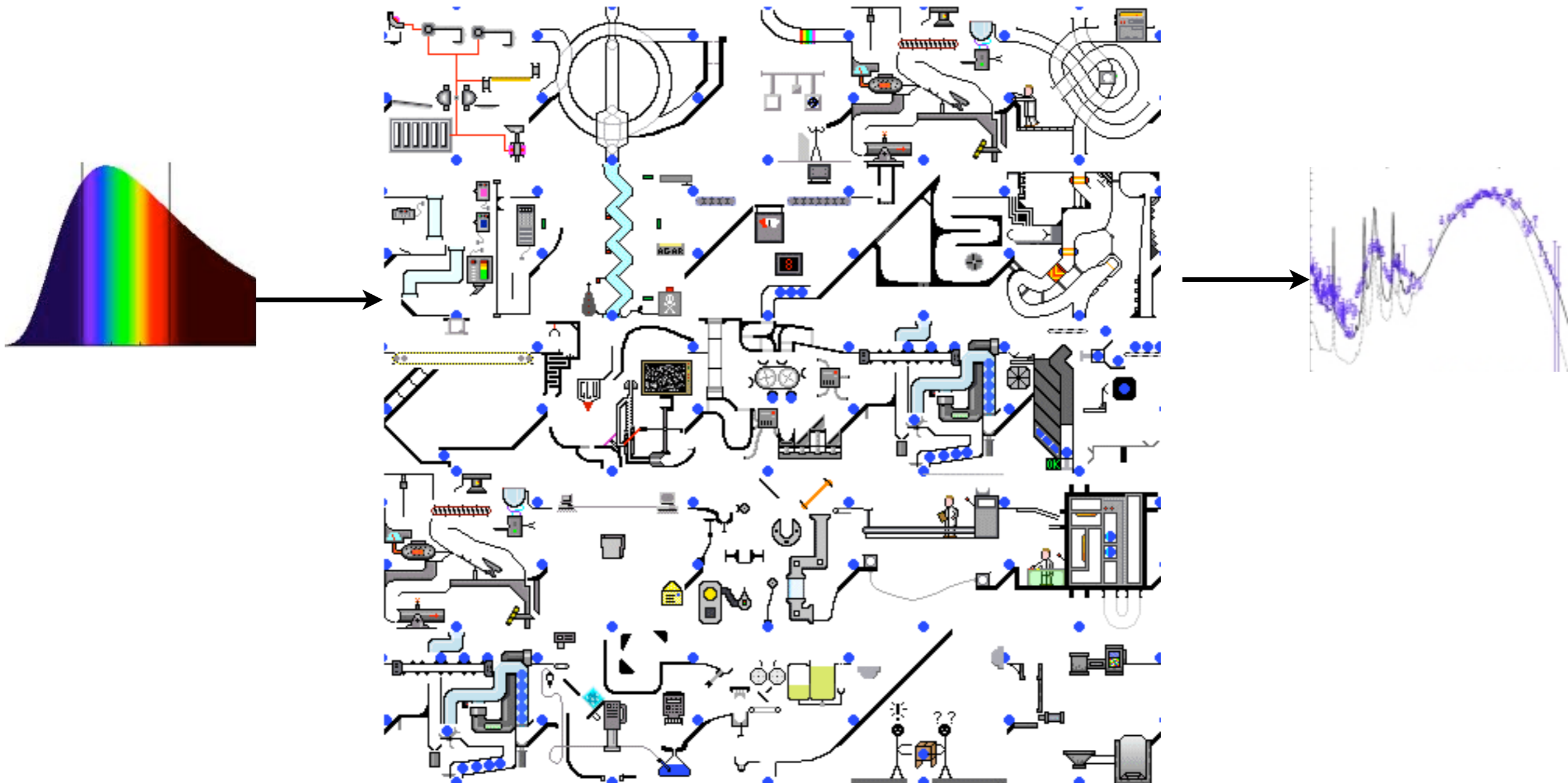
Find the dust:

<http://www.astro.princeton.edu/~draine/dust/dustmix.html>

Draine (2003abc): extinction, absorption, albedo,  $\langle \cos(\theta) \rangle$ ,  $\langle \cos^2(\theta) \rangle$  for wavelengths 1 cm - 1 Angstrom for a mixture of C and Silicate grains for ISM



# The Problem

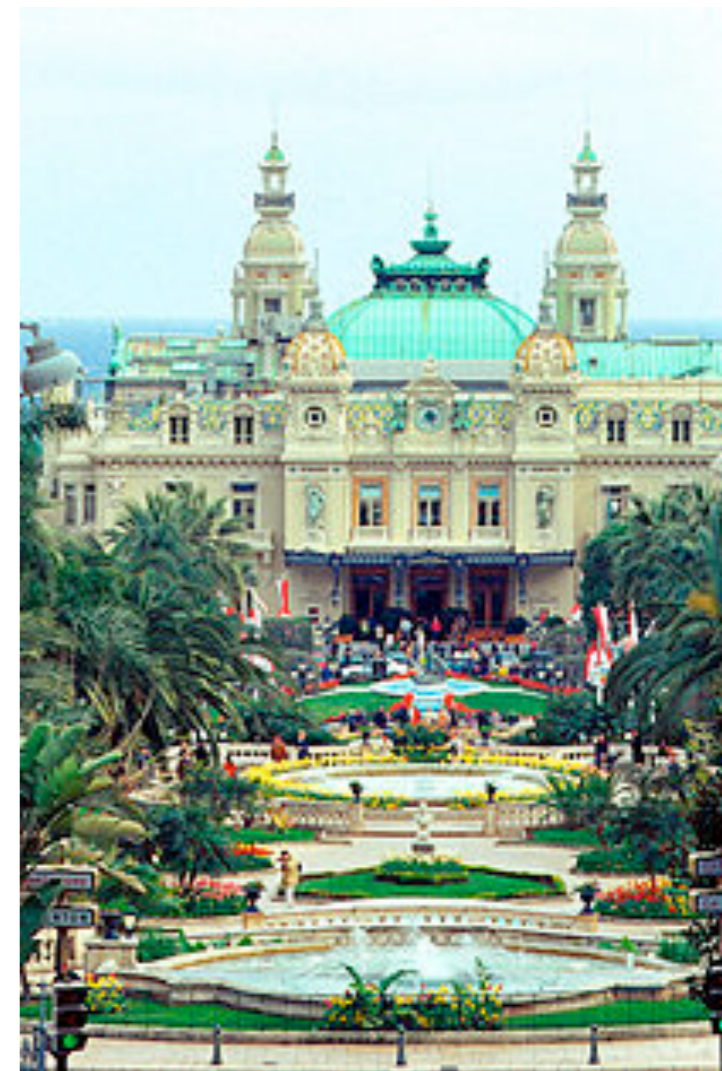


# Outline

- Why model dust?
- The physics of dust: emission, absorption & scattering
- Monte Carlo methods
- Hyperion
- Project

# Monte Carlo Method

- Repeated random sampling from a probability distribution
- Invented by Stanislaw Ulam, John Von Neumann, and Nicholas Metropolis in 1940s, who were working on the Manhattan Project at LANL
- Led to the field of random number generation



# Monte Carlo Method

- Radiative Transfer: randomly sample frequencies of photons (or “photon packets (PPs)” ) from some source spectrum
- Don't solve radiation transfer directly; instead follow interaction of each PP with the dust
- After traveling some optical depth, PPs are either scattered, absorbed or re-emitted; actions also randomly sampled from some probability distribution function

# Outline

- Why model dust?
- The physics of dust: emission, absorption & scattering
- Monte Carlo methods
- **Hyperion**
- Project



[robitaille@mpia.de](mailto:robitaille@mpia.de)

“astrofrog”

# hyperion

Read  
Docs

Download  
TAR Ball

View On  
GitHub

## Getting started

Hyperion is a parallelized 3-d dust continuum radiative transfer code. The code is described in [Robitaille \(2011\)](#). Its main features include:

- Dust continuum radiative transfer
- Dust temperature calculation
- SEDs, images, and polarization maps
- Support for arbitrary 3-d geometry
- Support for multiple sources and dust populations
- Support for arbitrary dust properties
- Cartesian, Polar, and Adaptive grids (Octree and AMR)
- Easy-to-use Python library to set up, run, and post-process models
- High performance parallelized (MPI) Fortran 2003 core

The current stable version of Hyperion is 0.9.1 - [download](#)

The documentation and installation instructions are located at <http://docs.hyperion-rt.org>





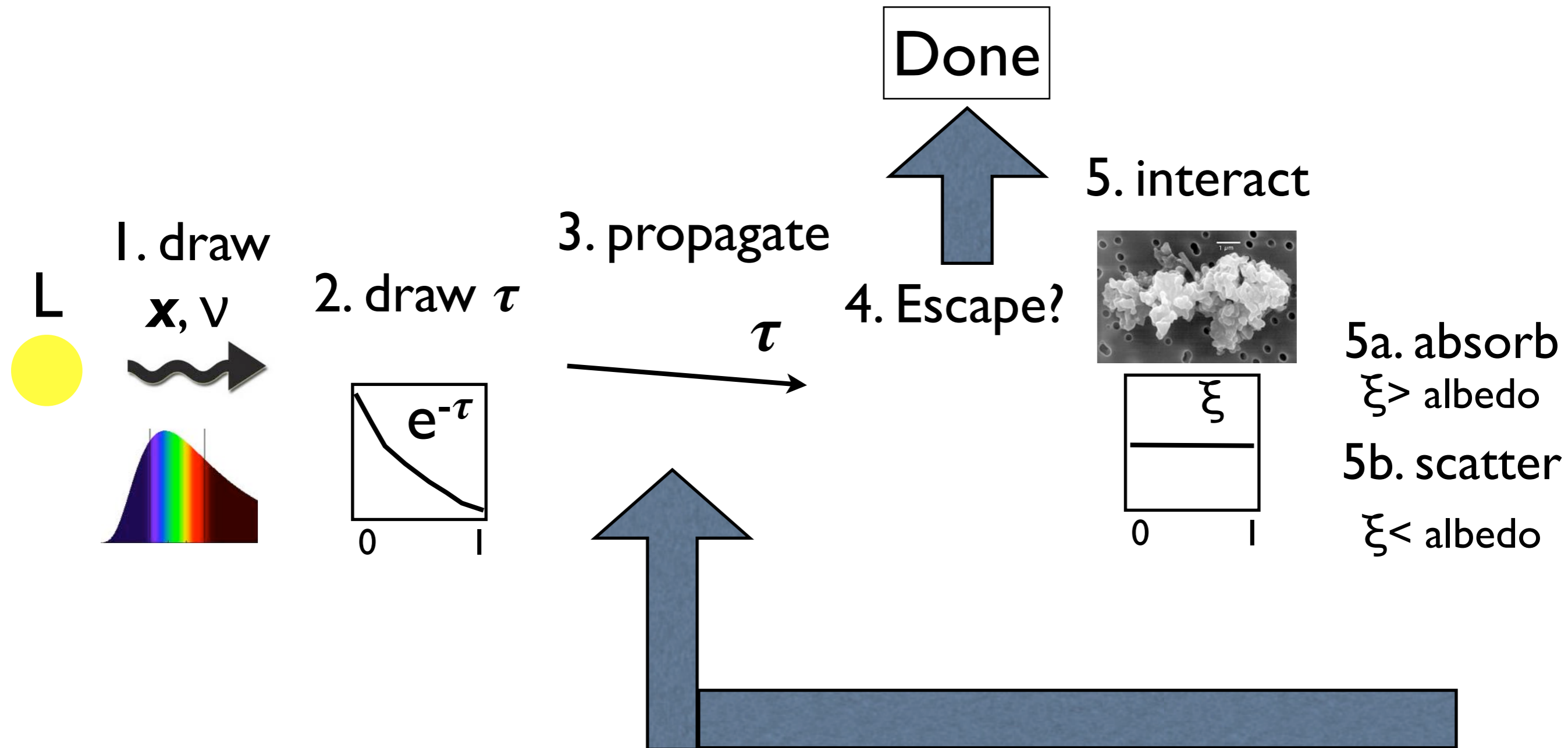
# Inputs I: Sources

- User specifies: (1) each source bolometric luminosity (2) source position (3) source spectrum
- Types of sources:
  - Isotropic point sources
  - Spherical sources (with or without limb darkening, hot/cool spots properties)
  - Diffuse sources: flux emitted from grid cells (e.g. unresolved sources like shocks or viscous energy dissipations)
  - External isotropic sources (e.g. interstellar radiation field)

# Inputs 2: Dust

- User specifies:
  - (1) Dust density distribution\*
  - (2) Dust properties (extinction coefficient, albedo, scattering properties)
  - (3) Dust sublimation (cap specific energy absorption; all dust removed from cells exceeding maximum specific energy absorption rate; dust density reduced but not zero)
- Mean dust opacities and emissivities are pre-computed (before MC), assuming LTE:  $j_\nu = \kappa_\nu B_\nu(T)$ .
- \*Types of grids: 3D cartesian, spherical, cylindrical, adaptive cartesian (octree and AMR)

# Photon Packet Propagation



- For high optical depth, switch to diffusion approximation

# Temperature/Energy absorption rate calculation I

- Iterative method to obtain temperature.
- In first iteration, compute the specific energy absorption rate of the dust:
- Then compute the dust temperature,  $T$ , assuming LTE:
- Dust quantities are tabulated as a functions of absorption rate not  $T$  ( $T$  is computed on-the-fly from  $A$ )

dt = time photon packets are emitted  
 $V$  = cell volume  
epsilon = energy of photon packet  
 $l$  = path length traveled  
kappa\_nu = mass absorption coefficient

$$A = \frac{1}{\Delta t} \frac{\epsilon}{V} \sum l \kappa_\nu$$

$$4\pi \kappa_P(T) B(T) = \dot{A}$$

kappa\_P = Planck mean mass absorption coefficient  
 $B(T)$  = nu integrated Planck function

$$B(T) = (\sigma/\pi) T^4$$

# Temperature/Energy absorption rate calculation II

- Iterative method to obtain temperature.
- Because emissivity depends on  $A$ , which depends on photon packet propagation, which depends on the photon frequency, which depends on the emissivity, must iterate....
- Converged when 99.9% of cells have absorption rate differences by less than a factor of 2 (need to specify)
- Users can set this threshold

$dt$  = time photon packets are emitted  
 $V$  = cell volume  
 $\epsilon$  = energy of photon packet  
 $l$  = path length traveled  
 $\kappa_{\nu}$  = mass absorption coefficient

$$\dot{A} = \frac{1}{\Delta t} \frac{\epsilon}{V} \sum \ell \kappa_{\nu}$$

$$4\pi \kappa_P(T) B(T) = \dot{A}$$

$\kappa_P$  = Planck mean mass absorption coefficient  
 $B(T)$  = nu integrated Planck function

$$B(T) = \left(\frac{\sigma}{\pi}\right) T^4$$

$$\kappa_P \equiv \frac{\int_0^{\infty} I_{b\lambda} \kappa_{\lambda} d\lambda}{\int_0^{\infty} I_{b\lambda} d\lambda}$$

# SEDs and Images

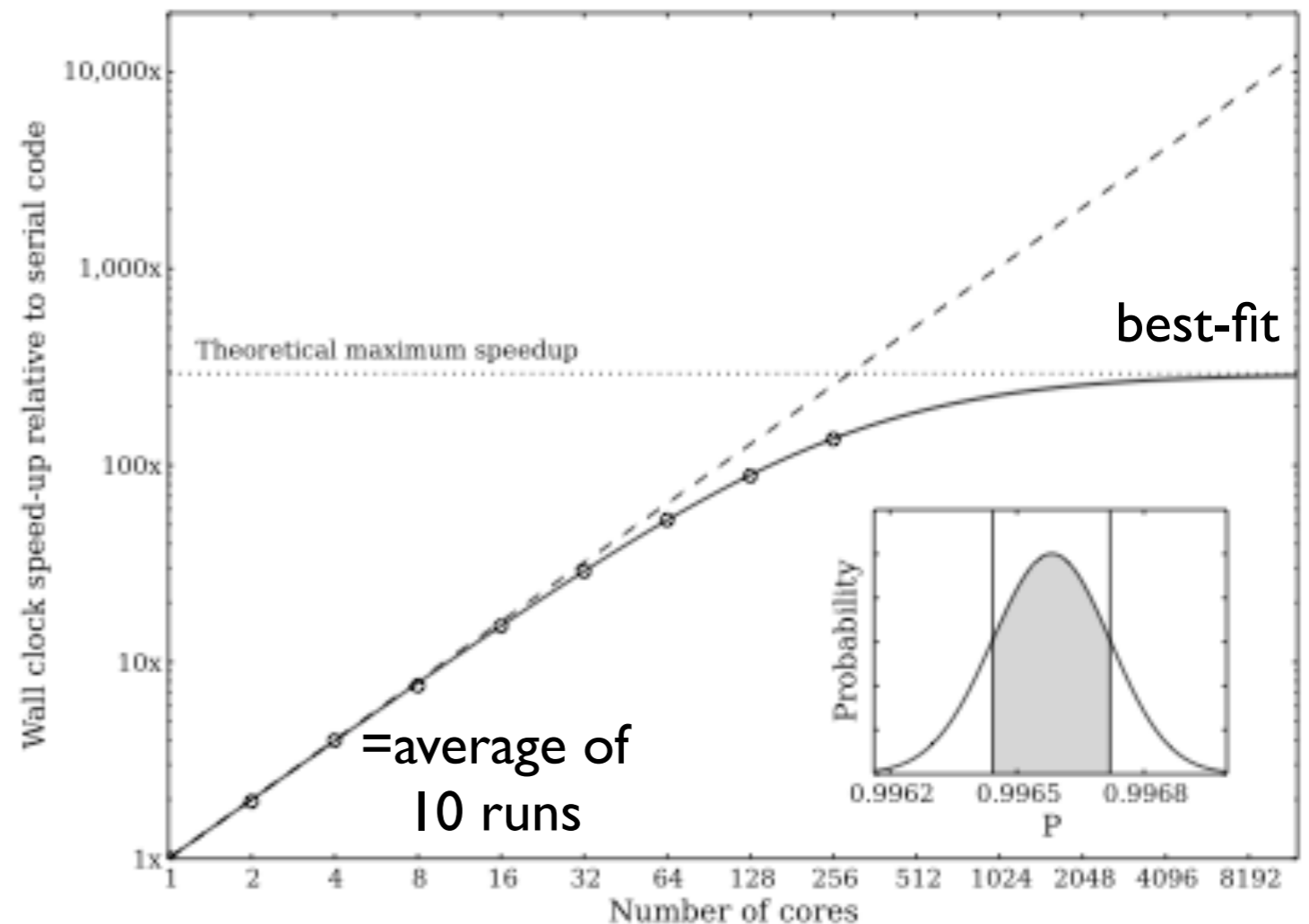
- Several options for computing these:
- “Photon binning” = bin PPs in viewing angles as they escape from the grid
- Inefficient since PPs only contribute once and angles can’t be arbitrarily small
- “Peeling-off” = after each scattering or re-emission, the probability,  $p$ , of the PP being scattered or re-emitted toward the observer is computed; this is added to the SED/images with weight  $pe^{-\tau}$
- better signal-to-noise
- “Raytracing” = determine the source function at each grid position and solving (in post-processing) the equation of radiative transfer along rays to observer
- currently only works for thermal emission (long wavelengths); implemented for scattering in future

combine

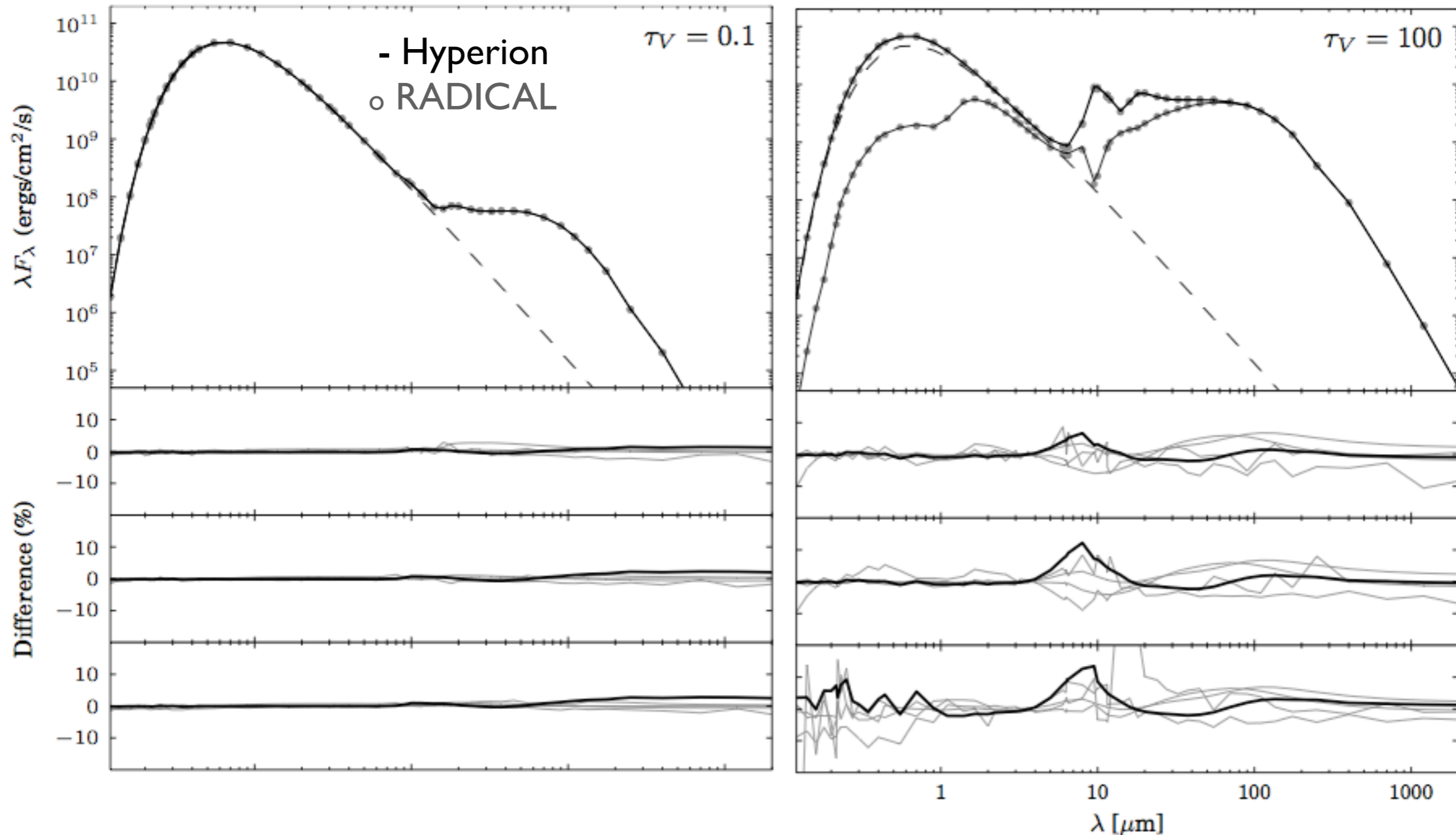
# Hyperion is Parallel

Robitaille 2011

- Scales great:
- Photon packet propagation is “embarrassingly parallel”
- Turnover is set by time of serial part (mostly I/O) of the code



# Test Problems



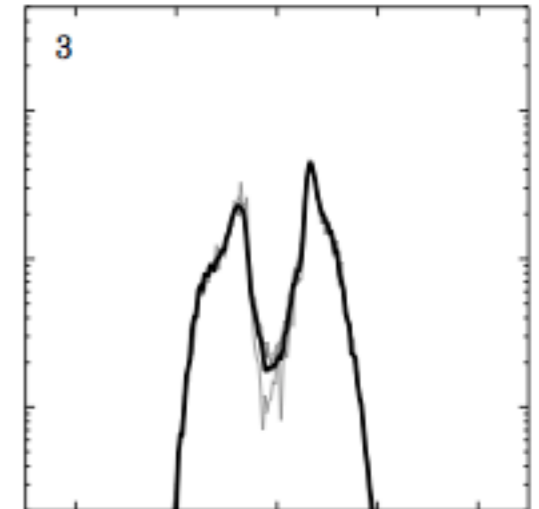
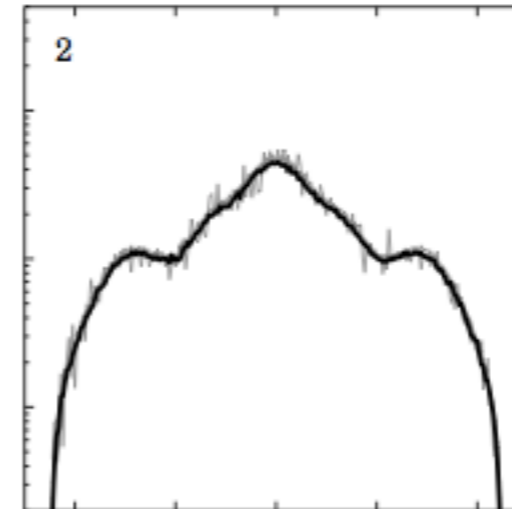
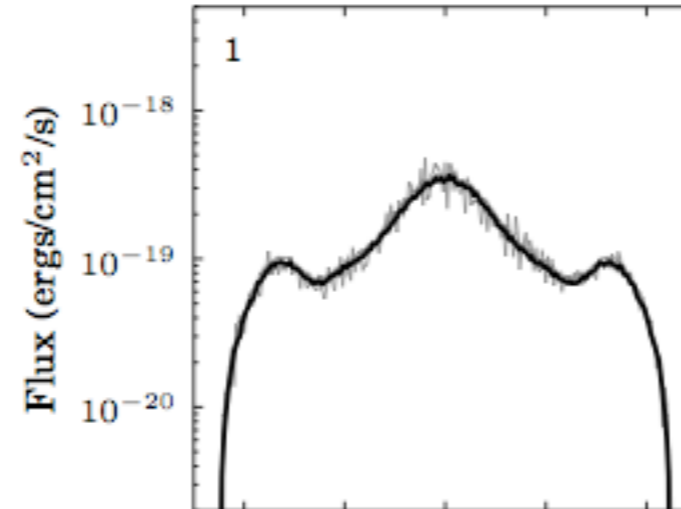
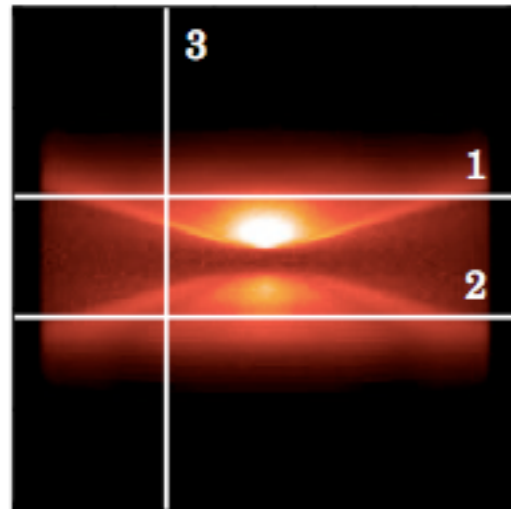
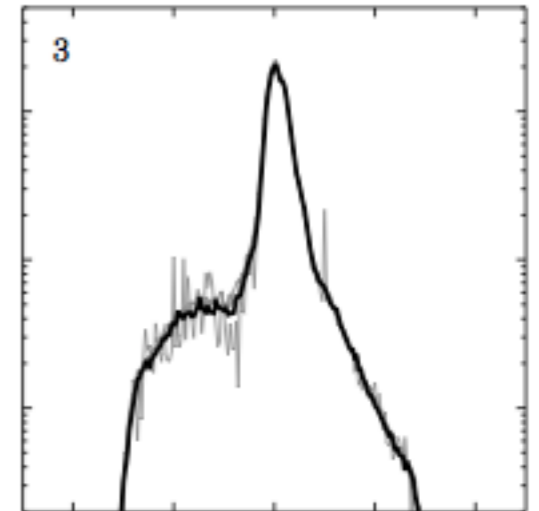
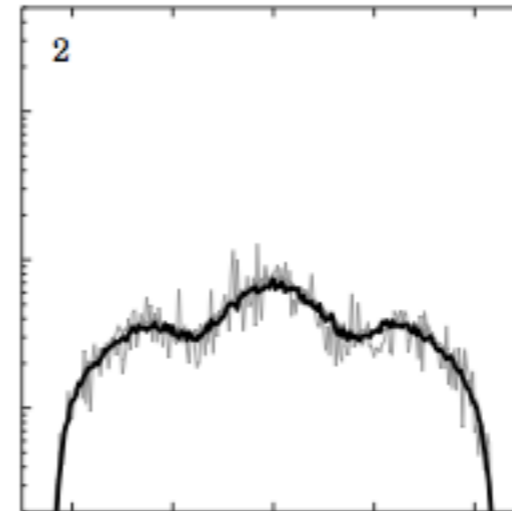
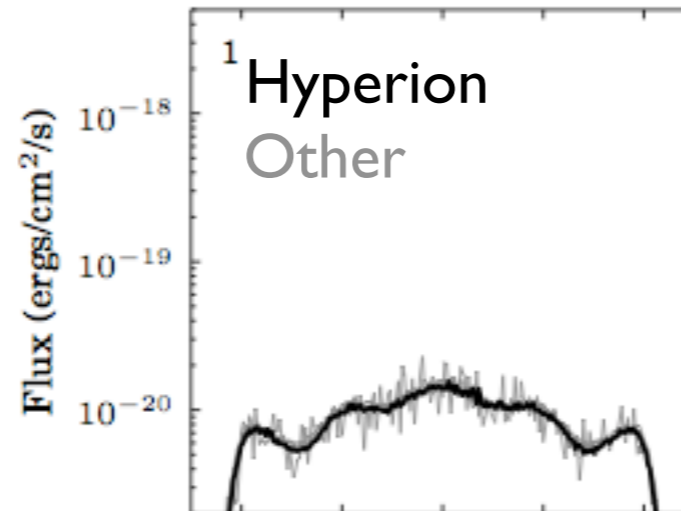
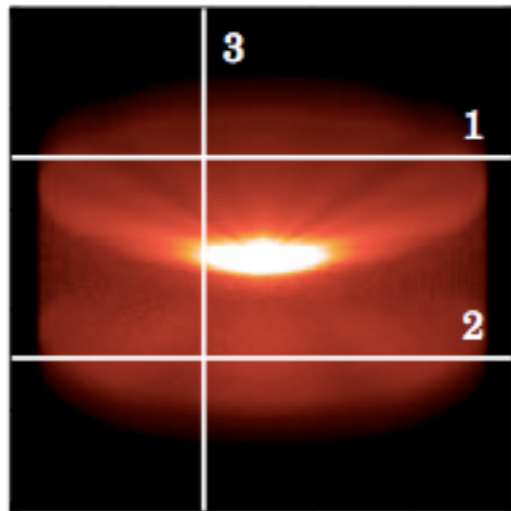
- Pascucci ea 2004, RADICAL; 2D disk bench mark
- Test opacity range with 4 disk masses

Robitaille 2011



# Test Problems

Robitaille 2011

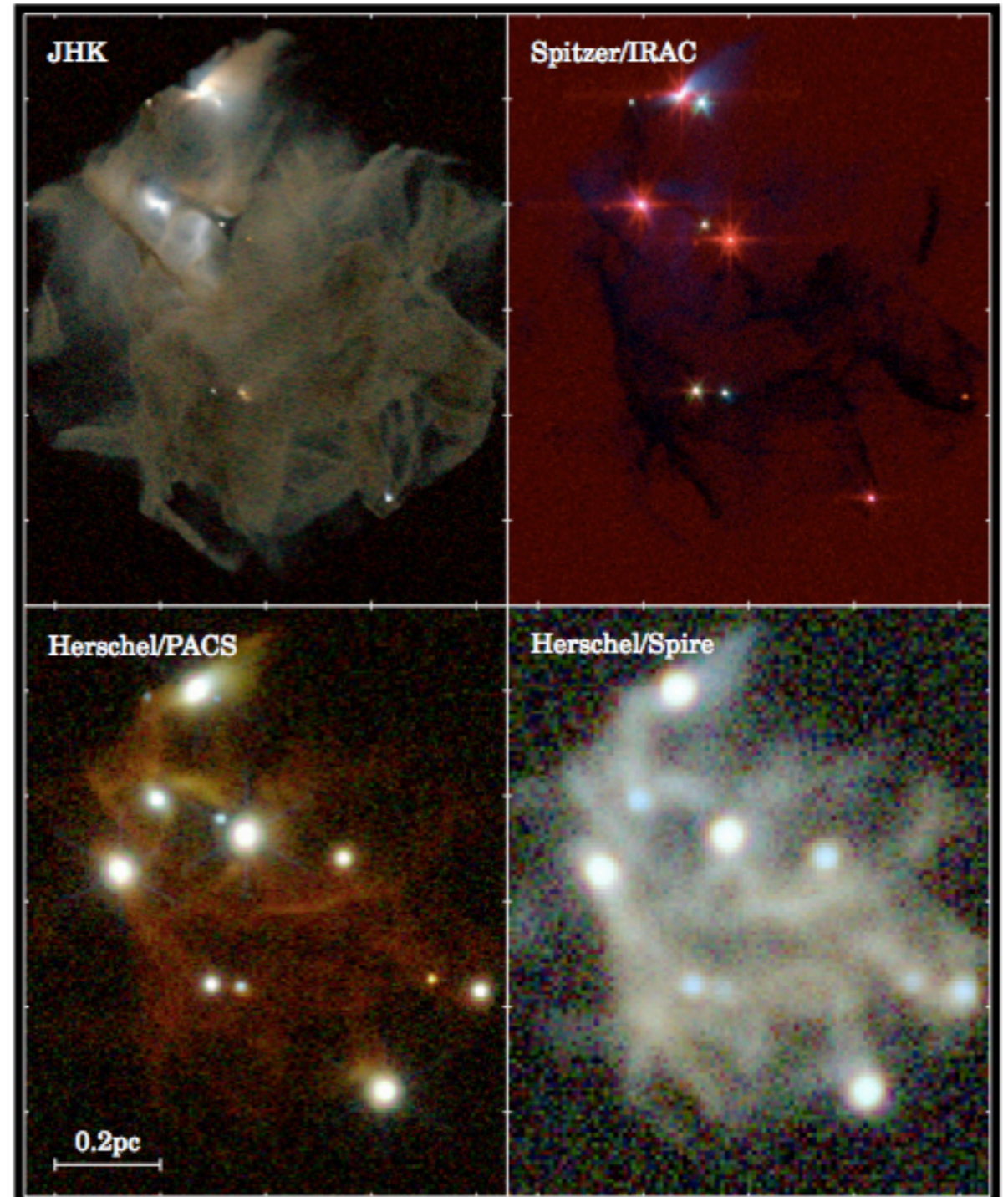
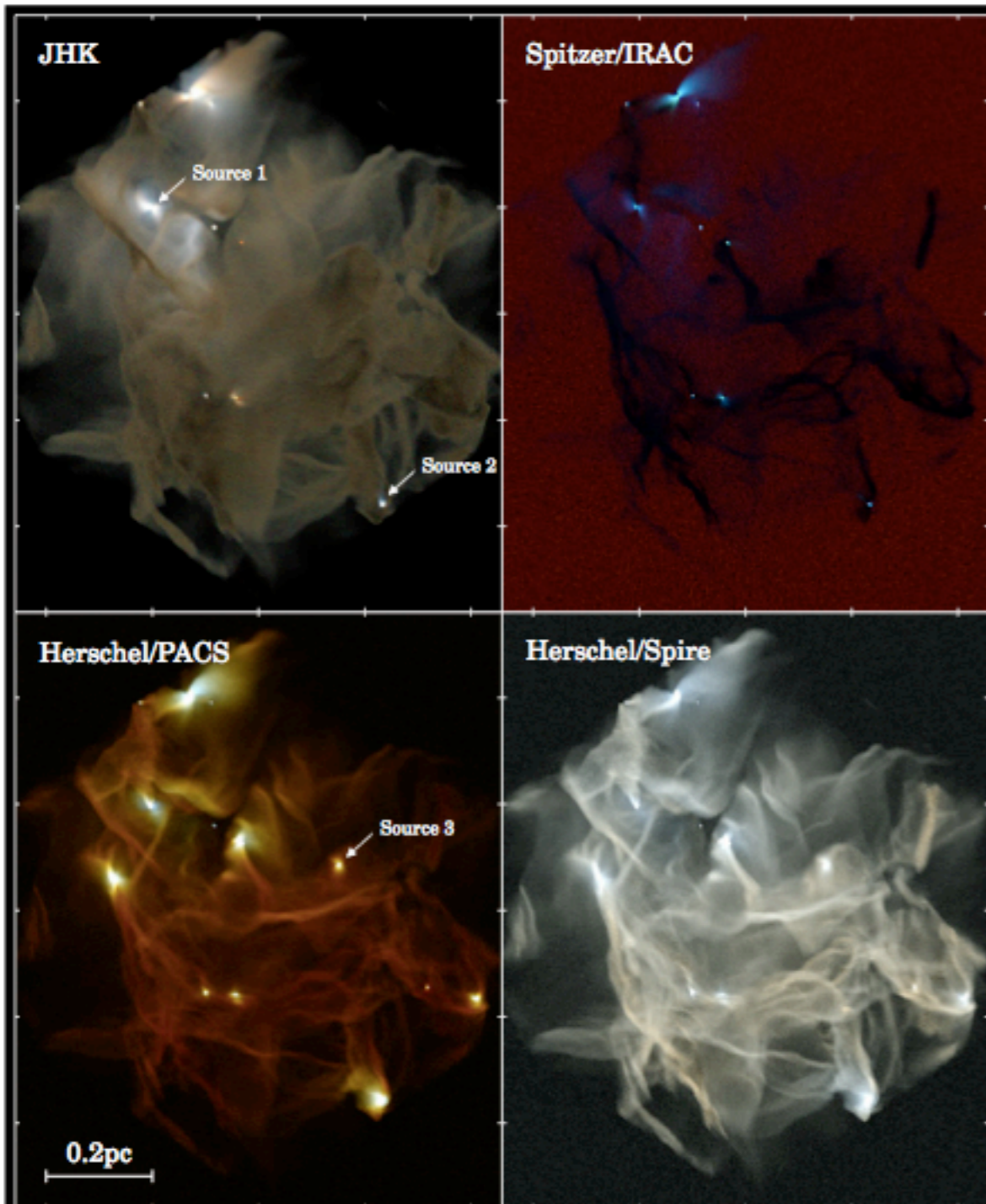


- Pinte et al 2009, MCFOST, MC MAX, TORUS and Pinball codes; disk bench mark
- Tests disk midplane  $\tau_v > 1e6$ , anisotropic scattering, images and polarization

# Application

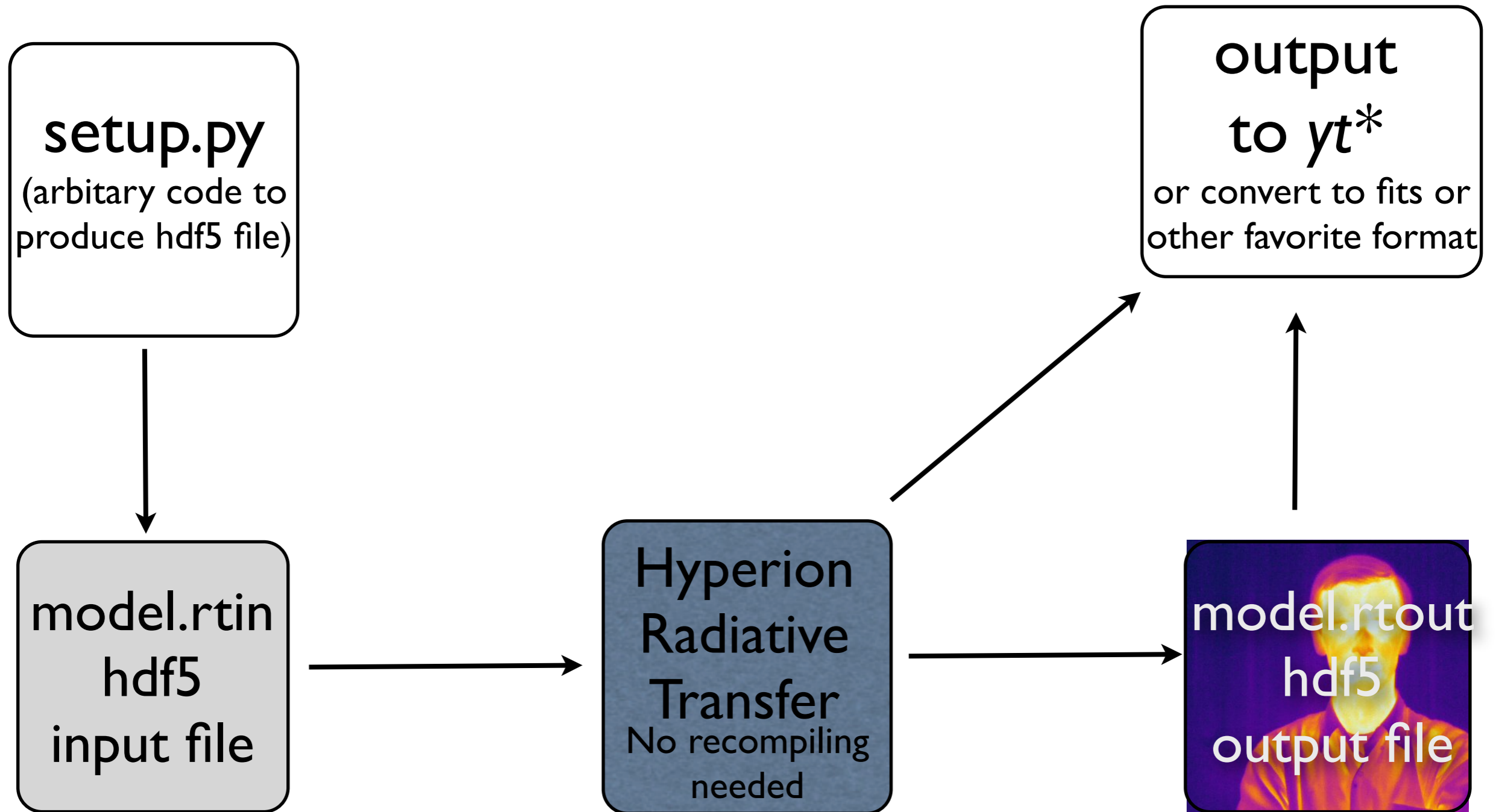
- Synthetic observation of star formation simulation of forming cluster:  
w/ noise, pixel resolution, PSF

Robitaille 2011



Simulation from Offner et al. 2009

# Schematic



\*Hyperion 0.9.2 to be released this week...

## Sample Python Setup Code

# Example

setup.py

The People  
Who Stare  
at Code II

```
import numpy as np
from hyperion.model import Model
from hyperion.util.constants import pc, lsun
```

```
# Initialize model
```

```
m = Model()
```

```
# Set one-cell cartesian grid
```

```
w = np.linspace(-pc, pc, 32)
m.set_cartesian_grid(w, w, w)
```

```
# Add density grid with constant density
```

```
m.add_density_grid(np.ones(m.grid.shape) * 4.e-20, 'kmh_lite.hdf5')
```

```
# Add a point source in the center
```

```
s = m.add_point_source()
s.luminosity = 1000 * lsun
s.temperature = 6000.
```



# Example

**# Add 10 SEDs for different viewing angles**

```
image = m.add_peeled_images(sed=True, image=False) setup.py  
image.set_wavelength_range(250, 0.01, 5000.)  
image.set_viewing_angles(np.linspace(0., 90., 10), np.repeat(20., 10))  
image.set_track_origin('basic')
```

**# Add multi-wavelength image for a single viewing angle**

```
image = m.add_peeled_images(sed=False, image=True)  
image.set_wavelength_range(30, 1., 1000.)  
image.set_viewing_angles([30.], [20.])  
image.set_image_size(200, 200)  
image.set_image_limits(-1.5 * pc, 1.5 * pc, -1.5 * pc, 1.5 * pc)
```

**# Add a fly-around at 500 microns**

```
image = m.add_peeled_images(sed=False, image=True)  
image.set_wavelength_range(1, 499., 501.)  
image.set_viewing_angles(np.repeat(45., 36), np.linspace(5., 355., 36))  
image.set_image_size(200, 200)  
image.set_image_limits(-1.5 * pc, 1.5 * pc, -1.5 * pc, 1.5 * pc)
```

# Example setup.py

**# Set runtime parameters**

```
m.set_n_initial_iterations(5)
```

```
m.set_raytracing(True)
```

```
m.set_n_photons(initial=1e6, imaging=1e7,  
               raytracing_sources=1e6, raytracing_dust=1e6)
```

Needed for calculation of  
dust temperature

**# Write out input file**

```
m.write('tutorial_model.rtin')
```

# Example setup.py

## # Set runtime parameters

```
m.set_n_initial_iterations(5)  
m.set_raytracing(True)  
m.set_n_photons(initial=1e6, imaging=1e7,  
               raytracing_sources=1e6, raytracing_dust=1e6)
```

## # Write out input file

```
m.write('tutorial_model.rtin')
```

Photon # for the specific  
energy calculation

### Rule of Thumb

For optically thin: #PP ~ #cells

For optically thick: #PP ~  
10-100 #cells

# Example setup.py

## # Set runtime parameters

```
m.set_n_initial_iterations(5)
```

```
m.set_raytracing(True)
```

```
m.set_n_photons(initial=1e6, imaging=1e7,  
               raytracing_sources=1e6, raytracing_dust=1e6)
```

## # Write out input file

```
m.write('tutorial_model.rtin')
```



Photon # for the images/SEDs



# Example setup.py

## # Set runtime parameters

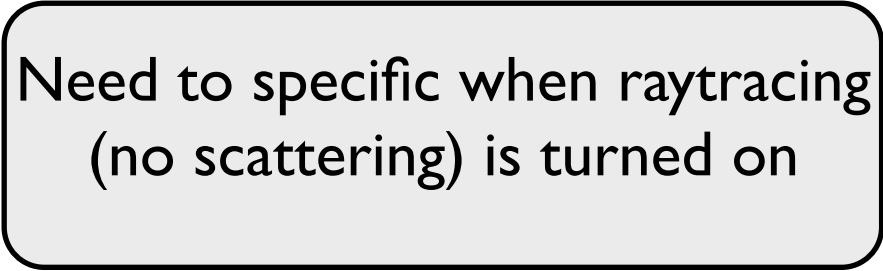
```
m.set_n_initial_iterations(5)
```

```
m.set_raytracing(True)
```

```
m.set_n_photons(initial=1e6, imaging=1e7,  
               raytracing_sources=1e6, raytracing_dust=1e6)
```

## # Write out input file

```
m.write('tutorial_model.rtin')
```



Need to specify when raytracing  
(no scattering) is turned on

# Example

## setup.py

**# Set runtime parameters**

```
m.set_n_initial_iterations(5)
```

```
m.set_raytracing(True)
```

```
m.set_n_photons(initial=1e6, imaging=1e7,  
               raytracing_sources=1e6, raytracing_dust=1e6)
```

**# Write out input file**

```
m.write('tutorial_model.rtin')
```

```
$ python setup.py
```

```
$ hyperion tutorial_model.rtin tutorial_model.rtout
```

or

```
$ mpirun -n 8 -env I_MPI_FABRICS shm:ofa
```

```
hyperion_car_mpi tutorial_model.rtin tutorial_model.rtout
```

# Example

## setup.py

### # Set runtime parameters

```
m.set_n_initial_iterations(5)
m.set_raytracing(True)
m.set_n_photons(initial=1e6, imaging=1e7,
               raytracing_sources=1e6, raytracing_dust=1e6)
```

### # Write out input file

```
m.write('tutorial_model.rtin')
```

```
$ python setup.py
```

```
$ hyperion tutorial_model.rtin tutorial_model.rtout
```

or

```
$ mpirun -n 8 -env I_MPI_FABRICS shm:ofa
```

```
hyperion_car_mpi tutorial_model.rtin tutorial_model.rtout
```

To view outputs:

1) `hdfview tutorial_model.rtout`

2) `hyperion2fits --images tutorial_model.rtout`

# Outline

- Why model dust?
- The physics of dust: emission, absorption & scattering
- Monte Carlo methods
- Hyperion
- Project

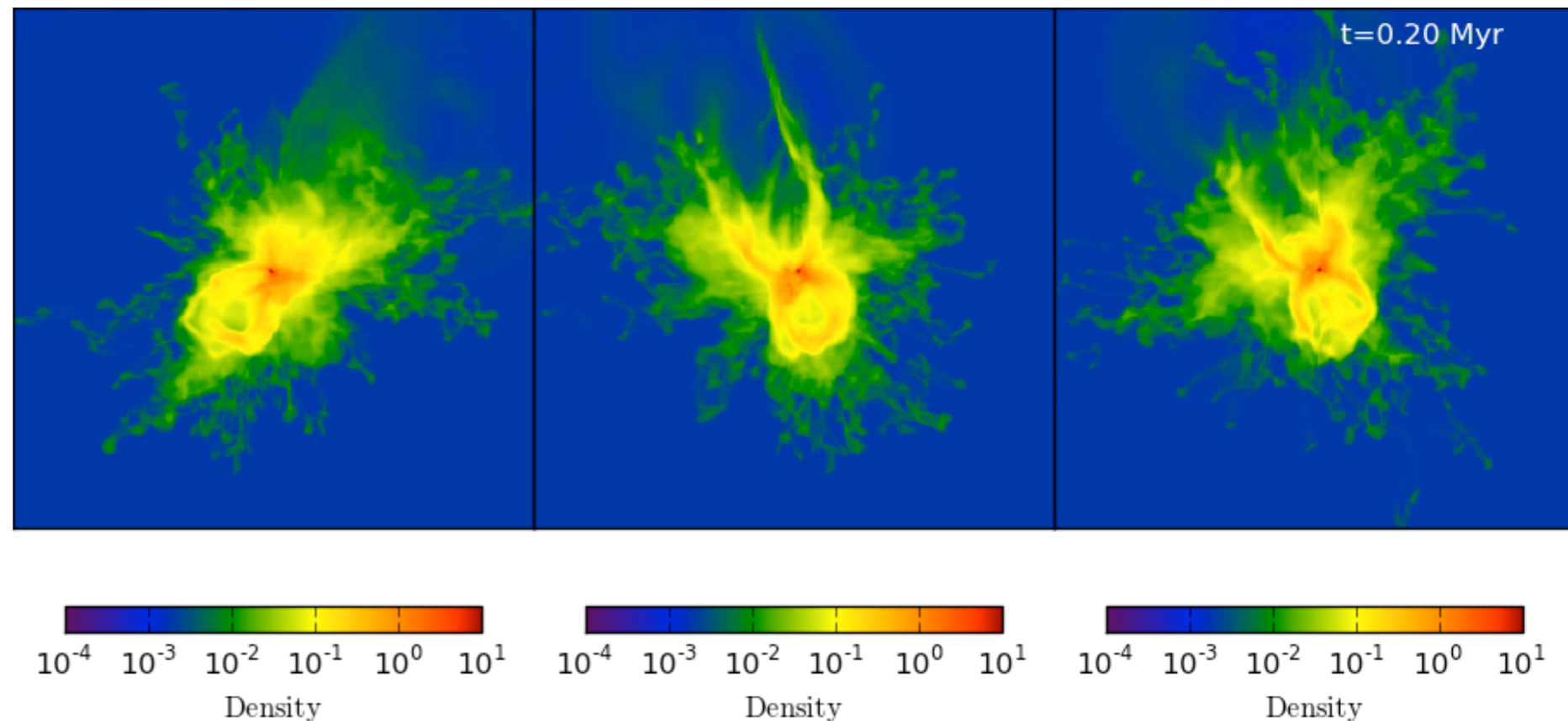
# Project: Multi-wavelength images of a protostellar outflow

- Given: a fits file of the density distribution with a  $1 L_{\text{sun}}$  protostellar source at the center
- Use Hyperion to compute an image of emission at several wavelengths along one (or more) sight-lines. Extract the estimated 3D dust temperature distribution.

Questions to answer:

(1) How many photons do I need for a converged image or SED?

2) What is the dust temperature distribution?



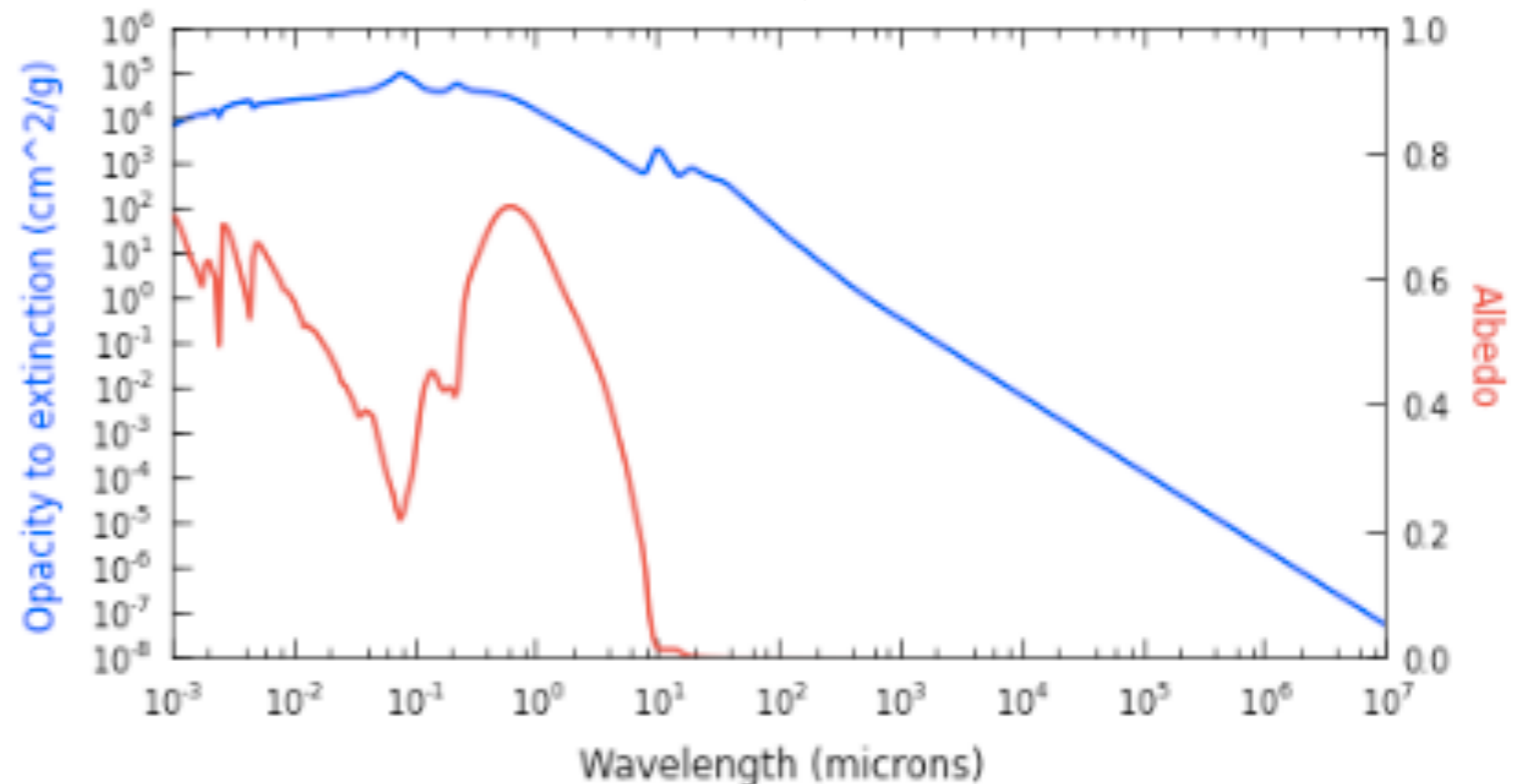
# Project: Multi-wavelength images of a protostellar outflow

- Source code in: `/home/soffner/hyperion-0.9.1/`
- Project stuff: `/home/soffner/hyperion-0.9.1/docs/tutorials/hipacc`

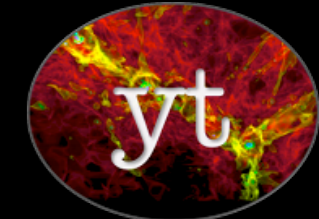
Contains:

Fits gas density file,  
hdf5 dust file,  
README

$R_V=5.5$ , abundance and size distribution from Weingartner & Draine 2001



# Outflow Temperature



160

hyperion

Temperature [K]

80

40

20

-16

-17

-18

-19

-20

Log10(Density) [cgs]

T. Robitaille  
& S. Offner

200 AU



# Useful References

- Journal articles: B. Whitney et al. 2003ab, T. Robitaille 2011, Weingartner & Draine 2001, Draine 2003abc
- Books: *Physics of the Interstellar and Intergalactic Medium*, Bruce Draine; *The Physics and Chemistry of the Interstellar Medium*, A. Tielens
- [help@hyperion-rt.org](mailto:help@hyperion-rt.org).